





Quantum simulation of colour in perturbative QCD

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Based on arXiv:2303.04818

In collaboration with Mathieu Pellen

Outline

- 1. Introduction
- 2. Basics of quantum computing
- 3. Quantum circuits for colour
 - Overview
 - Details
- 4. Results/validation
- 5. Outlook and summary





Outline

Introduction

- Why perturbative QCD?
- Why quantum computers?
- Why now?
- Proposed applications of quantum computing in high-energy physics
- 2. Basics of quantum computing
- 3. Quantum circuits for colour
 - Overview
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Why perturbative QCD?

- High-precision predictions for colliders like the LHC
 - Stringent tests of the standard model
 - Could give first hints of new physics
 - High precision is worthwhile in its own right!
- Computationally intense
 - e.g. multi-loop amplitude calculations
 - e.g. Monte-Carlo integration of cross sections





What can quantum computers do?

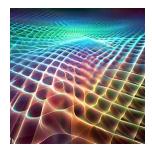
- Prime factorisation
- Unstructured search
 - e.g. searching abstract spaces
 - e.g. Monte-Carlo integration
- Simulating quantum systems
 - Computational chemistry
 - Condensed matter systems
 - Lattice QFT/QCD
- Machine learning















Why now?

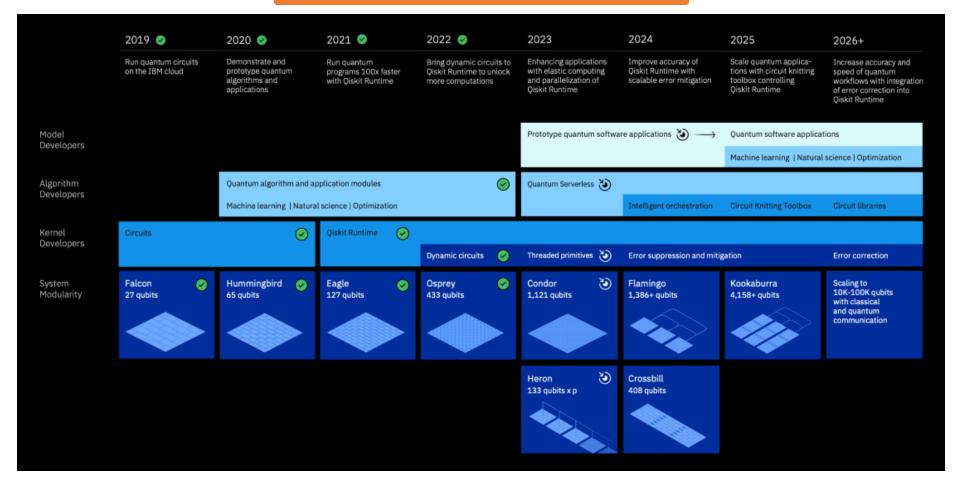
- Hardware progress
 - Trapped ions
 - Neutral atoms
 - Photonic systems
 - Superconducting systems
 - ...
- Software progress
 - e.g. Error-correcting codes (e.g. "surface codes")
- Commercial interest





Why now?

IBM Quantum Development Roadmap

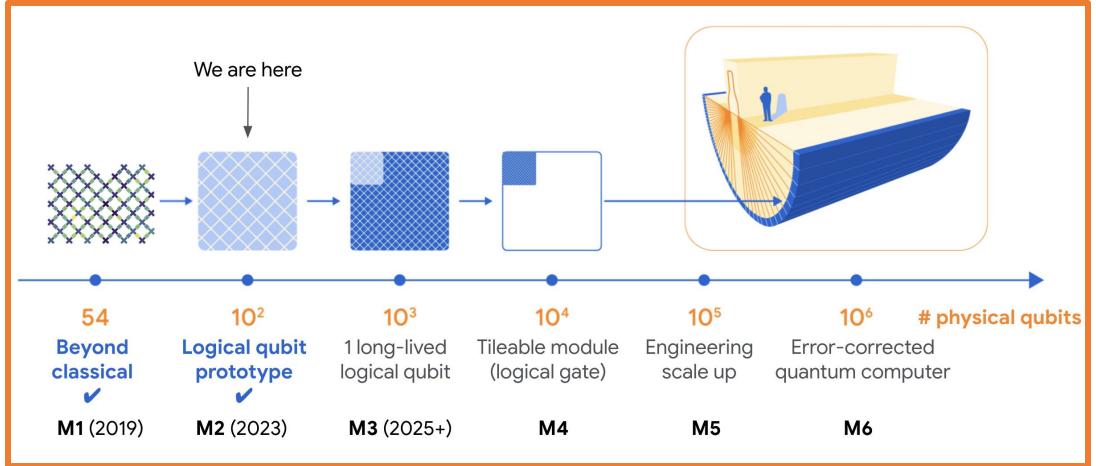






Why now?

Google's quantum roadmap







Proposed applications in high-energy physics

- Experiments / data analysis
- PDFs [Pérez-Salinas, Cruz-Martinez, Alhajri, Carrazza, '20], [QuNu Collaboration, '21]
- EFTS [Bauer, Freytsis, Nachman, '21]
- Monte Carlo for cross-sections [Agliardi, Grossi, Pellen, Prati, '22]
- Parton showers [Bauer, de Jong, Nachman, Provasoli, '19], [Bepari, Malik, Spannowsky, Williams, '20], [Gustafson, Prestel, Spannowsky, Williams, '22]
- Event generation [Gustafson, Prestel, Spannowsky, Williams, '22], [Bravo-Prieto, Baglio, Cè, Francis, Grabowska, Carrazza, '21], [Kiss, Grossi, Kajomovitz, Vallecorsa, '22]
- Lattice QCD (See reviews [Klco, Roggero, Savage, '21] and [Bauer et al., '22] and references therein)
- More [Cervera-Lierta, Latorre, Rojo, Rottoli, '17], [Ramírez-Uribe, Rentería-Olivo, Rodrigo, Sborlini, Vale Silva, '21], [Fedida, Serafini, '22], [Clemente, Crippa, Jansen, Ramírez-Uribe, Rentería-Olivo, Rodrigo, Sborlini, Vale Silva, '22]





Spotlight: quantum simulation

- Quantum simulation: a flagship application of quantum computers
- Recent years: proposals for quantum simulation of lattice QFTs (e.g. lattice QCD)
- Quantum simulation of perturbative QCD remains largely unexplored
 - Notable exception: several papers on parton showers
- This talk: first steps towards generic perturbative QCD processes
 - Quantum simulation of colour in perturbative QCD





Motivation for quantum simulation of pQCD

- 1. Perturbative QCD requires quantum-coherent combination of contributions from many unobservable intermediate states
 - natural candidate to exploit superpositions of quantum states in quantum computers
- 2. Processes with high-multiplicity final states, with full interference effects
- Improve speed/precision of perturbative QCD predictions by exploiting known quantum algorithms
 - e.g. quantum amplitude estimation; quantum Monte Carlo





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What QCs can and cannot do

Formally, no more than a Turing machine

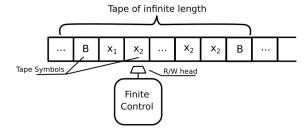


Figure from: opengenus.org

• But QCs are potentially faster for certain problems





Quantum circuit model

- Qubits
- Gates
 - Unitary, reversable
 - Can be controlled by other qubits

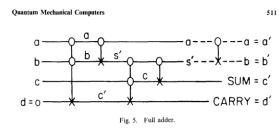
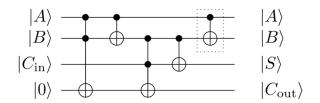


Figure from: Feynman, R.P. Quantum mechanical computers. Found Phys **16**, 507–531 (1986)



Operator	Gate(s)		Matrix
Pauli-X (X)	$-\mathbf{x}$	-—	$\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$
Pauli-Y (Y)	$-\mathbf{Y}$		$\begin{bmatrix} 0 & -i \\ i & 0 \end{bmatrix}$
Pauli-Z (Z)	$-\boxed{\mathbf{z}}-$		$\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$
Hadamard (H)	$- \boxed{\mathbf{H}} -$		$rac{1}{\sqrt{2}} egin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$
Phase (S, P)	$-\!\!\left[\mathbf{s}\right]\!\!-\!\!$		$\begin{bmatrix} 1 & 0 \\ 0 & i \end{bmatrix}$
$\pi/8~(\mathrm{T})$	$-\!\!\left[\mathbf{T}\right]\!\!-\!\!$		$\begin{bmatrix} 1 & 0 \\ 0 & e^{i\pi/4} \end{bmatrix}$
Controlled Not (CNOT, CX)	<u> </u>		$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$
Controlled Z (CZ)			$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \end{bmatrix}$
SWAP			$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$
Toffoli (CCNOT, CCX, TOFF)			$\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0$





Example: the increment circuit

$$|k\rangle \to |k+1 \pmod{2^N}\rangle$$

• Examples:

- $|00000\rangle \rightarrow |00001\rangle$
- $|01011\rangle \rightarrow |01100\rangle$
- $|11111\rangle \rightarrow |00000\rangle$ (overflow)
- $\stackrel{\bullet}{\underset{|\alpha|^2+|\beta|^2}{}} \stackrel{\alpha|00000\rangle+\beta|01011\rangle}{\rightarrow} \stackrel{\alpha|00001\rangle+\beta|01100\rangle}{\underset{|\alpha|^2+|\beta|^2}{}}$

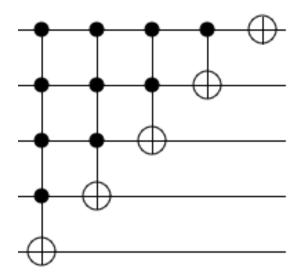


Figure adapted from: algassert.com/circuits/2015/06/12/Constructing-Large-Increment-Gates.html





Example: the increment circuit

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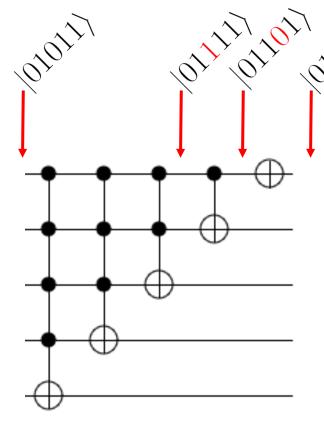


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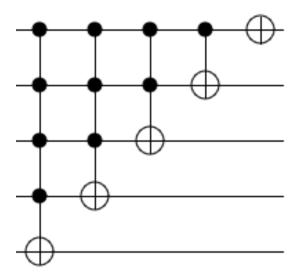


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Outline

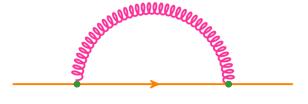
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Rapid reminder of colour in QCD calculations

- SU(3) structure function fabc at each triple-gluon vertex
- SU(3) generator Ta_{ii} at each quark-gluon vertex
- Trace over unmeasured (unmeasurable) colours
- e.g.



$$\sum_{\substack{a \in \{1, \dots, 8\} \\ j \in \{1, 2, 3\}}} T_{ij}^a T_{jk}^a$$

• Note: the large-N_c expansion is <u>not</u> used in this work





Idea: can Gell-Mann matrices become gates?

$$\lambda^{1} = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \quad \lambda^{2} = \begin{pmatrix} 0 & -i & 0 \\ i & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \quad \lambda^{3} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix},$$

$$T_{ij}^a = \frac{1}{2}\lambda_{ij}^a$$

$$\lambda^4 = \begin{pmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix}, \quad \lambda^5 = \begin{pmatrix} 0 & 0 & -i \\ 0 & 0 & 0 \\ i & 0 & 0 \end{pmatrix}, \quad \lambda^6 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix},$$

$$\lambda^7 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & -i \\ 0 & i & 0 \end{pmatrix}, \quad \lambda^8 = \frac{1}{\sqrt{3}} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -2 \end{pmatrix}.$$

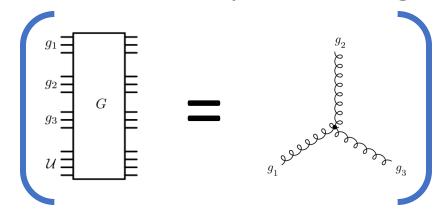
- Short answer: yes, but there are complications:
 - Not 2ⁿ x 2ⁿ
 - Not unitary

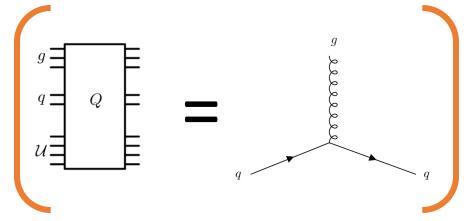




Key results of this work

• Two quantum gates (G and Q) to simulate colour parts of the interactions of quarks and gluons









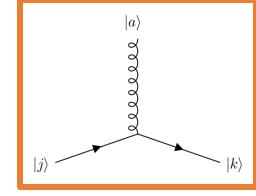
Methods

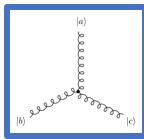
- Quark colours: represented by 2 qubits $(2^2 = 4 \text{ basis states}, \text{ of which 1 is unused})$
- Gluon colours: represented by 3 qubits $(2^3 = 8 \text{ basis states})$
- Quark-gluon interaction gate is designed such that

$$Q|a\rangle_{g}|k\rangle_{q}|\Omega\rangle_{\mathcal{U}} = \sum_{j=1}^{3} T_{jk}^{a}|a\rangle_{g}|j\rangle_{q}|\Omega\rangle_{\mathcal{U}} + (\text{terms orthogonal to } |\Omega\rangle_{\mathcal{U}})$$

Triple-gluon interaction gate is designed such that

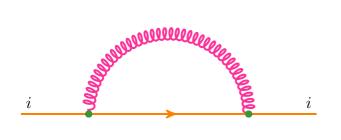
$$G|a\rangle_{g_1}|b\rangle_{g_2}|c\rangle_{g_3}|\Omega\rangle_{\mathcal{U}} = f^{abc}|a\rangle_{g_1}|b\rangle_{g_2}|c\rangle_{g_3}|\Omega\rangle_{\mathcal{U}} + (\text{terms orthogonal to } |\Omega\rangle_{\mathcal{U}})$$

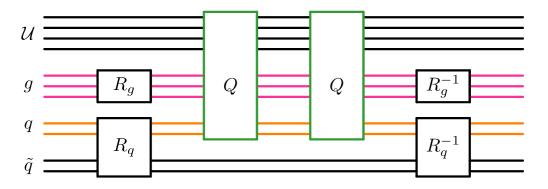




• Note: $|\Omega\rangle_{\mathcal{U}}$ is a reference state of a "Unitarisation register", which we introduce because in SU(3), T_{ik}^a and f_{ik}^{abc} are non-unitary.

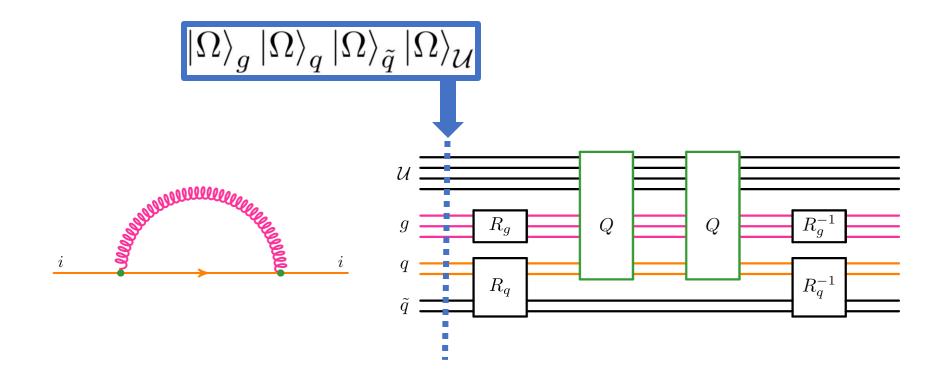






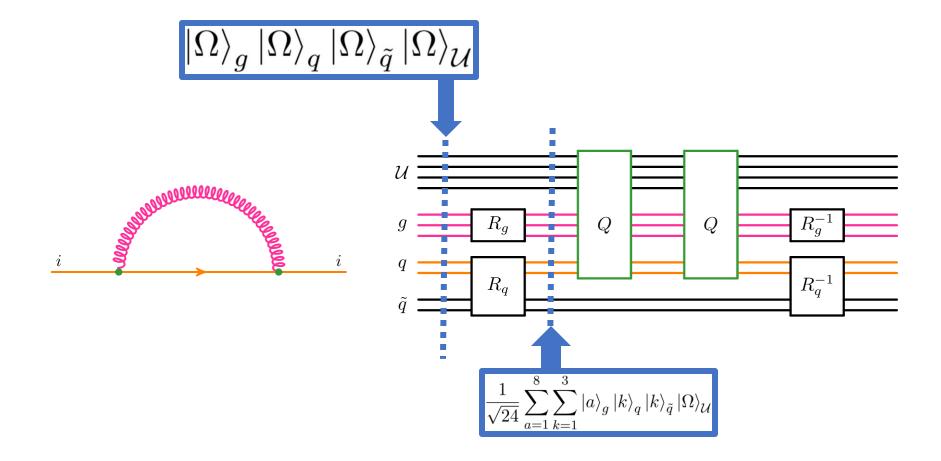






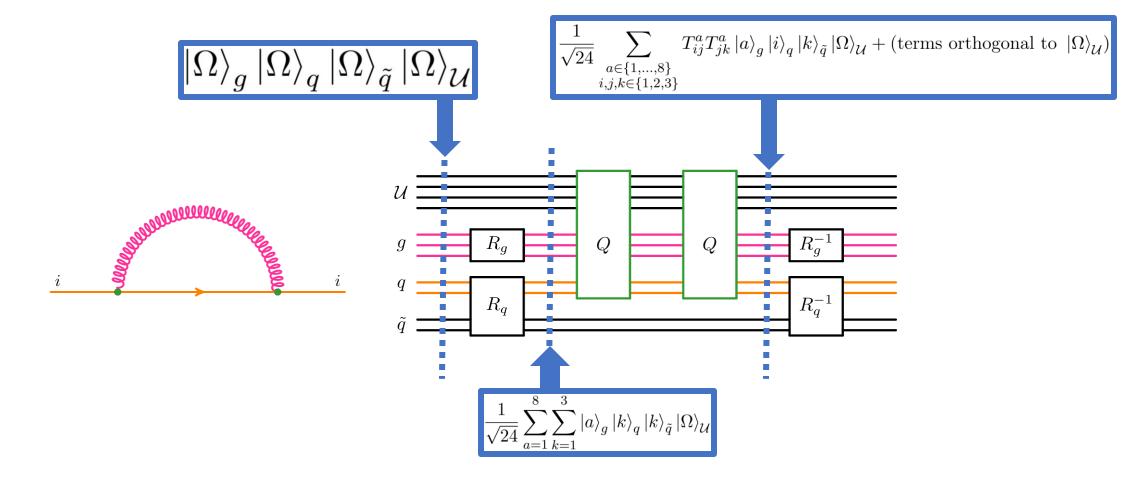






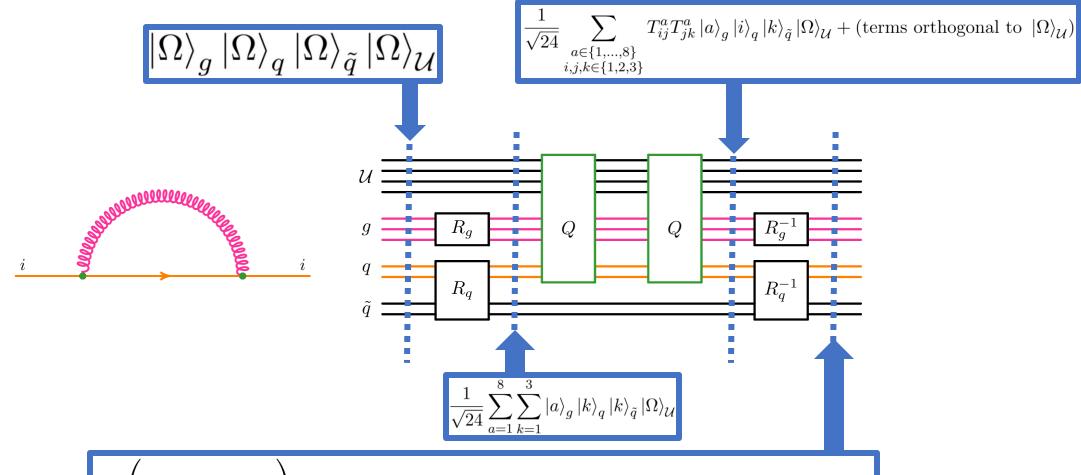






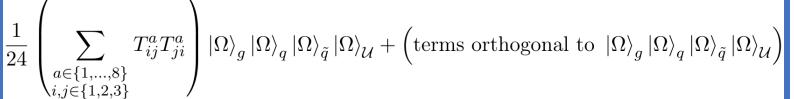


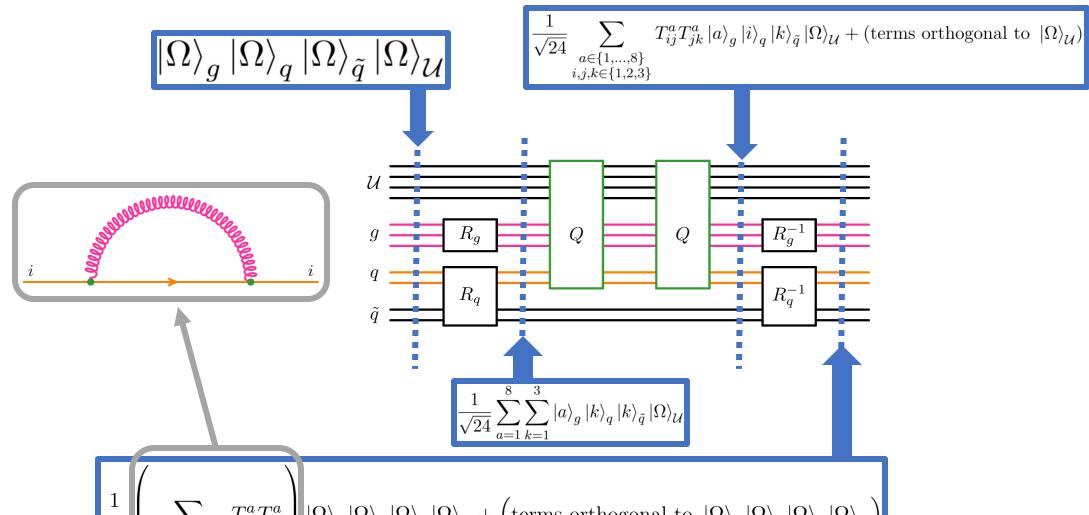
















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 - Non-unitary matrices
 - Constructing the Q and G gates
 - General algorithm for calculating colour factors for arbitrary Feynman diagrams
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Non-unitary operators in perturbative QCD

Would like quantum gates for the 8 linear operators

$$|j\rangle_q \to \sum_i T^a_{ij} |i\rangle_q$$

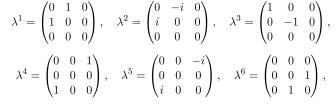
and also for the (diagonal) operator

$$|a\rangle_{g_1}|b\rangle_{g_2}|c\rangle_{g_3} \to f^{abc}\,|a\rangle_{g_1}|b\rangle_{g_2}|c\rangle_{g_3}$$

- An operator is unitary iff the rows of its matrix representation are orthonormal
 - In matrices Taii and fabc, rows are orthogonal
 - But not necessarily of unit norm
- Need a unitary way to alter a state's norm







$$\lambda^7 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & -i \\ 0 & i & 0 \end{pmatrix}, \quad \lambda^8 = \frac{1}{\sqrt{3}} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -2 \end{pmatrix}.$$

Recall:

Unitarisation register: expanding the space

- Let L be an operator acting on a Hilbert space \mathcal{H}_1
- ullet If L is non-unitary, it cannot be directly implemented as a circuit
- But it may be possible to define a new unitary operator \hat{L} acting on a larger space $\mathcal{H}_1\otimes\mathcal{H}_{\mathcal{U}}$ such that

$$\langle \Omega |_{\mathcal{U}} \langle \chi_2 | \hat{L} | \chi_1 \rangle | \Omega \rangle_{\mathcal{U}} = \langle \chi_2 | L | \chi_1 \rangle$$
 for some state $|\Omega_{\mathcal{U}}\rangle \in \mathcal{H}_{\mathcal{U}}$ for all states $|\chi_1\rangle, |\chi_2\rangle \in \mathcal{H}_1$

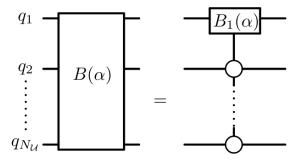
• In this work, we introduce a single additional register \mathcal{U} , whose size is small: $N_{\mathcal{U}} = \lceil \log_2(N_V + 1) \rceil$





Unitarisation register: gates A and B

- Let A denote the increment circuit described earlier
- Define a gate $B(\alpha)$:



where:

$$B_1(\alpha) = \begin{pmatrix} \sqrt{1 - |\alpha|^2} & \alpha \\ -\alpha & \sqrt{1 - |\alpha|^2} \end{pmatrix}$$





Unitarisation register: key properties

• Together, gates A and B(α) act on \mathcal{U} in the following way:

$$B(\alpha)A|k\rangle = \begin{cases} \alpha|0\rangle + \sqrt{1 - |\alpha|^2}|1\rangle & \text{if } k = 0\\ |k+1\rangle & \text{if } 0 < k < 2^{N_{\mathcal{U}}} - 1\\ \sqrt{1 - |\alpha|^2}|0\rangle - \alpha|1\rangle & \text{if } k = 2^{N_{\mathcal{U}}} - 1. \end{cases}$$

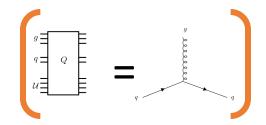
which means we can apply B(α)A repeatedly up to $2^{N_{\mathcal{U}}}-1$ times and satisfy

$$\langle \Omega |_{\mathcal{U}} \prod_{i=1} \{ B(\alpha_i) A \} | \Omega \rangle_{\mathcal{U}} = \prod_{i=1} \alpha_i$$









 $Q|a\rangle_{g}|k\rangle_{q}|\Omega\rangle_{\mathcal{U}} = \sum_{j=1}^{3} T_{jk}^{a}|a\rangle_{g}|j\rangle_{q}|\Omega\rangle_{\mathcal{U}} + (\text{terms orthogonal to } |\Omega\rangle_{\mathcal{U}})$

• Start by defining matrices $\overline{\lambda}_a$

$$\overline{\lambda}_1 = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad \overline{\lambda}_2 = \begin{pmatrix} 0 & -i & 0 \\ i & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad \overline{\lambda}_3 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

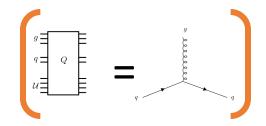
$$\overline{\lambda}_4 = \begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix}, \quad \overline{\lambda}_5 = \begin{pmatrix} 0 & 0 & -i \\ 0 & 1 & 0 \\ i & 0 & 0 \end{pmatrix}, \quad \overline{\lambda}_6 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}$$

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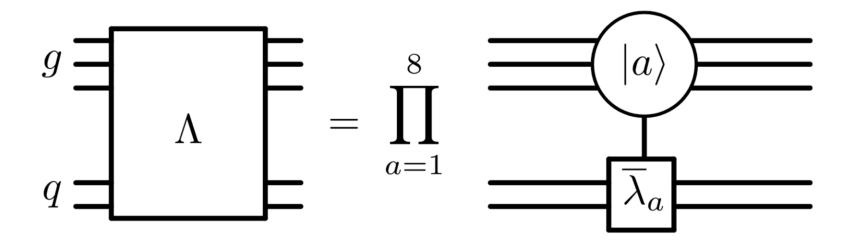


Construction of the Q gate



 $Q\left|a\right\rangle_{g}\left|k\right\rangle_{q}\left|\Omega\right\rangle_{\mathcal{U}}=\sum_{j=1}^{3}T_{jk}^{a}\left|a\right\rangle_{g}\left|j\right\rangle_{q}\left|\Omega\right\rangle_{\mathcal{U}}+\left(\text{terms orthogonal to }\left|\Omega\right\rangle_{\mathcal{U}}\right)$

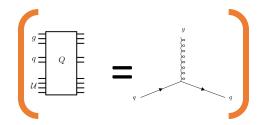
ullet Next, define a gate Λ







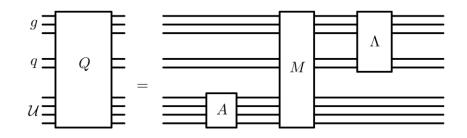
Construction of the Q gate



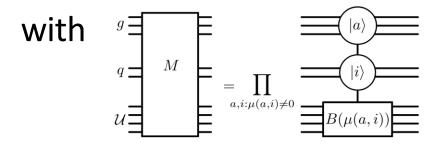
 $Q\left|a\right\rangle_{g}\left|k\right\rangle_{q}\left|\Omega\right\rangle_{\mathcal{U}}=\sum_{j=1}^{3}T_{jk}^{a}\left|a\right\rangle_{g}\left|j\right\rangle_{q}\left|\Omega\right\rangle_{\mathcal{U}}+\left(\text{terms orthogonal to }\left|\Omega\right\rangle_{\mathcal{U}}\right)$



Finally, define the gate Q



Recall: $\langle \Omega |_{\mathcal{U}} B(\alpha) A | \Omega \rangle_{\mathcal{U}} = \alpha$

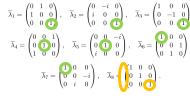


$$\mu(a,i) = \begin{cases} \frac{1}{2} & \text{if } (\overline{\lambda}_a)_{ij} - (\lambda_a)_{ij} = 0 \quad \forall j \\ \frac{1}{2\sqrt{3}} & \text{if } a = 8 \text{ and } i \in \{1,2\} \\ \frac{-1}{\sqrt{3}} & \text{if } a = 8 \text{ and } i = 3 \\ 0 & \text{otherwise.} \end{cases}$$

where μ is defined such that $\mu(a,i)\overline{\lambda}_a |i\rangle = \frac{1}{2}\lambda_a |i\rangle$

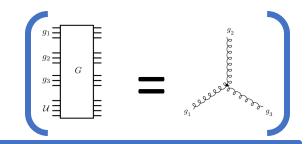
Recall:

Explicitly:



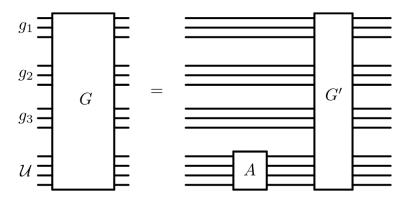






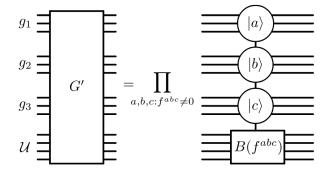
$$G|a\rangle_{g_1}|b\rangle_{g_2}|c\rangle_{g_3}|\Omega\rangle_{\mathcal{U}} = f^{abc}|a\rangle_{g_1}|b\rangle_{g_2}|c\rangle_{g_3}|\Omega\rangle_{\mathcal{U}} + (\text{terms orthogonal to }|\Omega\rangle_{\mathcal{U}})$$

• Define G gate:



Recall:
$$\langle \Omega |_{\mathcal{U}} B(\alpha) A | \Omega \rangle_{\mathcal{U}} = \alpha$$

where:

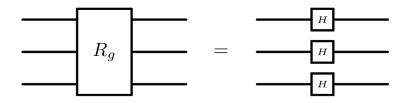






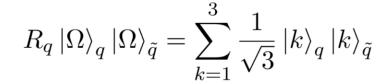
R_q and R_q gates for tracing

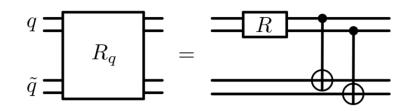
$$R_g |\Omega\rangle_g = \sum_{a=1}^8 \frac{1}{\sqrt{8}} |a\rangle_g$$



$$H = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix}$$

$$R_g^{-1} \sum_{a=1}^{8} c_a |a\rangle_g = \left(\frac{1}{\sqrt{8}} \sum_{a=1}^{8} c_a\right) |\Omega\rangle_g + \left(\text{terms orthogonal to } |\Omega\rangle_g\right)$$





$$R = \begin{pmatrix} \sqrt{\frac{1}{3}} & \sqrt{\frac{1}{2}} & \sqrt{\frac{1}{6}} & 0\\ \sqrt{\frac{1}{3}} & -\sqrt{\frac{1}{2}} & \sqrt{\frac{1}{6}} & 0\\ \sqrt{\frac{1}{3}} & 0 & \sqrt{\frac{2}{3}} & 0\\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$R_q^{-1} \sum_{i,k \in \{1,2,3\}} c_{ik} |i\rangle_q |k\rangle_{\tilde{q}} = \left(\frac{1}{\sqrt{3}} \sum_{i=1}^3 c_{ii}\right) |\Omega\rangle_q |\Omega\rangle_{\tilde{q}} + \left(\text{terms orthogonal to } |\Omega\rangle_q |\Omega\rangle_{\tilde{q}}\right)$$



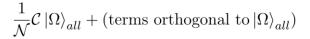


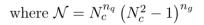
Calculating the colour factor of arbitrary Feynman diagrams

- Build a quantum circuit with:
 - For each gluon, 1 gluon register, with 3 qubits per register
 - For each quark <u>line</u>, a pair of quark registers: q and \tilde{q} , with 2 qubits per register
 - A unitarisation register with $N_{\mathcal{U}} = \lceil \log_2(N_V + 1) \rceil$ qubits
- Initialise each register \mathcal{T} into the state $|\Omega\rangle_r$
- For each gluon, apply R_g
- For each quark, apply R_q
- For each quark-gluon vertex, apply Q gate to the corresponding g and q registers (not \tilde{q})
- For each triple-gluon vertex, apply G gate to the corresponding g registers
- For each gluon, apply (R_g)⁻¹
- For each quark, apply $(R_q)^{-1}$
- Colour factor \mathcal{C} is found encoded in the final state of the quantum computer, which is:









Recall the illustrative example:

Outline

- 1. Introduction
- 2. Basics of quantum computing
- 3. Quantum circuits for colour
 - Overview
 - Details
- 4. Results/validation
- 5. Outlook and summary



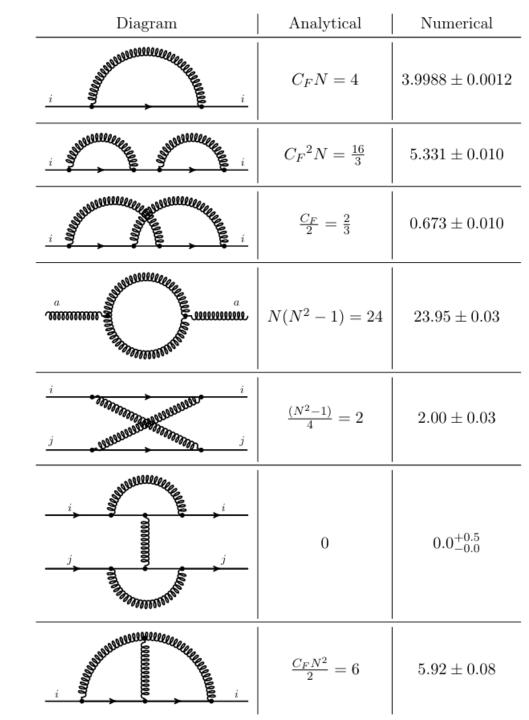


Validation

- Implemented using Qiskit (IBM)
- Simulated various diagrams
 - Simulated noiseless quantum computer
 - These examples use up to 30 qubits
 - Ran each diagram 10⁸ times
 - Measured output to infer colour factor

$$\frac{1}{N}C|\Omega\rangle_{all} + (\text{terms orthogonal to} |\Omega\rangle_{all})$$

Full agreement with analytic expectation







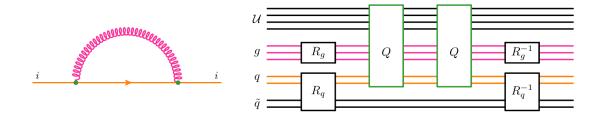
Outlook

- Interference of multiple diagrams
 - Natural application for a quantum computer
 - Can try with/without quantum simulation of kinematic parts
- Kinematic parts
 - Unitarisation register could be useful here too
 - Much larger Hilbert space since kinematic variables are continuous
- High-multiplicity processes
- Monte-Carlo integration of cross-sections
 - quadratic speed-up





Summary and outlook



- Designed quantum circuits to simulate colour part of perturbative QCD
 - Example application: colour factors for arbitrary Feynman diagrams
 - First step towards a full quantum simulation of generic perturbative QCD processes
- Natural avenues for follow-up work:
 - Kinematic parts of Feynman diagrams
 - Interference of multiple Feynman diagrams
 - Use in a quantum Monte Carlo calculation of cross-sections
 - Quadratic speed-up over classical Monte Carlo



