

Electronics for the readout of segmented semiconductor radiation detectors with emphasis on X-ray detector systems

Part 1: Introduction to hybrid pixel detectors Classification of technologies, limitations of hybrid pixel detectors

Part 2: Introduction to signal processing

Part 3: Review of ASICs

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CERN Microelectronics Section 1

Semiconductor Hybrid Pixel Detectors

- A hybrid pixel detector is a 2-dimensional matrix of microscopic radiation-sensitive elements each of which is connected to its own pulse processing electronics.
- The sensor element and the readout electronics are implemented in different substrates i.e. can be optimized separately
	- Sensor material can be changed (Si, GaAs, CdTe)

Chips can be used to readout the signal from other detectors (e.g. MCP)

MCP-based systems can be used to detect visible light photons and soft X-rays (with photocathode) and electrons, ions or neutrons (when e.g. B doped)

Measurements

Information from the incoming beam

- The number of particles deposited during a given exposure time
- The energy deposited by an individual particle
- The time of arrival of the particle

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"Different particles have a different "signature" in their interaction with the detector material"

*a. Alpha particle, b. Muon, c. Electron Timepix data, 55*m*m pixels*

Information from the incoming beam

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- The angle of incidence of the incoming charged particle based on the difference in the induced signal time in the pixels

Outline

Part 1:

- Classification of X-ray detector systems
	- X-ray conversion
	- Signal processing
	- Detector geometry
- The ideal detector system
- Limiting factors in real systems

Part 2:

- Signal chain for readout electronics
- Sensor geometry modelling
- Preamplifier topologies
- The CSA/TIA
- Noise (basic introduction)
- Noise in the MOS transistor
- Noise in a cascade of amplifiers
- Transfer of noise sources to the output of the CSA
- Noise filtering
- CR-RC shaper

Part 3:

- Review of ASICs (full picture)
- Review of ASICs (details)
- Techniques for increasing the count rate
- Techniques for allowing spectroscopic information at fine pixel pitch
- Towards large area detectors
- Summary and conclusions

3 side buttable

4 side buttable

Classification of detector systems: X-ray conversion to electrical signal

X-ray imaging technologies classification: conversion of X-rays

Readout Photodiodes

- 100-1000 e generated in the diode (Interaction depth dependent)
- Degraded energy and spatial resolution
- Cheaper

• 4000-25000 e induced (Medical radiography range) (reproducible)

Classification of detector systems: signal processing

Signal processing in the readout electronics: integrating vs pulse processing

- Energy integration
	- The signal deposited in the sensor is integrated (together with the noise)
	- The weight of each photon in the image is proportional to its energy
	- The system does not suffer from pile up

Signal processing in the readout electronics

- Single Quantum Processing (*See presentation E. Heijne*)
	- Signal from each individual photon is treated on an event-by-event basis
	- Signal attributed to a particle only when it exceeds a threshold (suppression of random electronics noise)
	- Possible measurements: Particle hit, Energy (Amplitude/ToT), Time of Arrival
	- With one threshold level: The weight of each photon in the image is one (photon counting)
	- With multiple thresholds: Spectral imaging (energy resolved information)

Due to the nature of how X-rays are generated in an X-ray tube, the beam that we obtain is polychromatic

The energy dependent attenuation is a signature of a material

Courtesy: S. Procz et al.

Photons in different energy bins give complementary information

Sampling different sections of the polychromatic energy spectrum allows to identify materials in a sample

Classification of detector systems: geometry

X-ray imaging direct conversion detectors geometry

The ideal detector system

The ideal X-ray detector

- Direct detection
	- Increased and reproducible signal, improved spatial resolution
- Signal deposited by a photon should be proportional to the photon energy and localized in a small volume in the detector
- Single quantum processing
	- Photons are detected and classified in a plurality of energy bins
	- That leads to possibility to energy weighting (optimal SNR), noise rejection, perfect linear behaviour
- Zero dead time (τ)
	- Limitation of single quantum processing
	- $-$ For a given application τ < \leq 1/r (τ is the dead time, r is the count rate and 1/*r* is the mean time between consecutive photons)

Limiting factors in real systems degrading spatial, time and energy resolution and count rate

3. Charge diffusion

Absorption efficiency

$$
100(1 - \frac{I}{I_0}) =
$$

100(1 - e^{-(\mu/\rho)\rho x})

x is the *thickness*

 μ is the *linear attenuation* coefficient (units: distance⁻¹) (inverse of the mean free path)

 ρ is the *density* of the material

 μ/ρ is the mass attenuation coefficient

- Silicon (Z=14) ideal for charged particle detection in many applications (homogeneity, availability, cost)
- Higher Z required above 20keV (unless edge on geometry is used)
- Ge (Z=32), GaAs (Z=31,33), CdTe (Z=48,52), CdZnTe

Charge diffusion

- Diffusion occurs when there are local differences of carrier concentrations in the semiconductor
	- Gaussian cross section of the distribution with standard deviation:

$$
\sigma = \sqrt{\sigma_0^2 + 2Dt}
$$

$$
D = \mu \frac{KT}{q}
$$

$$
t = \frac{d}{\mu E}
$$

D: Diffusion coefficient t: time

Diffusion enhanced by Coulombic repulsion 1

Charge density distribution (hole component) (Charges/cm³), Si sensor, deposition at 50um, 4ns and 14ns after conversion (Thesis L. Tlustos)

1X. Lai et al. "CZT modeling for photon counting computer tomography" <https://doi.org/10.1117/12.2512531>

Charge diffusion

Fluorescence

Mean free path of fluorescence photon \lim Fluorescence yield $\frac{1}{2}$

9.25 10.54

23.17

27.47

9.22

40.62 15.62

113.20

59.32

40.28 15.47

110.75

57.85

50.5 56.6

83.6

87.3

10.50

22.98

27.20

The fluorescence yield increases with the atomic number

GaAs Ga, 48.20%

CdTe Cd, 46.84%

As, 51.80%

Te, 53.16%

31 33

48 52 10.36 11.87

26.71

31.81

The mean free path of the fluorescence photons is in the same order of magnitude as the pixel pitch for high-Z materials

1.11 1.32

3.53 4.34

Implications: degradation of the energy measurement, blur the image

1.14 1.36

3.73 4.61

> *Table: L. Tlustos, PhD thesis* 33

Signal induction

Induced charge on detector electrodes

- Signals on detector electrodes arise from motion of charge carriers
- Induced current is derived from laws of electrostatics

Induced charge on detector electrodes

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Signal induction in the pixel electrodes

- 1mm CdTe
- 60keV photon
- 600V sensor bias
- Energy deposition at $z=240 \mu m$
- (No charge trapping, charge sharing included in simulation)

Signal shape depends on detector geometry

0.2 **pixel effect** 0.4 **Ramo theorem: The small Consequence of Shockley**ns
m
C

pixel surface that 0 electrode. induced on the pixel 40 to most of the charge electrodes will contribute to the induced charge. Integra
Integra
Integra It is the motion close to the contributes most strongly The carrier that drifts towards the pixel

Message: The geometry of the sensor (pitch/thickness) determines the shape of the induced current

Information from the incoming beam

- The number of particles deposited during a given exposure time
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Ballistic deficit

Ballistic deficit refers to the loss of signal amplitude at the shaper output due to an incomplete integration of the sensor signal by the readout electronics

42 Mathematical model (other effects like charge sharing are not included).

Channel i

- Pile-up is the overlap in the processing chain, of the signals due to two consecutive photons
- The mean time between consecutive photons (μ) follows exponential probability density function

The impact of pulse pile up is on an incorrect number of recorded photons and also a distortion in the measured energy spectrum

Dead time models

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These models represent an idealized system behaviour. Real counting systems will often display a behavior that is intermediate between these extremes. Assumptions: 1. events arrive following Poisson statistics with average true interaction rate n, 2. Signals are rectangle-like shaped of duration .

G.F. Knoll, Radiation Detection and Measurement Inc., 2000, Chapter 3.

Summary and conclusions

- We reviewed hybrid pixel detector systems (with emphasis on X-ray detection)
- We classified them in terms of
	- X-ray conversion
	- Signal processing
	- Detector geometry
- The ideal detector system
- The limiting factors in real systems

Part 1: Introduction to hybrid pixel detectors

Classification of technologies, limitations of hybrid pixel detectors

Part 2: Introduction to signal processing

Thanks to D. Gascón (ICCUB), A. Rivetti (INFN), J. Kaplon (CERN), P. O'Connor (BNL)

Part 3: Review of ASICs

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CERN Microelectronics Section

Signal chain for readout electronics

- The sensor converts the energy (or part of it) of an incoming particle into an electrical signal and delivers a small signal (fC)
- The front-end amplifier and shaper
	- amplifies and shapes the signal (optimizing the signal to noise ratio and ability to deal with flux)
	- ensures an efficient signal transfer in presence of parasitic elements between adjacent channels (ensuring low cross talk).
- The stages following the front-end amplifier extract the information from the signal about the incoming quanta in a quantized domain
	- Energy (ADC)
	- Time of arrival (TDC)
	- Number of particles above threshold
	- Location, particle type
- In modern detectors, this is done in systems containing thousands of channels (low power)

Requirements for readout electronics

Reliability, Radiation hardness, Low material, Low Cost

Sensor geometry modeling

The (simplified) detector model

• **Signal:**

- Radiation event creates charges in the detector volume
- **i SENSOR represents the currents induced in the sensing electrodes by the charge carriers moving in the detector volume**
- It is usually modeled as a $\delta(t)$, which is convenient because it allows to study the front-end electronics impulse response
- The model is adequate if the impulse response of the electronics is long compared to the signal delivered by the sensor
- The polarity of the source has to be accounted for
- $\alpha_{\sf IN}$ depends on the interaction of the particle with the sensor material (For photons in Si: Qin=E_y/ ε , for MIPS 60-80e⁻ /h⁺ /mm (Presentation E. Heijne, L. Pancheri))
- **Leakage (semiconductor detectors)**
	- e-/h+ pairs thermally generated in the depletion region and swept by the electric field
	- The discrete nature of carriers crossing a junction intrinsically implies some fluctuations in their number (*shot noise*)
- **Capacitance: determines the system performance**
	- Monolithic Active Pixel Sensors (~1fF), Hybrid Pixel Detectors (10s of fF), Strips Detectors (~pF), PMT (10s of pF), SiPMs (pF-nF)
- Interconnect parasitics and accurate models for the sensor signal required especially for precise timing measurements.

Example 1: The detector model for a hybrid pixel detector

R. Ballabriga et al. "The Timepix4 Analog Front-end Design: Lessons learnt on Fundamental Limits to Noise and Time Resolution in Highly Segmented Hybrid Pixel Detectors" <https://doi.org/10.1016/j.nima.2022.167489>

* G. Gorfine et al., "Capacitance of silicon pixels", Nucl. Instrum. Methods Phys. Res. A 460 (2) (2001) 336–351.

Example 2: The detector model

The model can be adapted to other sensor geometries

R. Ballabriga et al. "The Timepix4 Analog Front-end Design: Lessons learnt on Fundamental Limits to Noise and Time Resolution in Highly Segmented Hybrid Pixel Detectors" <https://doi.org/10.1016/j.nima.2022.167489>

Example 3: Importance of the details in high performance measurements: timing for high energy charged particle detection

The $\delta(t)$ model is convenient and widely used if the impulse response of the electronics is long compared to the signal delivered by the sensor.

In precise timing applications with fast readout electronics, accuracy in the models is essential to capture some effects that can degrade the measured time resolution

The preamplifier output waveform changes its shape depending on the position of the interaction. This leads to a contribution that can't be corrected for in leading edge discriminator systems

Fluctuations in the number of electron/hole pairs created along the path of the particle introduce fluctuations on the shape of the induced signal.

** H. Bichsel, Straggling in thin silicon detectors, Rev. Mod. Phys. 60 (1988) 663–699. doi:10.1103/RevModPhys.60.663.*

Example: TDCpix time resolution was measured 71ps rms (laser at the center of the pixel generating 2.4fC signal at surface). Test beam with MIPs showed a time resolution of 115ps rms

Plots: M. Noy (CERN), VERTEX 2016

Preamplifier topologies

Preamplifier topologies

Charge sensitive amplifier

- Capacitive feedback around the amplifier (current integral)
- A resistor (R_F , usually very large) in parallel with the capacitor is required to discharge it and to fix the DC operating point at the preamplifier input
- Long tail in the signal at v_{out} ($\tau_f = C_f R_f$) might limit the count rate for the application
- Excellent noise performance
- Ideal to readout sensors without intrinsic amplification
- $\tau_{\rm F}$ > $\tau_{\rm sensor}$ (time constant of the signal delivered by the sensor)

R. Ballabriga et al. "The Timepix4 Analog Front-end Design: Lessons learnt on Fundamental Limits to Noise and Time Resolution in Highly Segmented Hybrid Pixel Detectors" <https://doi.org/10.1016/j.nima.2022.167489>

Transimpedance amplifier

- Resistive feedback around the amplifier
- It preserves the shape of the signal delivered by the sensor
- A capacitor (C_F) in parallel with the resistor is required for stability
- Shorter tail in the signal at v_{out} ($\tau_{\text{F}} = C_{\text{F}} R_{\text{F}}$) makes this more adequate for high count rate applications
- $\tau_{\rm f}$ < $\tau_{\rm sensor}$ (time constant of the signal delivered by the sensor)
- In practice, TIAs are used for fast front end electronics in which band pass filters following the input stage are tuned to high frequencies. For such applications, TIAs will offer lower input impedance and consequently lower crosstalk signals than CSAs.

J. Kaplon and W. Dabrowski "Fast CMOS Binary Front End for Silicon Strip Detectors at LHC Experiments" IEEE TNS, VOL. 52, NO. 6, 2005

Current buffer / voltage buffer

- Typically used for the readout of detectors with intrinsic amplification (e.g. SiPMs) for precise timing
- In these applications the CSA is not optimal due to bandwidth limitations. Frequency associated with rising time (where typically $C_F < C_{SENSOR}$):

$$
f_C = GBWP \frac{C_F}{C_F + C_{SENSOR}}
$$

• The current buffer is more advantageous due to noise shaping effects and to the lower input impedance*.

*F. Ciciriello, F. Corsi, F. Licciulli, C. Marzocca and G. Matarrese, "Time performance of voltage-mode vs current-mode readouts for SiPM's," 2015 6th International Workshop on Advances in Sensors and Interfaces (IWASI), Gallipoli, Italy, 2015, pp. 249-253, doi: 10.1109/IWASI.2015.7184979.

The CSA/TIA

General case

In the general case, the feedback impedance is the combination of a capacitor and a resistor

The real amplifier has finite gain bandwidth product.

The feedback impedance defines the transfer function $\mathsf{v}_\mathsf{OUT}/\mathsf{i}_\mathsf{SENSOR}(1)$

The feedback lowers the input impedance to minimize the voltage swing at the input node (2) :

- Avoid destabilizing sensor
- Minimize crosstalk in multielectrode systems
- Reduce sensitivity of the output signal to the sensor capacitance
- Improve speed

General case

Time expressions (CSA)

Same GBWP for the two amplifiers but different gain

Transfer function when $R_E \rightarrow \infty$

$$
\frac{v_{OUT}}{i_{IN}}(s) = \frac{1}{\left(C_F + \frac{C_{SENSOR}}{A_0}\right)s\left(1 + \frac{1}{1 + A_0}\frac{C_F}{C_{SENSOR}}\right)s\left(1 + \frac{1}{1 + A_0}\frac{C_F}{C_{SENSOR}}\right)}
$$

Impulse response $i_{IN} = Q_{IN} \delta(t)$

$$
v_{OUT}(t) = \frac{Q_{IN}}{\left(C_F + \frac{C_{SENSOR}}{A_0}\right)} \left(1 - e^{-t/\tau}\right)
$$

Importance of driving up the gain and the bandwidth of the amplifier in order to obtain a fast response of the amplitude independently of the capacitive load of the sensor (C_{SFNSOR}) .

Increasing the open loop gain allows decreasing C_{FR} and increase the charge gain. This is important from the perspective of optimizing the system's noise-power. High gain is also important for low PSRR.

Input impedance

CSA configuration: C_F=190fF, R_F=1G Ω TIA configuration: C_F=190fF, R_F=100k Ω

Amplifier: A_0 =14000 (83dB) f_0 =42.8kHz

$$
Z_{FE} = \frac{Z_F(s)}{A(s) + 1} \approx \frac{Z_F(s)}{A(s)} = \frac{R_F}{(1 + R_F C_F s)} \frac{(1 + \tau_0 s)}{A_0}
$$

$$
f_F = \frac{1}{2\pi R_F C_F}
$$

$$
f_0 = \frac{1}{2\pi \tau_0}
$$

Inductive behaviour for the transimpedance configuration

Stability

 $GBWP\cdot R_F$

 $C_F > 2$

- The expression for $v_{\text{OUT}}/I_{\text{SENSOR}}$ is that of a second order system
- In the case of a transimpedance amplifier we can calculate the minimum value for C_F required for stability

Q<1/2 (Overdamped system) Q=1/2 (Critically damped system) Q>1/2 (Underdamped system)

- For overdamped system
- High GBWP amplifiers are easier to compensate
- Trade off stability-closed loop bandwidth

Stability

TIA configuration: C_F=120fF, R_F=100k Ω Amplifier: A_0 =14000 (83dB) f_0 =42.8kHz $Q_{in} = 1 fC$

Preamplifier configurations: Examples

Hybrid Pixel Detector: Strip Detector:

R. Ballabriga et al. "The Timepix4 Analog Front-end Design: Lessons learnt on Fundamental Limits to Noise and Time Resolution in Highly Segmented Hybrid Pixel Detectors" <https://doi.org/10.1016/j.nima.2022.167489>

CSA configuration: C_F ~3fF, R_F ~80M Ω (tunable) Amplifier: A_0 =1000 (60dB), GBWP=1GHz C_{SENSOR} =25fF (Nominal)

(RF is simplified in this schematic)

J. Kaplon and W. Dabrowski "Fast CMOS Binary Front End for Silicon Strip Detectors at LHC Experiments" IEEE TRANSACTIONS ON NUCLEAR SCIENCE, VOL. 52, NO. 6, DECEMBER 2005

TIA configuration: C_F =190fF, R_F^{\sim} 120k Ω Amplifier: A₀=14000 (83dB), f_0 =42.8kHz, GBWP=600MHz C_{SENSOR} =20pF (Nominal) τ_{F} =22ns

Single ended common source (cascoded) configuration

M² MOS: M. Manghisoni, D. Comotti, L. Gaioni, L. Ratti, V. Re, "Dynamic compression of the signal in a charge sensitive amplifier: From concept to design", IEEE Trans. Nucl. Sci. 62 (5) (2015) 2318–2326

Reset configurations in CSAs

Switch Reset (charge injection to preamplifier input)

Continuous Reset: Resistor (high value for R difficult to implement in CMOS)

Continuous Reset: MOS transistor Compact solution, Non-linearity

P. Grybos "Front-end Electronics for Multichannel Semiconductor Detector Systems"; EuCARD Editorial Series on Accelerator Science and Technology, Vol.08

Noise Basic introduction Types of noise Noise in the MOS transistor Noise in a cascade of amplifiers
Noise (basic introduction)

- Noise is a random process (its value cannot be predicted at any time)
- Statistical model allows us to predict its long term r.m.s. value (its randomness) and its average power
- Average power delivered by a periodic signal to a load resistance

$$
P_{av} = \frac{1}{T} \int_{-T/2}^{+T/2} \frac{v^2(t)}{R} dt \quad [Watts]
$$

The average power for a random signal is given by

$$
P_{av} = \lim_{T \to \infty} \frac{1}{T} \int_{-T/2}^{+T/2} x^2(t) dt \quad [V^2]
$$

- We can also define the rms value as sqrt(P_{av})
- The power spectral density $(S_x(f))$ shows how much power the signal carries at each frequency. S_x(f) is the average power carried by x(t) in a 1Hz bandwidth around frequency f

$$
P_{av} = \int_{-\infty}^{\infty} S_x(f) \, df \quad [V^2] \qquad \qquad r.m.s. = \sqrt{P_{av}} \quad [V \, r.m.s.]
$$

Noise (basic introduction)

The average noise power of the sum of two separate sources is:

• If a signal (noise) with power spectral density $S_x(f)$ is applied to a linear time-invariant system with transfer function H(f), then the output spectrum $\mathsf{S}_{\mathsf{Y}}(\mathsf{f})$ is given by

 $S_Y(f) = S_X(f)|H(f)|^2$

h(t) $H(s)$ x(t) $X(s)$ – $S_{\sf X}$ (f) $y(t)=x(t)^*h(t)$ $Y(s)=X(s)H(s)$ $S_Y(f)=S_X(f)|H(f)|^2$

The noise (in the frequency domain) is shaped by the filter

Types of noise

Thermal noise

• Results from random thermal motion of carriers in a conductor. The thermal noise of a resistor can be modelled by a series voltage source with one sided spectral density:

$$
\sum_{k=1}^{n} S_{k}(f) = \frac{V_{n}^{2}}{\Delta f} = 4KTR \quad [V^{2}/Hz]
$$

• We can consider thermal noise is white (in reality it decreases at high frequencies \sim 10THz at room temperature or \sim 10GHz at 4K)

$$
S_v(f) = \frac{V_n^2}{\Delta f} = 4KTR \quad [V^2/Hz]
$$

\n
$$
P_{n,out} = \frac{KT}{C} [V^2]
$$

\n
$$
v_{rms} = \sqrt{\frac{KT}{C}} [V r.m.s.]
$$

The noise is independent of R Larger values of R, the associated noise per unit bandwidth increases but the overall bandwidth of the circuit decreases.

Sound: "shhhhhh"

Shot noise

• Occurs when there exist distinctive transitions of charge carriers happening (for example carriers crossing a potential barrier p-n junction)

- We consider it white although the shape of the power spectral density is determined by the shape of the current that is generated in every distinctive event
- *Sound: "rain hitting the ground"*

Pop corn noise, Burst Noise, Random Telegraph Noise

- Can be determined by the behaviour of a single trap site in the semiconductor. It is the basis for the discussion on flicker noise
- Autocorrelation function (cusp shape), Lorentzian (1/f²) Power Spectral Density due to a single trap:

$$
R_{XX}(\tau) = R_{XX}(\tau)e^{-|\tau|/\tau_t} \qquad S_i(f) = \frac{c_t \tau_t}{1 + (2\pi f)^2 \tau_t^2}
$$

• *Sound: "Old audio systems, clicking sound (gold impurities in bipolars)*

We saw it due to the switching behaviour of post breakdown conduction in thin oxide SiO² films Can also be observed in very small transistors due to the percolation nature of the I_{DS} and the impact on this current from a single charge trap

Wafer grounded on chuck

"The thin oxide degradation in the plasma environment would appear as a random effect due to the fact that it would influence differently every transistor"^a

circuit operation temperatures the diode is in low leakage, low capacitance reverse state.

• "Recommended that all gates be tied down to a diode at M1" .

Pop corn noise, Burst Noise, Random Telegraph Noise

• We measured RTS on individual pixels

• 2 hour measurement RTS on less than 1% of the pixels showing RTS

• Different frequencies (changes between states from tens of second to hours)

Take home message: "If you want to keep a good integrity of the thin oxide of your transistors (and have a good matching and prevent gate leakage current) put a (minimum size) tie down diode at the gate connected to the poly with M1."

Flicker noise

- 1/f noise is related to the random distribution of time constants of charge traps (e.g. in interfaces or in dislocations of the crystal structure)
- Interface traps "capture" and "release" charge
- In the case of the transistor, the larger the gate area, the more these fluctuations are averaged out
- Large number of traps uniformly distributed with independent $\tau_{\rm t}$ values means that their superposition approximates a 1/f behaviour

Noise in the MOS transistor

MOS transistor noise (simplified)

• MOS transistors exhibit thermal noise generated in the channel and 1/f noise (other noise sources are neglected here)

Thermal noise from the channel and flicker noise expressions (referred to the gate terminal) :

$$
\frac{v_{CH}^2}{\Delta f} + \frac{v_F^2}{\Delta f} = 4KTn\gamma\frac{1}{g_m} + \frac{K_a}{C_{ox}WLf^{\alpha}}
$$

 $i_{\mathcal{CH}}^2$ 2 Δf $= 4K T n \gamma \alpha_w g_{d0}$

- α_w is the noise excess factor (1.09 NMOS, 1.04 PMOS in 65nm CMOS)*
- g_{d0} is the drain-source conductance when $V_{\text{DC}}=0$, the same as R_{ON}^{-1} . For long channel devices (i.e. non velocity saturation) $g_{ds0} = g_{mg}$

**M. Manghisoni, L. Gaioni, L. Ratti, V. Re, G. Traversi, Introducing 65nm CMOS technology in low-noise read-out of semiconductor detectors, Nucl. Instrum. Methods Phys. Res. A 624 (2) (2010) 373–378*

Variability of Low Frequency Noise and Mismatch in Enclosed-Gate and Standard nMOSFETs

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Fig. 1. Layout of enclosed gate transistors with drain at the center, and outer poly-edge cut a), and layout of standard transistor b).

IV. CONCLUSIONS

Enclosed gate nMOS transistors show reduced low frequency noise levels compared to standard-layout devices of the same technology, reduced by a factor of 2 to 3 in weakmoderate inversion. Furthermore, the EG nMOS devices show also a reduced standard deviation of LFN. Another advantage is the suppression of gate voltage mismatch degradation in weak inversion. These improvements are all attributed to the absence of the STI-edge effect in the enclosed-gate transistor structures. The 50 measured devices show a typical 1/f noise behavior at higher gate voltages, while RTN components appear at gate voltages around moderate and weak inversion. The statistical LFN model [17], [18] can cover both gate- and drain-voltage bias-dependence of average noise and its standard deviation, similarly for enclosed-gate as well as standard-layout transistors.

ELT transistors are effective in minimizing flicker noise

In the early 90's E. Heijne suggested the use of special gate all around design techniques to make radiation hard components in standard commercial CMOS processes.

A. Marchioro was key to getting access to the 0.25 km CMOS process and led the development of a digital library which was radiation tolerant.

Thesis: G. Anelli «Conception et caractérisation de circuits intégrés résistants aux radiations pour les détecteurs de particules du LHC en technologies CMOS submicroniques profondes»

Noise in a cascade of amplifiers

Noise in a cascade of amplifiers

Most of the noise in a typical readout electronics chain for the readout of semiconductor detectors comes from the input transistor.

Transfer of noise sources to the output of the CSA

Transfer of noise sources to the output of the CSA

Noise mechanisms arising from (1) the preamplifier's transistors (thermal, flicker), (2) the feedback resistor (thermal) and (3) the sensor (shot) can be represented in the circuit domain by two equivalent noise generators placed at the input in "series" and "parallel".

The series noise generator usually has two components, thermal noise with a white spectral density and flicker noise (more generally $1/f^{\alpha}$) due to interface effects and is strongly process dependent.

The parallel noise generator includes the thermal noise from R_F and the shot noise from the sensor.

Transfer of noise sources to the output of the CSA

Full noise calculations can be found in A. Rivetti "CMOS Front-End Electronics for Radiation Sensors" * X. Llopart et al 2019 JINST 14 C01024

Noise filtering

Noise filtering

Objectives of signal processing after preamplifier:

- Improve the Signal-to-Noise ratio
- Minimize pile-up by *shaping* the signal
- Minimize baseline fluctuations
- Add additional gain

Shaping implies manipulating the frequency component of the signal i.e. a shaper is a filter

CR-RC shaper

The shaper

- CR-RCⁿ filters offer a good compromise between performance, power consumption and simplicity
- Unipolar semi gaussian shaper (CR-RCⁿ) consists of one differentiation of the signal followed by n integrations
- n is the order of the shaper
- If the differentiation and integration time constants are chosen to be the same the transfer function of the shaper is given by:

$$
H(s) = \frac{1}{2} \left(\frac{s\tau}{1 + s\tau} \right) \left(\frac{1}{1 + s\tau} \right)^n
$$

$$
H(s) = \frac{1}{2} \left(\frac{s\tau}{1 + s\tau} \right)^n
$$

The shaper

- In the time domain the high pass filter removes low frequency part of the signal creating a waveform that goes to the baseline before the next pulse arrives.
- Following the high pass filter, a low pass filter smooths the signal

The shaper

• In the time domain the response to a step function is:

$$
v_{out}(t) = \frac{1}{n!} \left(\frac{t}{\tau}\right)^n \exp\left(-\frac{t}{\tau}\right)
$$

- The peaking time is at $t = n\tau$
- And the amplitude of the signal is

$$
v_{out_max}(t) = \frac{n^n}{n!e^n}
$$

Noise equation of the system:

Noise equation of the system:

In most designs, the dominant noise source is the input transistor

Increasing the width of the input transistor (if biased in s.i.) increases both its g_m and the input capacitance. Usually an optimum of ENC exists w.r.t. input transistor width.

Note as well that a minimum exists w.r.t. the shaping time. For small values, the thermal noise dominates, for high values of τ_{s} the parallel noise dominates.

In a system in which the peaking time can be optimized, the flicker noise imposes the achievable noise performance. The flicker can be improved increasing the area and choosing the right transistor type (PMOS instead of NMOS).

In front-ends optimized for low power, and speed the channel thermal is the dominant contribution.

Part 1: Introduction to hybrid pixel detectors

Classification of technologies, limitations of hybrid pixel detectors

Part 2: Introduction to signal processing

Part 3: Review of ASICs

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CERN Microelectronics Section

Outline

- Review of ASICs
- Digitization methods
- Techniques for increasing the count rate
- Techniques for allowing spectroscopic information at fine pixel pitch
- Towards large area detectors
- Summary and conclusions

Review of ASICs (full picture)

Photon Counting Detectors for X-Ray Imaging With Emphasis on CT

R. Ballabriga[®], J. Alozy, F. N. Bandi, M. Campbell[®], Member, IEEE, N. Egidos, J. M. Fernandez-Tenllado, E. H. M. Heijne, Life Fellow, IEEE, I. Kremastiotis[®], X. Llopart, B. J. Madsen, D. Pennicard, V. Sriskaran[®], and L. Tlustos

- *Tables (included for completeness)*
- *Tables report published material*
- *Reported measurement values not taken as absolute values for comparison but should be used to identify trends and performance envelopes*

The indexes (in italics and inside curly brackets) in the table identify the chips in the following plots (they should not be confused with the references).

The maximum count-rate corresponds to the input flux at which the output count-rate saturates (which corresponds, for the particular case of the paralyzable model, to the inverse of the dead time)

For ASICs implementing a non-paralyzable type of behaviour, the maximum count-rate corresponds to the input count-rate for which the measured count-rate reaches ~95% of the asymptotic maximum.

In order to do spectroscopy at fine pitches a charge reconstruction and hit allocation architecture is 107**required.**

Reminder

Message: The geometry of the sensor (pitch/thickness) determines the shape of the induced current pulse (and puts a lower limit on the electronics integration time)

We assume the maximum count rate as

$$
\frac{1}{\tau} \frac{1}{pixel \text{ area}} \big[Mcps / \text{mm}^2 \big]
$$

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In which the dead time of the channel is chosen to ensure that a percentage of the charge will be integrated in the electronics
Maximum count rates (Mcps/mm²) vs pixel size (μm)

The red curves indicate the maximum count rate that we would achieve if we designed the electronics system to integrate 90%, 95% or 97.5% of the charge

Maximum count rates (Mcps/mm²) vs pixel size (μm)

Review of ASICs (details)

Digitization methods

Digitization methods

- On-pixel
	- Flash ADC (e.g. ChromAIX chips)
	- SAR ADC (e.g. CEA-Multix)
	- Ramp-compare ADC (e.g. Ajat-0.35)
	- Time-Over-Threshold (e.g. Timepix3, Dosepix)
- Other
	- Digitization off-pixel (e.g. Hexitec)

ChromAIX: A high-rate energy-resolving photon-counting ASIC for **Spectral Computed Tomography**

Roger Steadman, Christoph Herrmann, Oliver Mülhens Philips Research Europe, Weisshausstrasse 2, 52066 Aachen, Germany

- ChromAIX1 (published 2010)
	- $8x16$ pixels (300 μ m pitch), 0.18 μ m CMOS
	- 4 energy thresholds, 20ns peaking time
	- Flash (parallel) ADC, applications for large bandwidth, high power consumption

R. Steadman, "ChromAIX: A high-rate energy resolving photon-counting ASIC for Spectral Computed Tomography" Proc. SPIE 7622, 762220–762228 (2010).

Nuclear Instruments and Methods in Physics Research A 862 (2017) 18-24

^a Philips Research Europe, High Tech Campus, 5656 AE Eindhoven, Netherlands ^b Philips Healthcare, 31004 Haifa, Israel

- ChromAIX2 (published 2017)
	- 22x32 pixels (500 μ m pitch), 0.18 μ m CMOS
	- 5 energy thresholds, ~10ns peaking time, ~23.5ns dead time @25keV Threshold

ChromAIX1 ASIC on evaluation PCB (2 side buttable design) 8x16 pixels **300**m**m pixel pitch**

ChromAIX2 ASIC on evaluation PCB (3 side buttable design) 22x32 pixels **500**m**m pixel pitch**

(Mcps/pixel) $\qquad \qquad \qquad$ Spectrum measured with a ²⁴¹Am source (threshold scan)

Spectrum measured with a ²⁴¹Am source (threshold scan)

This example illustrates how the pixel size is related to (1) the ability to process high fluxes and (2) the spectral fidelity

Time-over-Threshold (ToT) digitization

ToT digitization: Timepix3 chip

- Developed in the framework of the Medipix3 collaboration
- 256x256 pixel matrix, 55x55 μ m² pixels
- CMOS 0.13µm technology
- **Simultaneous measurement of Time and Energy per event with a data driven readout**
- **No frames but continuous data stream. Every event consists of**
	- **16 bits address**
	- **18 bits Time (1.56ns resolution)**
	- **10 bits Energy**
- Maximum hit rate of **0.4 10⁶ hits/s/mm²**
- Impact of charge diffusion/fluorescence can be compensated by offline processing, sub-pixel resolution possible

T. Poikela et al. "Timepix3: a 65K channel hybrid pixel readout chip with simultaneous ToA/ToT and sparse readout" JINST 9 C05013, 2014. The mass of the state of th

ToT digitization: Timepix3 chip

T. Poikela et al. "Timepix3: a 65K channel hybrid pixel readout chip with simultaneous ToA/ToT and sparse readout" JINST 9 C05013, 2014. 119

Slide courtesy of B. Bergmann, S. Pospisil, IEAP, CTU, Prague

ToT digitization: Dosepix chip

- Developed in a partnership between CERN, University of Erlangen and IBA dosimetry
- Main applications: dosimetry, X-ray tube diagnostics tool
- 16x16 pixel matrix, $220x220\mu m^2$ pixels
- CMOS $0.13 \mu m$ technology
- 1 global analog threshold
- Operation Modes:
	- Energy binning mode
		- 12 bit ToT measurement @100MHz
		- 16 digital thresholds (on each pixel) for event-by-event energy binning
		- 16x 16-bit energy bin registers
	- Photon counting mode (8 bits)
	- Integral ToT (24 bits)

W.S.Wong et al., Electrical measurements of a multi-mode hybrid pixel detector ASIC for radiation detection, JINST 7, 2012. doi:10.1088/1748-0221/7/01/C01056

ToT digitization: Dosepix chip

Spectrum of gamma emissions Am²⁴¹ source, filtered to block alphas (1 frame of data)

Maximum count rates (Mcps/mm²) vs pixel size (μm)

A High-Rate Energy-Resolving Photon-Counting ASIC for Spectral Computed Tomography

Mikael Gustavsson, Member, IEEE, Farooq Ul Amin, Anders Björklid, Andreas Ehliar, Cheng Xu, and Christer Svensson, Fellow, IEEE

- 0.4x0.5mm detector element size
- 1 detector module has 50 Si strips (edge-on-geometry)
- 1 strip is divided into 16 segments
- 800 channels per module (8 thresholds/channel)
- 1500 modules in a full system
- **Segmentation in the direction of the X-rays increases the maximum flux the system can deal with**
- **Longer segments (~4.8mm) together with complicated wiring increase the input capacitance of the readout channel (~3pF)**

ASIC: M. Gustavsson et al. "A high-rate Resolving Photon Counting ASIC for Spectral Computed Tomography" , IEEE Trans Nucl. Sci, Vol. 59, No. 1, Feb 2012.

Module description and characterization: C. Xu et al. "Energy resolution of a segmented silicon strip detector for photon-counting spectral CT" NIMA 715 (2013) 11–17 43

Power consumption

- Power consumption versus channel density
- Edge-on configuration: An effective sensor channel is read out by 16 electronics channels
	- Interconnection scheme adds input capacitance
	- Requirement to achieve low minimum thresholds to account for primary Compton interactions to 125 improve the detection efficiency

Edge-on silicon detectors F Arfelli et al 1997 Phys. Med. Biol. 42 1565

A linear array silicon pixel detector: images of a mammographic test object and evaluation of delivered doses

F Arfelli††, V Bonvicini†, A Bravin†§, G Cantatore†§, E Castelli†§, L Dalla Palma||, M Di Michiel†§, R Longo†§¶, A Olivo†§, S Pani†‡, D Pontoni††, P Poropat†§, M Prest†§, A Rashevsky†, G Tromba†† and A Vacchi⁺

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§ Dipartimento di Fisica dell'Università di Trieste, via Valerio 2, 34127 Trieste, Italy

Il Istituto di Radiologia dell'Università di Trieste, Ospedale di Cattinara, Strada di Fiume, 34100 Trieste, Italy

Received 30 January 1997

[…] A 1.4 cm length linear array detector was developed with a pixel size of 200 × 300 µm² . It consists of a silicon microstrip device used in a configuration in which radiation impinges on the side rather than on the surface of the chip (Arfelli et al 1996). Due to the way the beam impinges on the detector, the radiation must traverse 1 cm of silicon. If the incident radiation has an energy lower than 30 keV it is fully absorbed. Figure 1 illustrates the detector geometry. […]

Techniques for increasing the count rate

Experimental evaluation of the Pile-Up Trigger method in a revised quantum-counting CT detector

E. Kraft*^a, F. Glasser^b, S. Kappler^a, D. Niederloehner^a, P. Villard^b ^aSiemens AG, Healthcare Sector, Siemensstr. 1, 91301 Forchheim, Germany; ^bCEA-LETI-MINATEC, Recherche Technologique, 17 rue de martyrs, 38054 Grenoble Cedex 09, France

The Counting Detector

Basic Geometry:

- CdTe sensor, 1.6mm thick
- 225µm sub-pixel pitch
- Macro-pixel mode (4x4) fits to geometry of anti -scatter grid
- 24 modules \rightarrow 22cm FOV
- z -coverage up to 32x0.5mm

ASIC:

- Fast pulse shaping < 20ns
- Counter thresholds 20keV ... 160keV
- Two counters per sub-pixel

ASIC

Siemens Photon Counting ASIC (pileup trigger method)

- $64x64$ pixel matrix, 225 μ m pixel pitch
- Pile-up trigger method
- Observation: higher thresholds paralyze at higher count rates
- Combine spectral counter signal with pile-up counter signal

$$
N = N_s + w \cdot N_p
$$

- Advantages
	- Unambiguous up to the highest fluxes
	- Full spectral sensitivity in the lowflux regime inside the patient $(N_p << N_S)$

E. Kraft et al. "Experimental evaluation of the pile-up trigger method in a revised quantum-counting CT detector" Proc. SPIE 8313, Medical Imaging 2012: Physics of Medical Imaging, 83134A (2012).

The New PILATUS3 ASIC with Instant Retrigger Capability

Teddy Loeliger, Member, IEEE, Christian Brönnimann, Member, IEEE, Tilman Donath, Matthias Schneebeli, Roger Schnyder, Member, IEEE, and Peter Trüb

Pilatus3 (Dectris)

- 60x97 pixel matrix, 172 µm pixel pitch
- 1 Threshold level
- 0.25µm CMOS technology
- Radiation hardness by design

(IBEX includes also the instant retrigger functionality)

Pilatus 3 ASIC (Instant retrigger)

After increasing counter, re-evaluation of the pulse after a pre-determined time interval Very accurate for monochromatic light (synchrotrons)

Contents lists available at ScienceDirect

Nuclear Inst. and Methods in Physics Research, A

journal homepage: www.elsevier.com/locate/nima

Dead time model for X-ray photon counting detectors with retrigger capability

NUCLEAR

P. Zambon DECTRIS Ltd., Taefernweg 1, 5405 Baden-Daettwil, Switzerland

Techniques for allowing spectroscopic information at fine pixel pitch

In order to do spectroscopy at fine pitches a charge reconstruction and hit allocation architecture is required.

The Medipix3RX: a high resolution, zero dead-time pixel detector readout chip allowing spectroscopic **imaging**

(2013 JINST 8 C02016)

R. Ballabriga, $a,1$ J. Alozy, a G. Blaj, a M. Campbell, a M. Fiederle, d E. Frojdh, a E.H.M. Heijne, a,b,c X. Llopart, ^a M. Pichotka, ^d S. Procz, ^d L. Tlustos^d and W. Wong^a

500

1000

1500

2000

 -1000

-500

 $\mathbf 0$

- Energy spectrum in Single Pixel Mode and in Charge Summing Mode (sum of all the pixels in the chip ~16k pixels)
- 60keV, 2mm CdTe, 110mm pitch
- Fluorescence photons are included in charge sum if their deposition takes place within the volume of the pixels neighbouring the initial deposition
- Ga K-edge (50.2keV) can be identified in CSM images
- SNR higher in CSM for the higher energy thresholds

PIXIE III: a very large area photon-counting CMOS pixel ASIC for sharp X-ray spectral imaging

2015 JINST 10 C01032

R. Bellazzini,^{*a,b*} A. Brez,^{*a,b*} G. Spandre,^{*a,b*,1} M. Minuti, a ,*b* M. Pinchera, a ,*b* P. Delogu, a ,*c* P.L. de Ruvo^{a,c} and A. Vincenzi^b

ERICA: An Energy Resolving Photon Counting Readout ASIC for X-Ray In-Line Cameras

Jose-Gabriel Macias-Montero a^* , Maher Sarraj b , Mokhtar Chmeissani a , Thomas Moore c , Raimon Casanova a , Ricardo Martinez d , Carles Puigdengoles d , Xavier Prats^a, and Machiel Kolstein^a.

Photon counting, dual energy X-ray imaging at CT count rates: measurements and implications of in-pixel charge sharing correction

Christer Ullberg, Mattias Urech, Charlotte Eriksson, Alexander Stewart, Niclas Weber XCounter AB, Svärdvägen 23, S-182 33 Danderyd, Sweden

2018 SPIE

350

IEEE TRANSACTIONS ON NUCLEAR SCIENCE, VOL. 62, NO. 1, FEBRUARY 2015

Measurements of Matching and Noise Performance of a Prototype Readout Chip in 40 nm CMOS Process for Hybrid Pixel Detectors

P. Maj, Member, IEEE, P. Grybos, Member, IEEE, R. Szczygiel, Member, IEEE, P. Kmon, Member, IEEE, R. Kłeczek, Member, IEEE, A. Drozd, Member, IEEE, P. Otfinowski, Member, IEEE, and G. Deptuch, Senior Member, IEEE

Towards large area fine pixel pitch detectors

Work carried out in the framework of the development of the NAEOTOM Alpha by Siemens Healthineers

138 Image: https://www.siemens-healthineers.com/en-uk/computed-tomography/photoncounting-ct-scanner/naeotom-alpha

FDA NEWS RELEASE

FDA Clears First Major Imaging Device Advancement for Computed Tomography in Nearly a Decade

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O More Press Announcements

U.S. FOOD & DRUG

For Immediate Release: September 30, 2021

Today, the U.S. Food and Drug Administration cleared the first new major technological improvement for Computed Tomography (CT) imaging in nearly a decade.

"Computed tomography is an important medical imaging tool that can aid in diagnosing disease, trauma or abnormality; planning and guiding interventional or therapeutic procedures; and monitoring the effectiveness of certain therapies," said Laurel Burk, Ph.D., assistant director of the Diagnostic X-ray Systems Team in the FDA's Center for Devices and Radiological Health. "Today's action represents the first major new technology for computed tomography imaging in nearly a decade and underscores the FDA's efforts to encourage innovation in areas of scientific and diagnostic progress."

https://www.fda.gov/news-events/press-announcements/fda-clears-first-major-imagingdevice-advancement-computed-tomography-nearly-decade

Towards large and seamless detector areas (Siemens Healthineers)

3 side buttable

4 side buttable

Slide courtesy Dr. E. Göderer, Siemens Healthineers. Presented at 6th Workshop on Medical Applications of Spectroscopic X-ray Detectors, CERN, September 2022.

MC3 ASIC, Siemens Healthineers

3 side buttable

4 side buttable

MC3 ASIC, Siemens Healthineers

- CT application
- 275x322 μ m² pixels, 4 side buttable
- 32x24 pixels
- Die size $^{\sim}10.5x8.4$ mm²
- 4 thresholds (Range 0-95keV)
- 16 bit counters
- 300Mbit/s readout speed (i.e. <200 μ s per frame)
- 12ns FWHM signal
- Non paralyzable
- 2.5keV (FWHM @60keV)
- $1mV/mm^2$ i.e. $125\mu W$ per pixel

Towards large detector areas: Medipix collaborations developments

The fill factor in the active pixel matrix is 100 % However the systems have traditionally been designed to be tiled seamlessly on 3 sides (i.e. active area <100%)

Through Silicon Vias on the Medipix3RX ASIC

Through Silicon Vias on the Timepix4 ASIC

Timepix4 chip image, 448×512 pixels, $55 \mu m$ pitch First wafers sent for TSV processing

Through Silicon Vias on the Medipix4 ASIC

*Picture courtesy: J. Alozy.

RDL view of the Timepix4 chip processed for TSVs

Summary and conclusions

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- We saw techniques for increasing the count rate
- TSVs are a technology enabling to achieve seamless large areas even at fine pixel pitches

1st international school on microelectronics for solid state detectors design, manufacturing, and application

Additional

General case

General case

General case

CSA: Signal integration. The circuit has higher gain and longer tails (limitation for high flux applications). TIA: Signal shape is preserved. Lower gain i.e. higher dynamic range, shorter tails.

Time expressions (CSA)

Same GBWP for the two amplifiers but different gain

Transfer function when $R_E \rightarrow \infty$

$$
\frac{v_{OUT}}{i_{IN}}(s) = \frac{1}{\left(C_F + \frac{C_{SENSOR}}{A_0}\right)s\left(1 + \frac{1}{1 + A_0}\frac{C_F}{C_{SENSOR}}\right)s\left(1 + \frac{1}{1 + A_0}\frac{C_F}{C_{SENSOR}}\right)}
$$

Impulse response $i_{IN} = Q_{IN} \delta(t)$

$$
v_{OUT}(t) = \frac{Q_{IN}}{\left(C_F + \frac{C_{SENSOR}}{A_0}\right)} \left(1 - e^{-t/\tau}\right)
$$

Importance of driving up the gain and the bandwidth of the amplifier in order to obtain a fast response of the amplitude independently of the capacitive load of the sensor (C_{SFNSOR}) .

Increasing the open loop gain allows decreasing C_{FR} and increase the charge gain. This is important from the perspective of optimizing the system's noise-power. High gain is also important for low PSRR.

Input impedance

CSA configuration: C_F=190fF, R_F=1G Ω TIA configuration: C_F=190fF, R_F=100k Ω

Amplifier: A_0 =14000 (83dB) f_0 =42.8kHz

$$
Z_{FE} = \frac{Z_F(s)}{A(s) + 1} \approx \frac{Z_F(s)}{A(s)} = \frac{R_F}{(1 + R_F C_F s)} \frac{(1 + \tau_0 s)}{A_0}
$$

$$
f_F = \frac{1}{2\pi R_F C_F}
$$

$$
f_0 = \frac{1}{2\pi \tau_0}
$$

Inductive behaviour for the transimpedance configuration

Stability

 $GBWP\cdot R_F$

 $C_F > 2$

- The expression for $v_{\text{OUT}}/I_{\text{SENSOR}}$ is that of a second order system
- In the case of a transimpedance amplifier we can calculate the minimum value for C_F required for stability

Q<1/2 (Overdamped system) Q=1/2 (Critically damped system) Q>1/2 (Underdamped system)

- For overdamped system
- High GBWP amplifiers are easier to compensate
- Trade off stability-closed loop bandwidth

Stability

TIA configuration: C_F=120fF, R_F=100k Ω Amplifier: A_0 =14000 (83dB) f_0 =42.8kHz $Q_{in} = 1 fC$

Timepix data, 55 µm pixels

Signal induction

Induced charge on detector electrodes

- Signals on detector electrodes arise from motion of charge carriers
- Induced current is derived from laws of electrostatics

Induced charge on detector electrodes

- Signals on detector electrodes arise from motion of charge carriers
- Induced current is derived from laws of electrostatics

In case the strips are segmented, the induced charge on each strip will change when the charge q is moving.

The movement of the charge therefore induces currents that flow between the strips and ground.

This is the principle of signal generation in ionization detectors.

W. Riegler, CERN

Induced charge on detector electrodes

• Method: Shockley-Ramo theorem: the instantaneous current induced on a given electrode is equal to

$$
i(t) = q\vec{v} \cdot \overrightarrow{E_w} \qquad \qquad \vec{v} = \mu \overrightarrow{E_d}
$$

where q is the charge of the carrier, v is its velocity, E_w *is the weighting field and E^d is the drift field*

• The induced charge (*Q*) on the electrode is given by

$$
Q=q\Delta\varphi_0
$$

where $\Delta\varphi$ is the weighting potential from the beginning *to the end of the carrier path*

> 166 S.Ramo, Proc. IRE, 27 (1939) p.584 W.Shockley, J. Appl. Phys. 9, 635 (1938) V. Radeka Ann. Rev. Nucl. Part. Sci. 1988 38: 217-277 Gatti et al., NIMA 193 (1982) 651

Induced signal on detector electrodes

Example of calculation of the weighting potential in pixelated system (Pitch/Thickness=0.5)

Total induced charge: $-n_0q$

Induced signal on detector electrodes

Example of calculation of the weighting potential in pixelated system (Pitch/Thickness=0.5)

Plot not to scale

The carrier that drifts towards the pixel electrodes will contribute to most of the charge induced on the pixel electrode. Furthermore, it is the motion close to the pixel surface that contributes most strongly to the induced charge.

For detectors in which electrons are much more mobile than holes, deriving the signal from a small pixel rather than from a large-area anode can help improve energy resolution by minimizing sensitivity of the pulse amplitude to the motion of the positive charges that may not be completely collected.

The **small pixel effect** is the consequence of signal induction process in a segmented detector.

Signal induction in the pixel electrodes

- 1mm CdTe
- 60keV photon
- 600V sensor bias
- Energy deposition at $z=240 \mu m$
- (No charge trapping, charge sharing included in simulation)

Message: The geometry of the sensor (pitch/thickness) determines the shape of the induced current

