

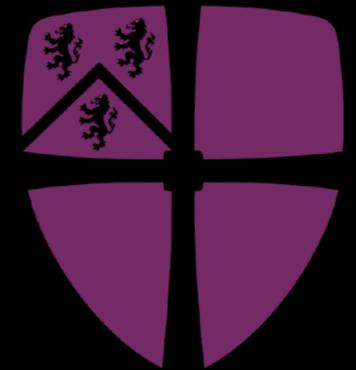
Dark Matter (h)eats Young Planets

Djuna Lize Croon (IPPP Durham)

PADUA, September 2023

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DC, J Smirnov, arXiv:2309.02495



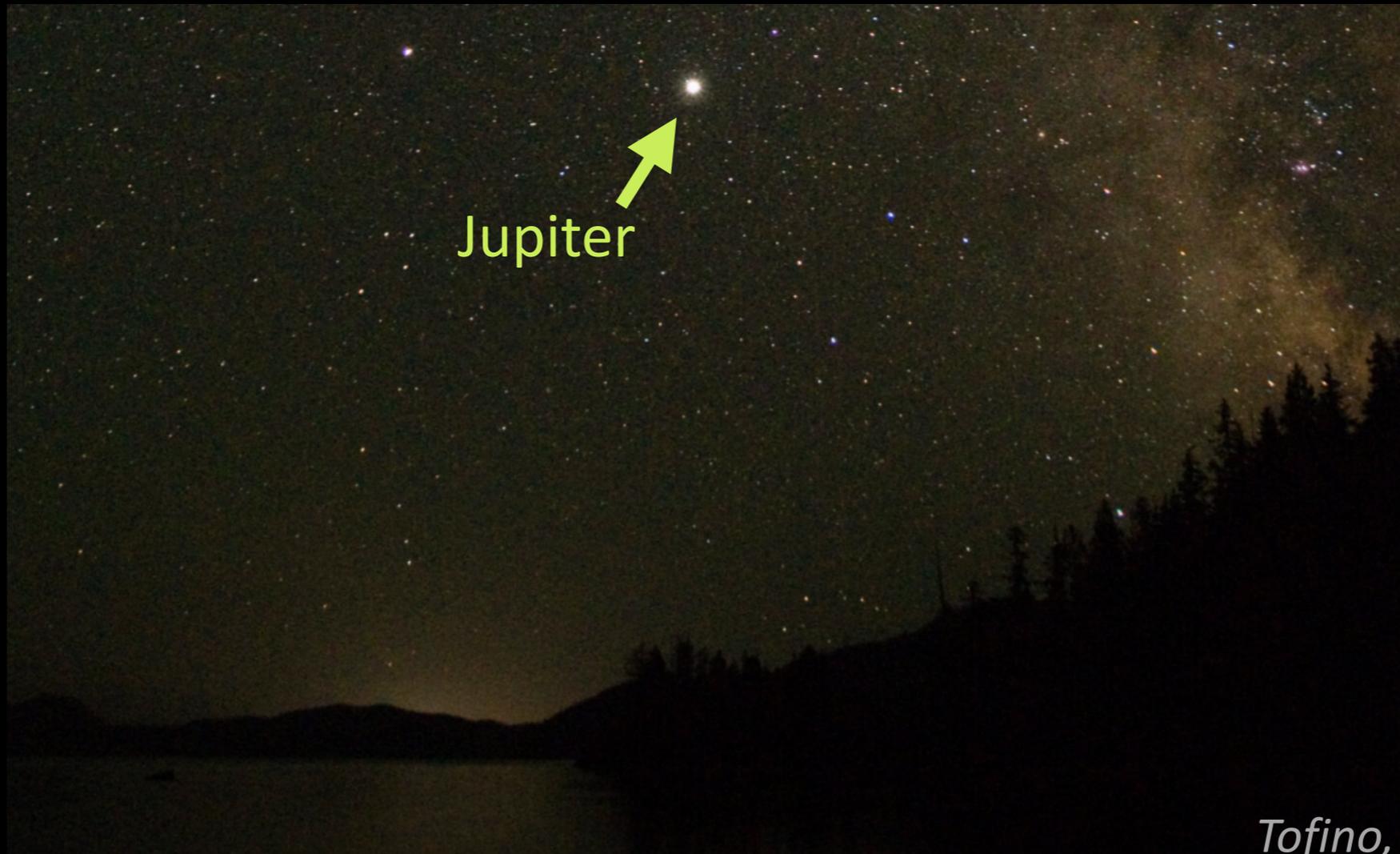
Your naked eyes



Tofino, August '20

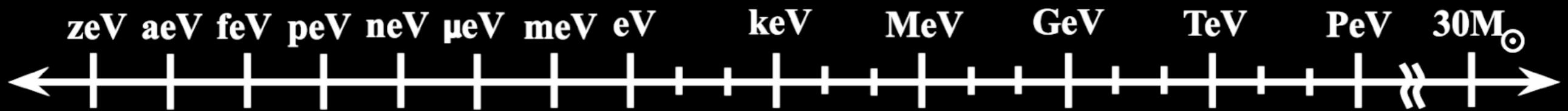
are a dark matter detector

Your naked eyes



Tofino, August '20

are a dark matter detector



Dark matter in extreme astrophysical environments



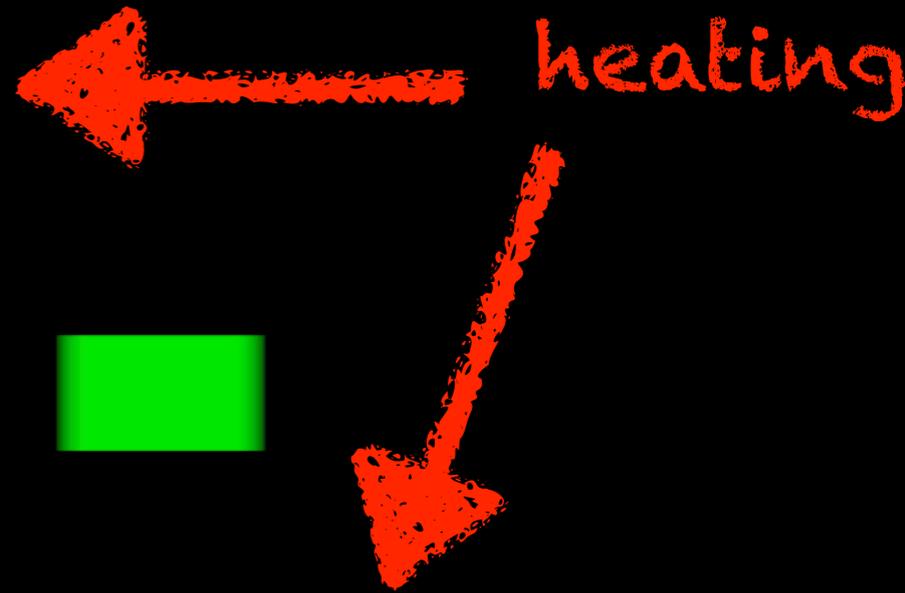
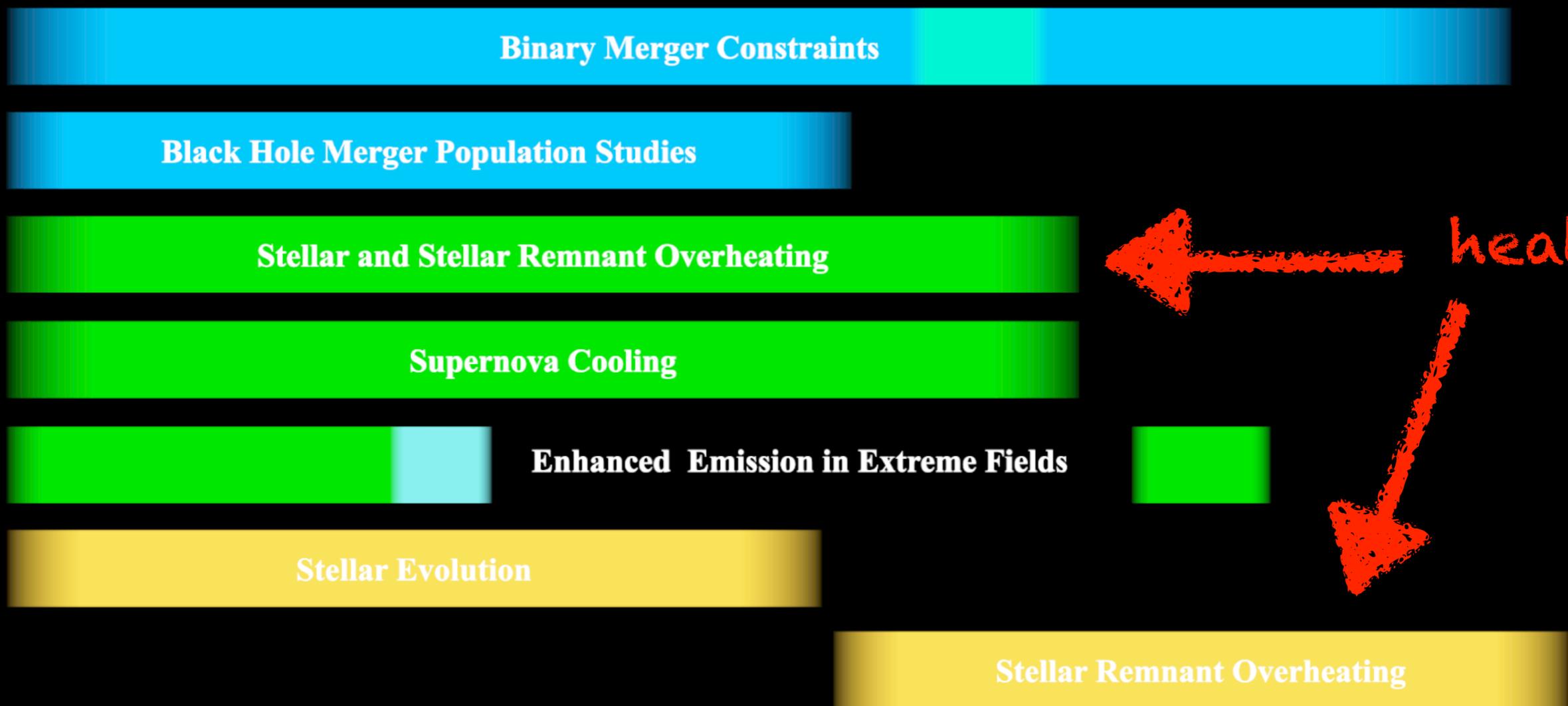
— Experimental Techniques —

Gravitational Waves

Radio

UV/Optical/
Near Infrared

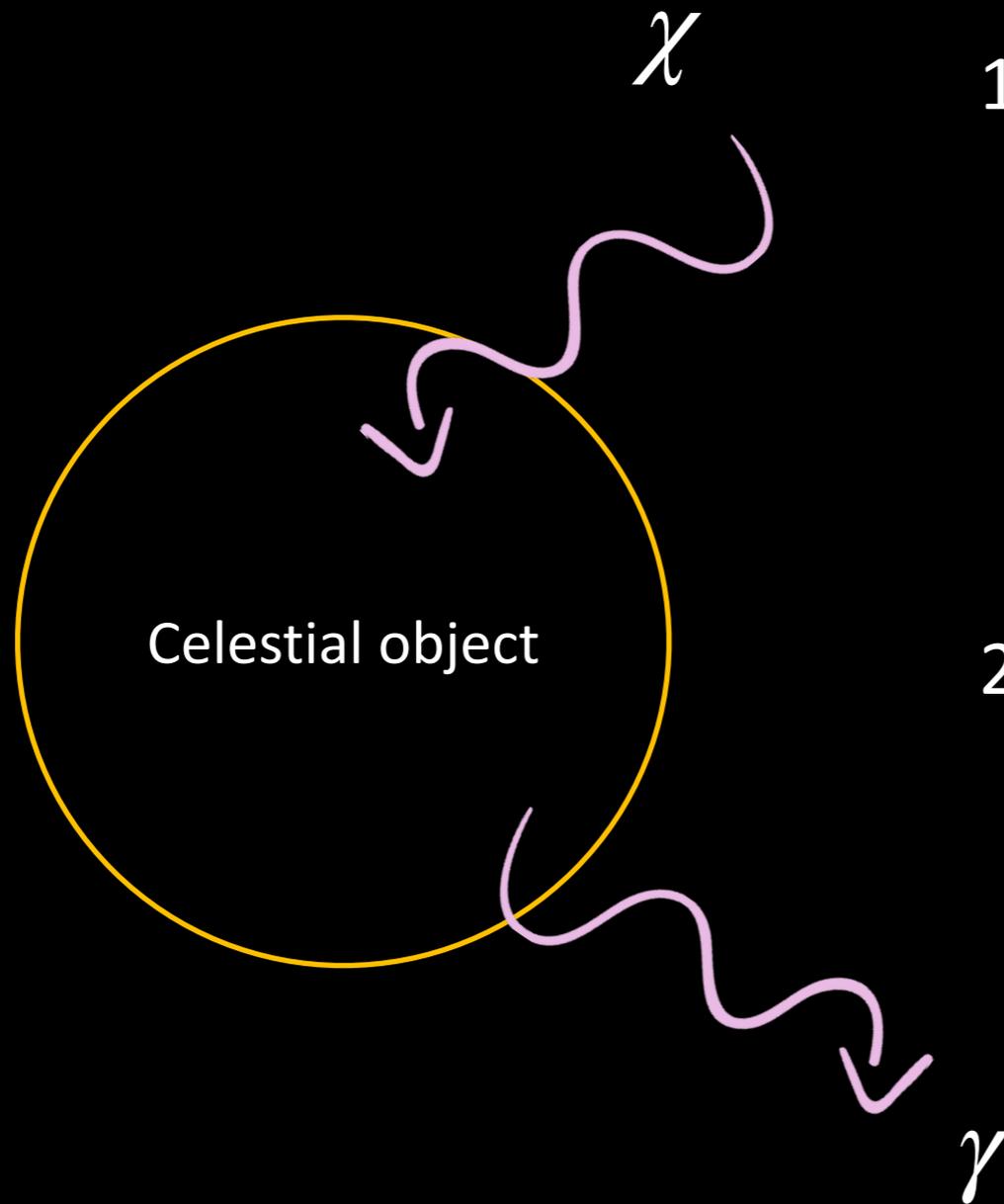
X-Ray/Gamma Ray



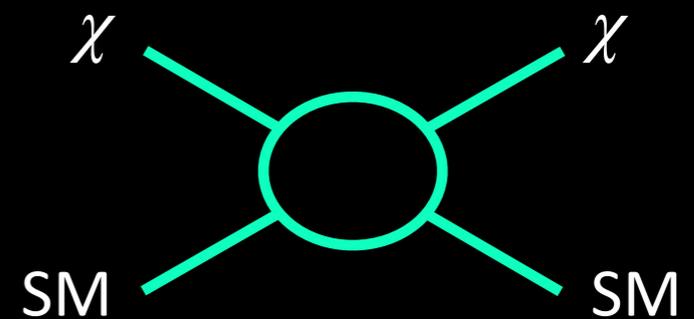
— **Experimental Techniques** —



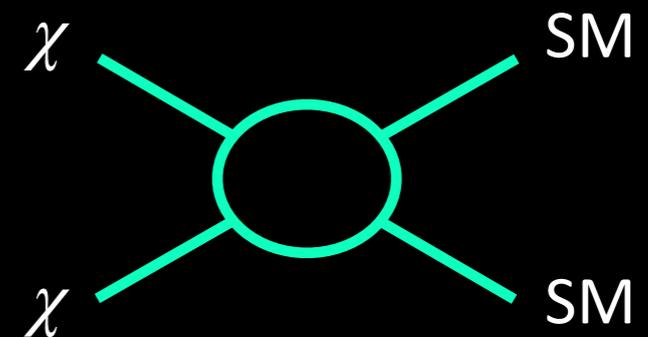
Dark matter heating



1. Capture



2. Annihilation



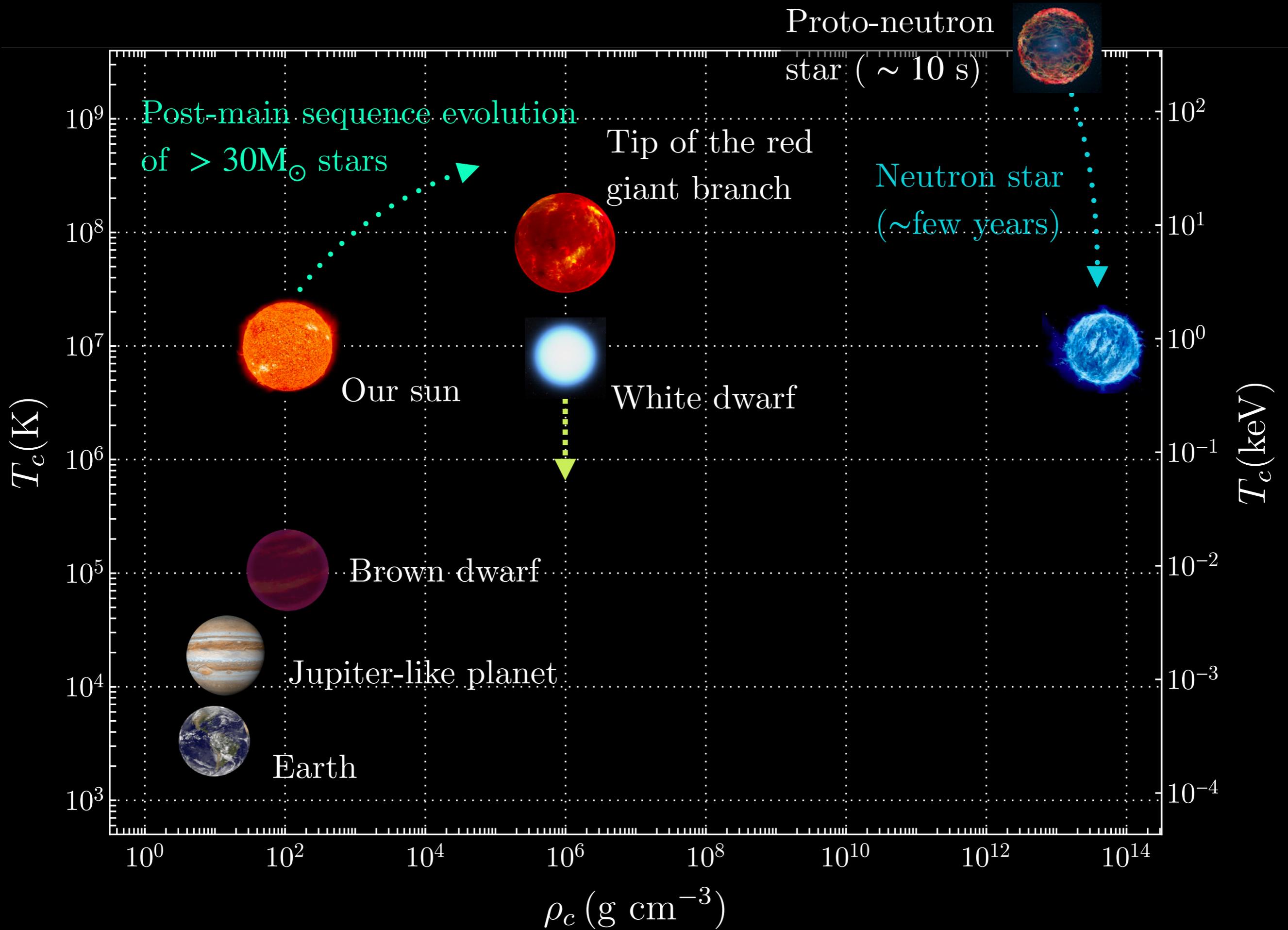
Sensitive to DM abundance ✓

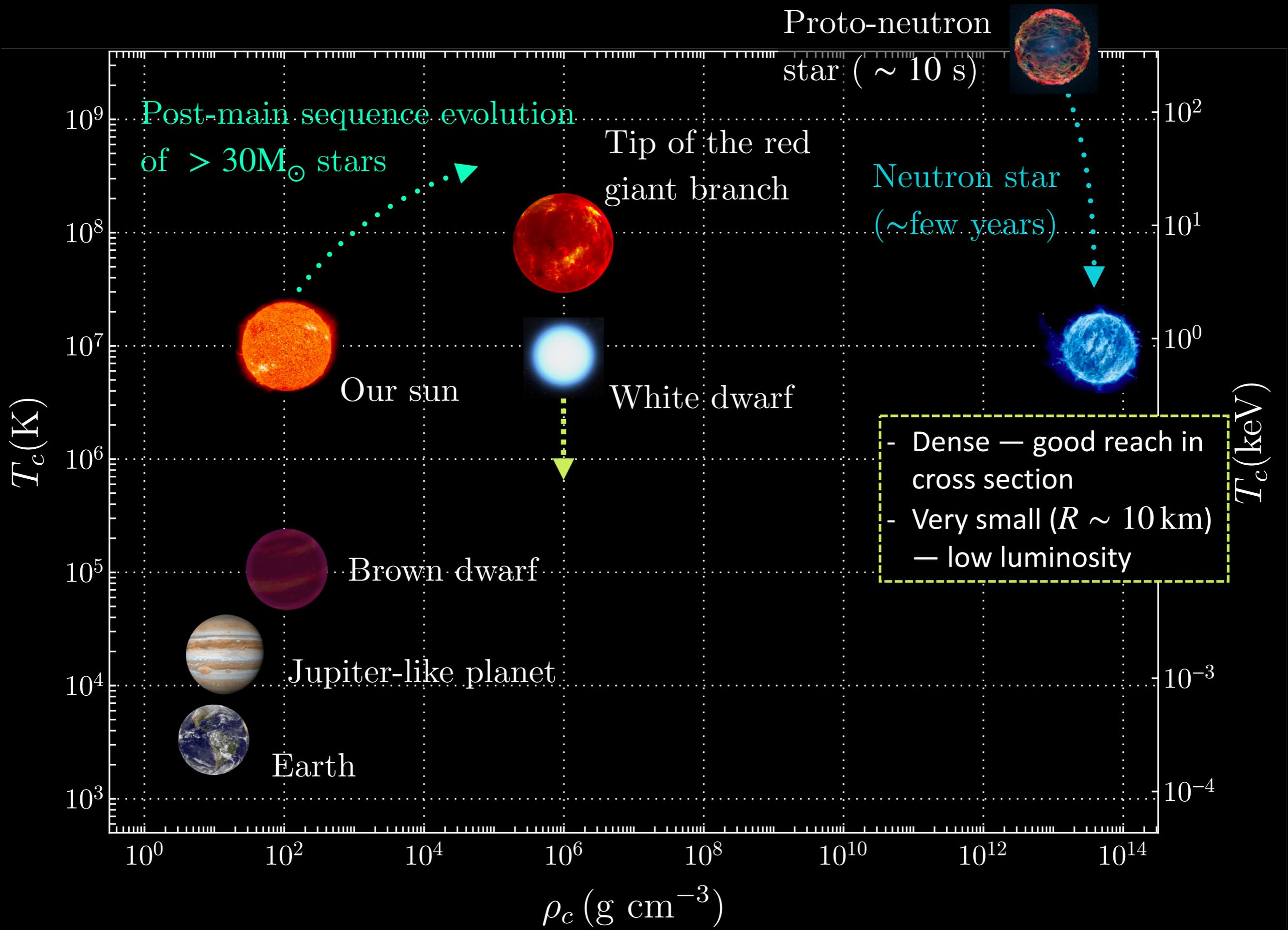
Maximum injection for a non-depleting abundance: annihilation equilibrium

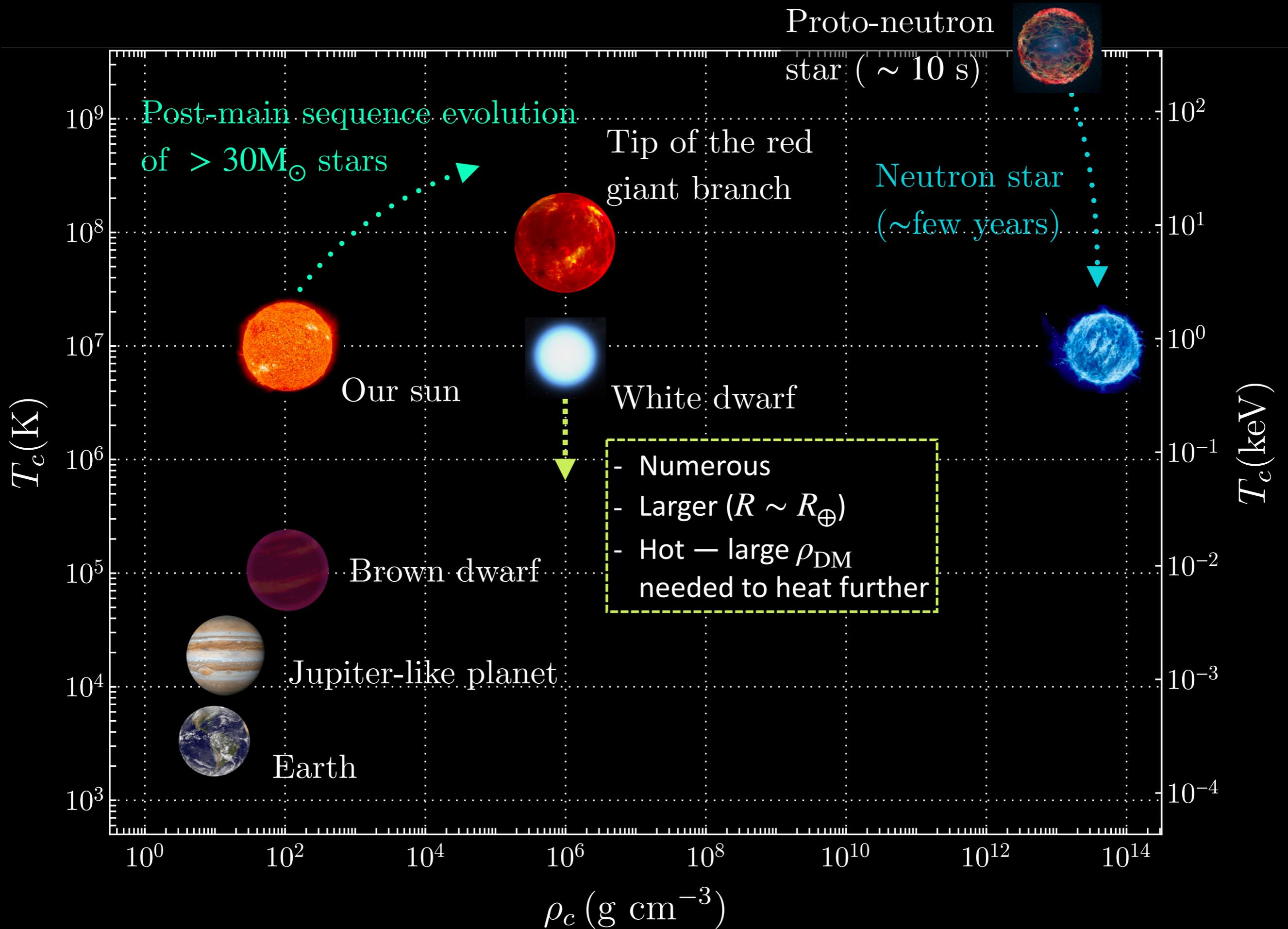
Dark matter heating

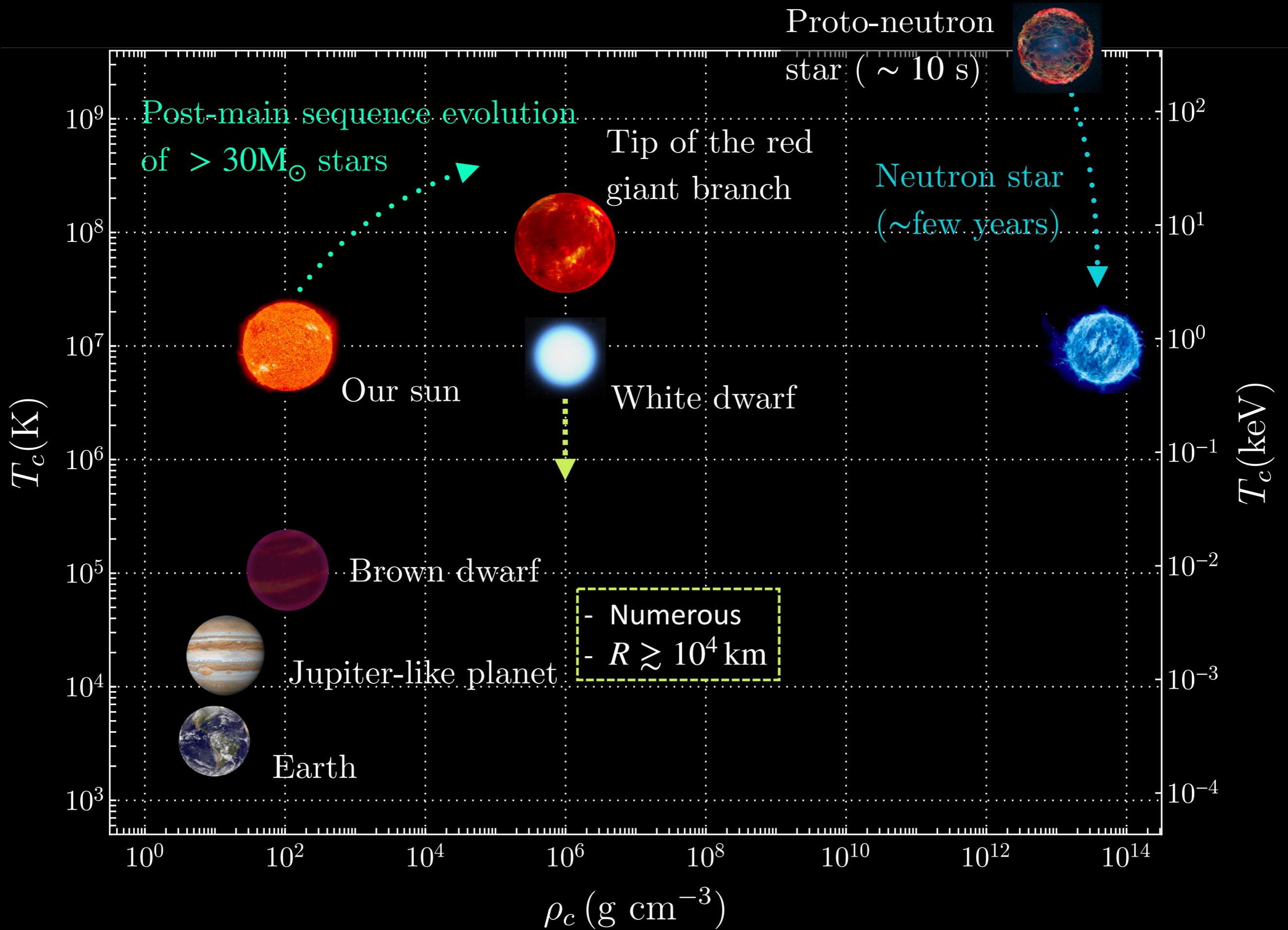
- Typically relevant for celestial objects **without** nuclear burning
- Sensitive to DM abundance ✓

Type of DM	signal	mass range	coupling range
DM with scattering and annihilation processes	Stars and planets overheating, or producing gamma rays/neutrinos	$\gtrsim \mathcal{O}(\text{keV})$ (depending on object and particle model)	$\sigma_{n\chi} \gtrsim 10^{-47} \text{ cm}^2$ (depending on object and particle model)
DM mixing with neutrons	NS overheating	$\lesssim 1.5 \text{ GeV}$	$10^{-17} \leq \epsilon_{nn'}/\text{eV} \leq 10^{-9}$

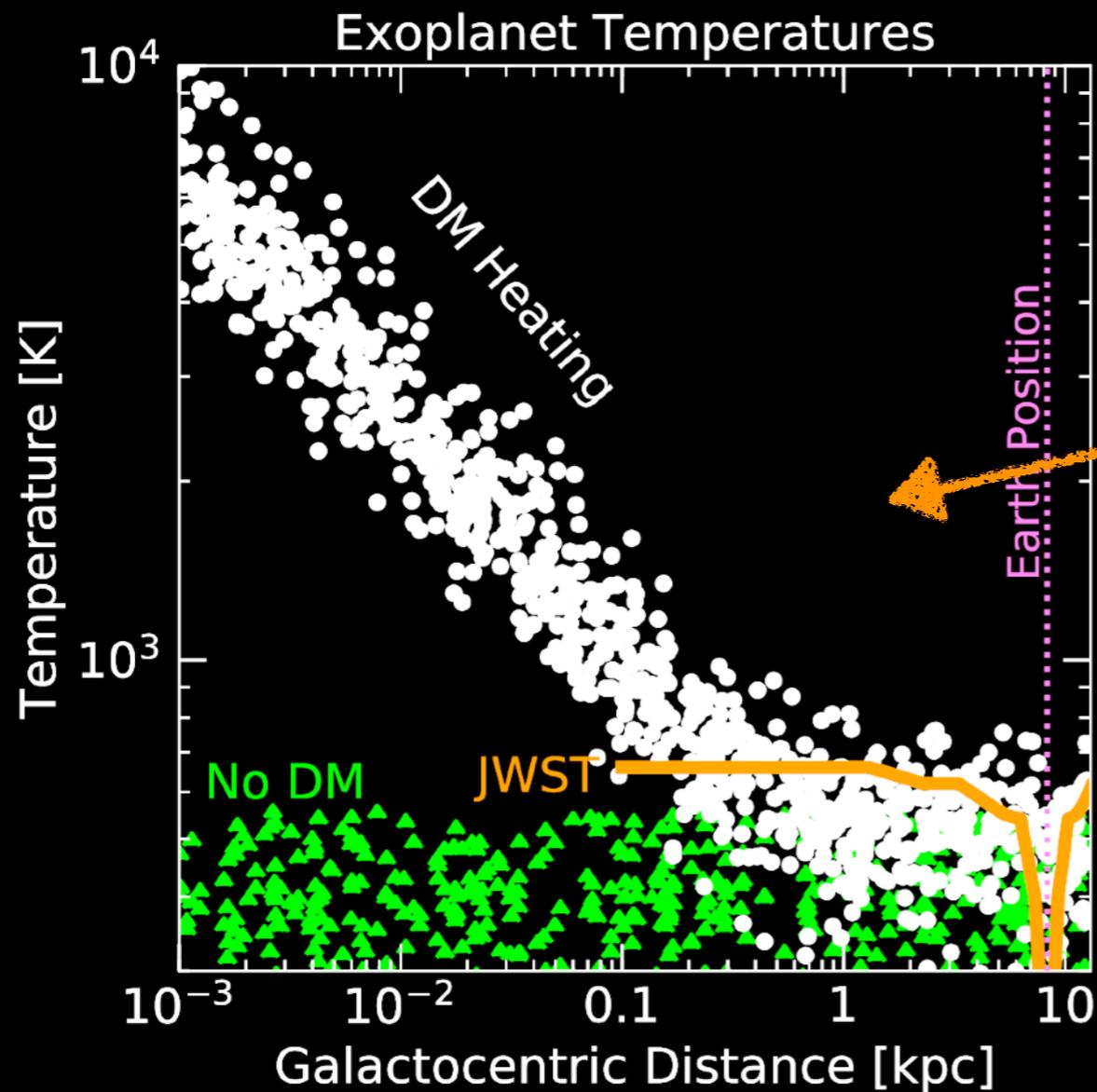








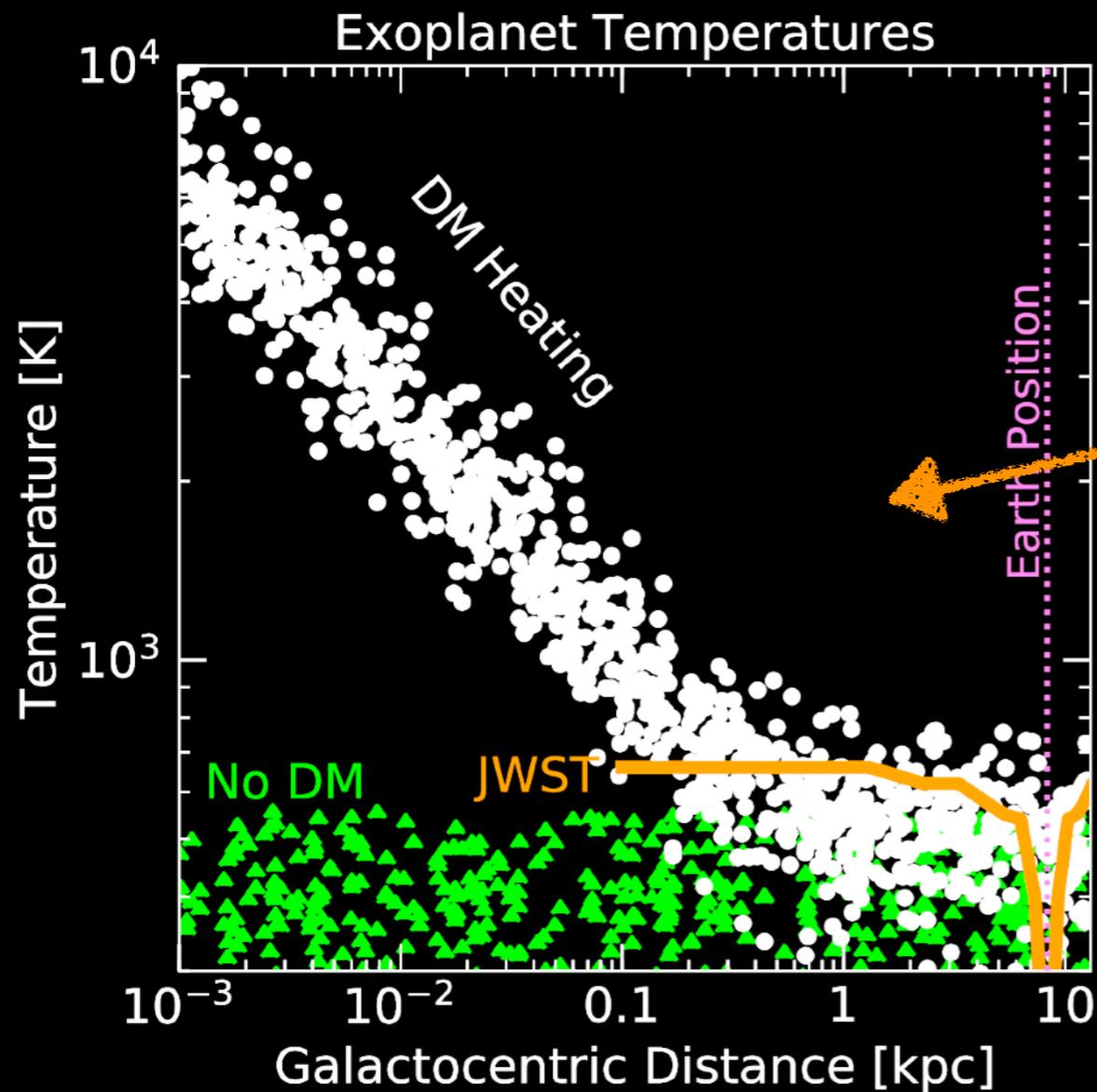
Exoplanet heating



- First be identified by e.g. Doppler spectroscopy or gravitational lensing
- Infrared telescopes (such as JWST) may be able to measure their temperature

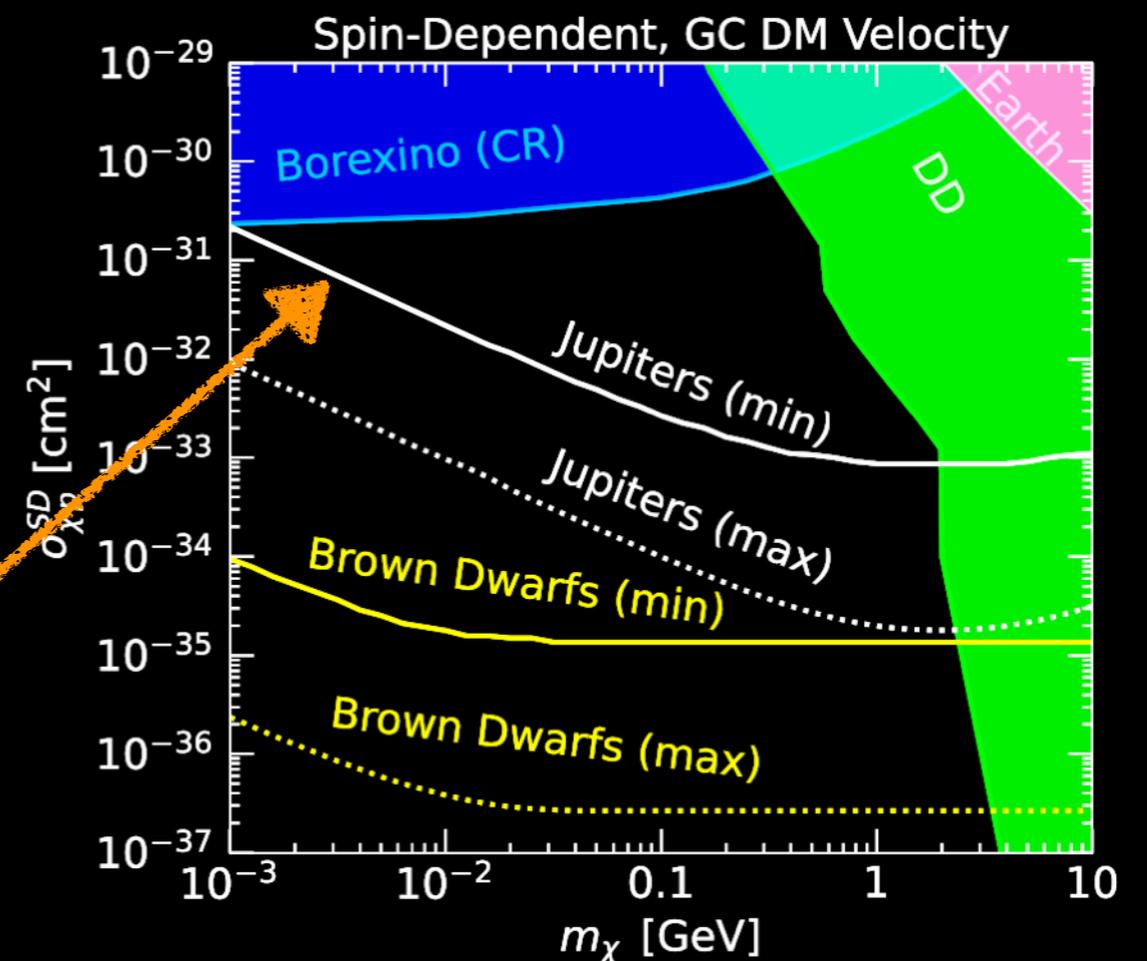
Assumption:
annihilation equilibrium

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all DM captured

Formation of Jovian planets

... a sensitive process

“If we could not see Jupiter with our own eyes, we might not believe that such a planet could exist anywhere.”

Formation of Jovian planets

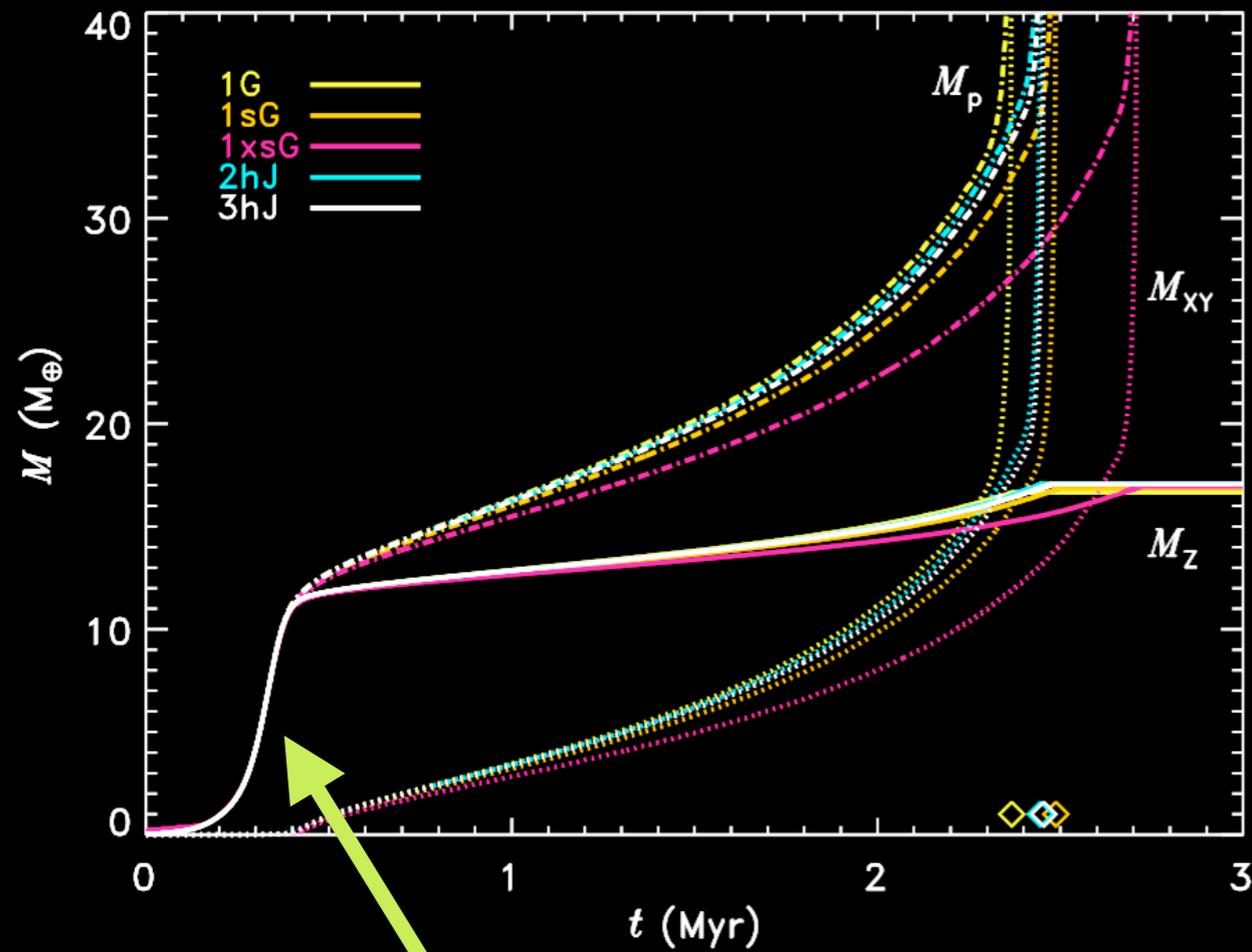
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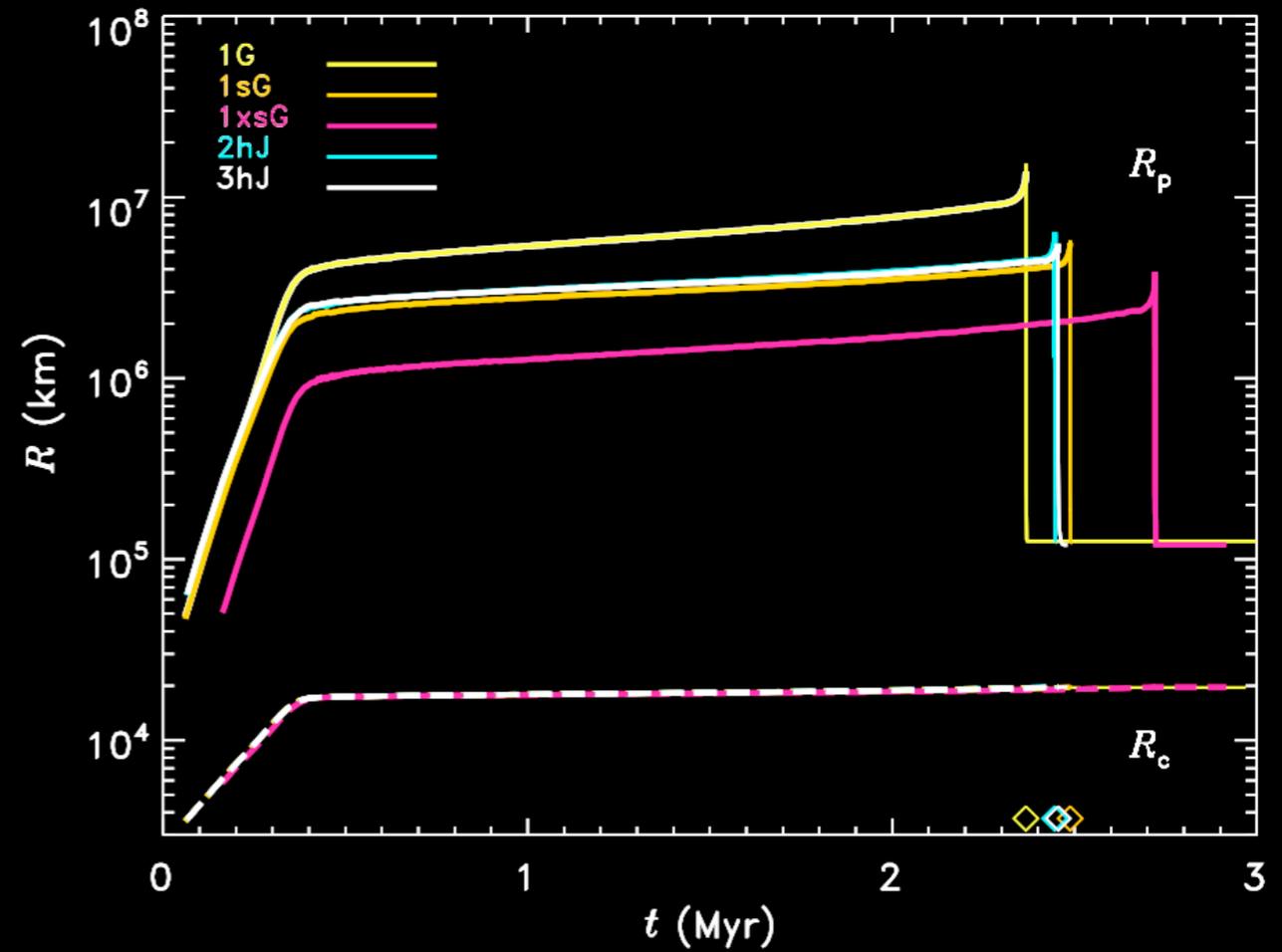
(Jupiter had less than ten million years to capture all of its gas because the Sun expelled most of the gas in the solar system shortly after thermonuclear fusion was initiated in its core)

Formation of Jovian planets

Core accretion gas capture theory

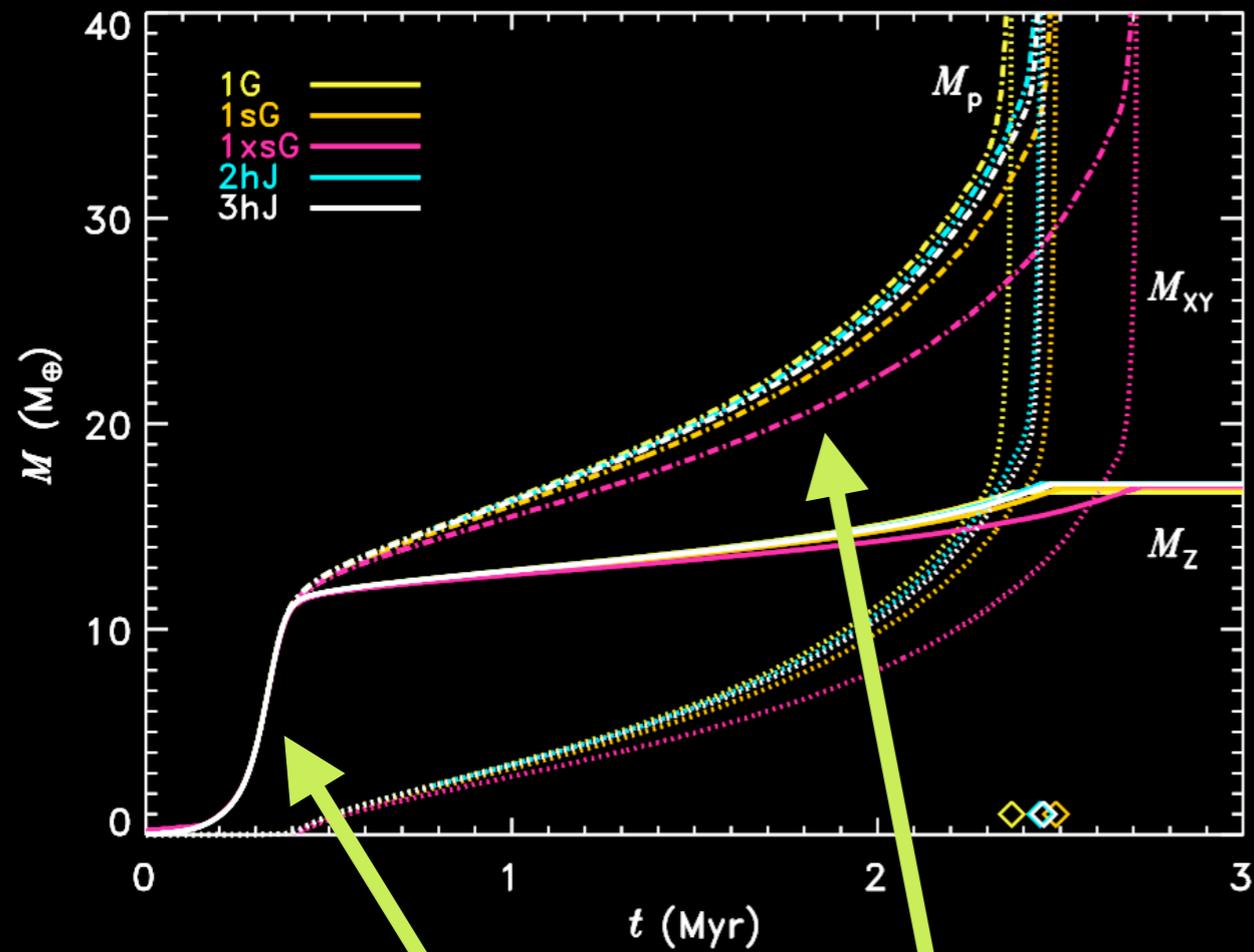


1. Core accretion



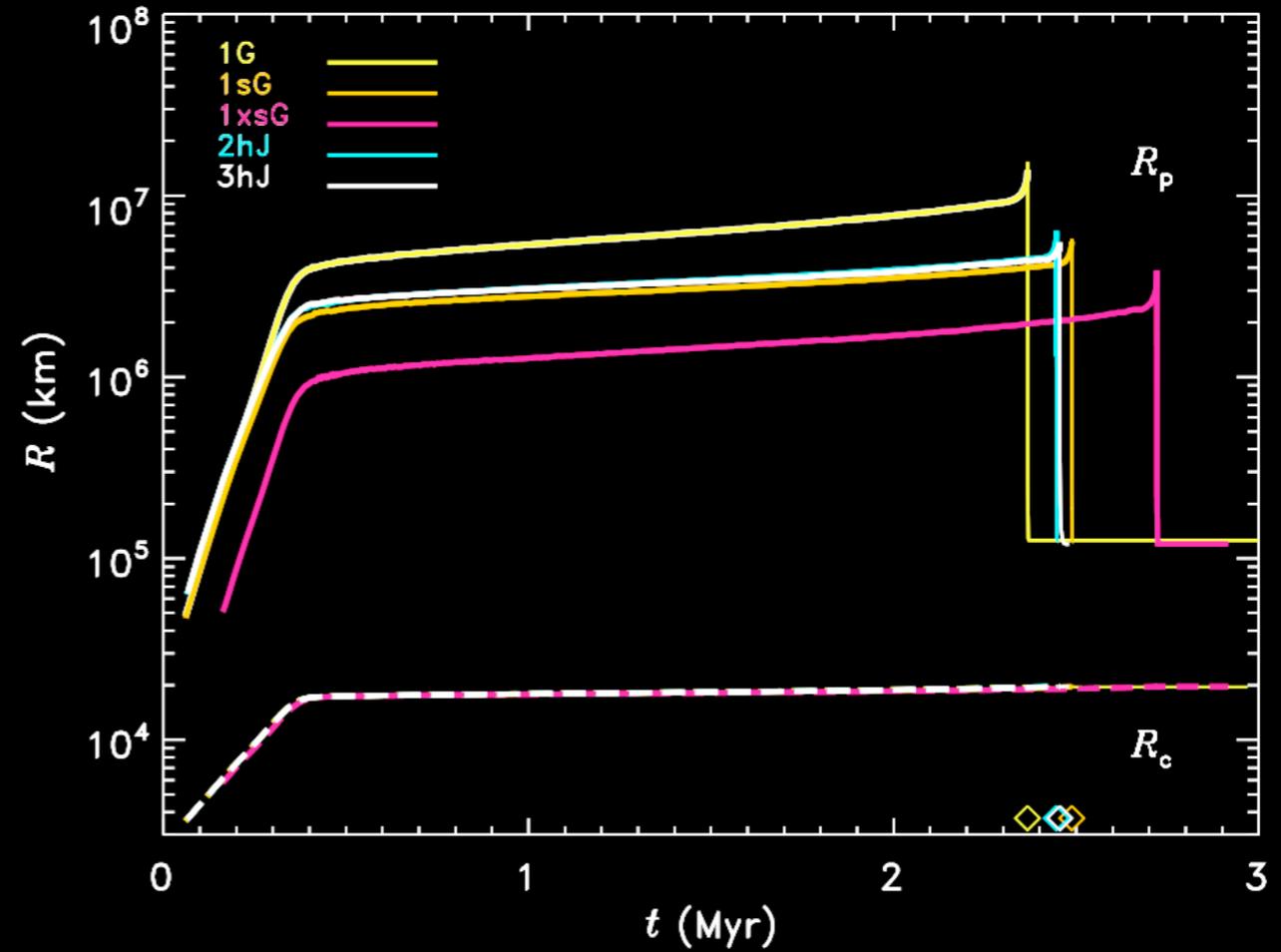
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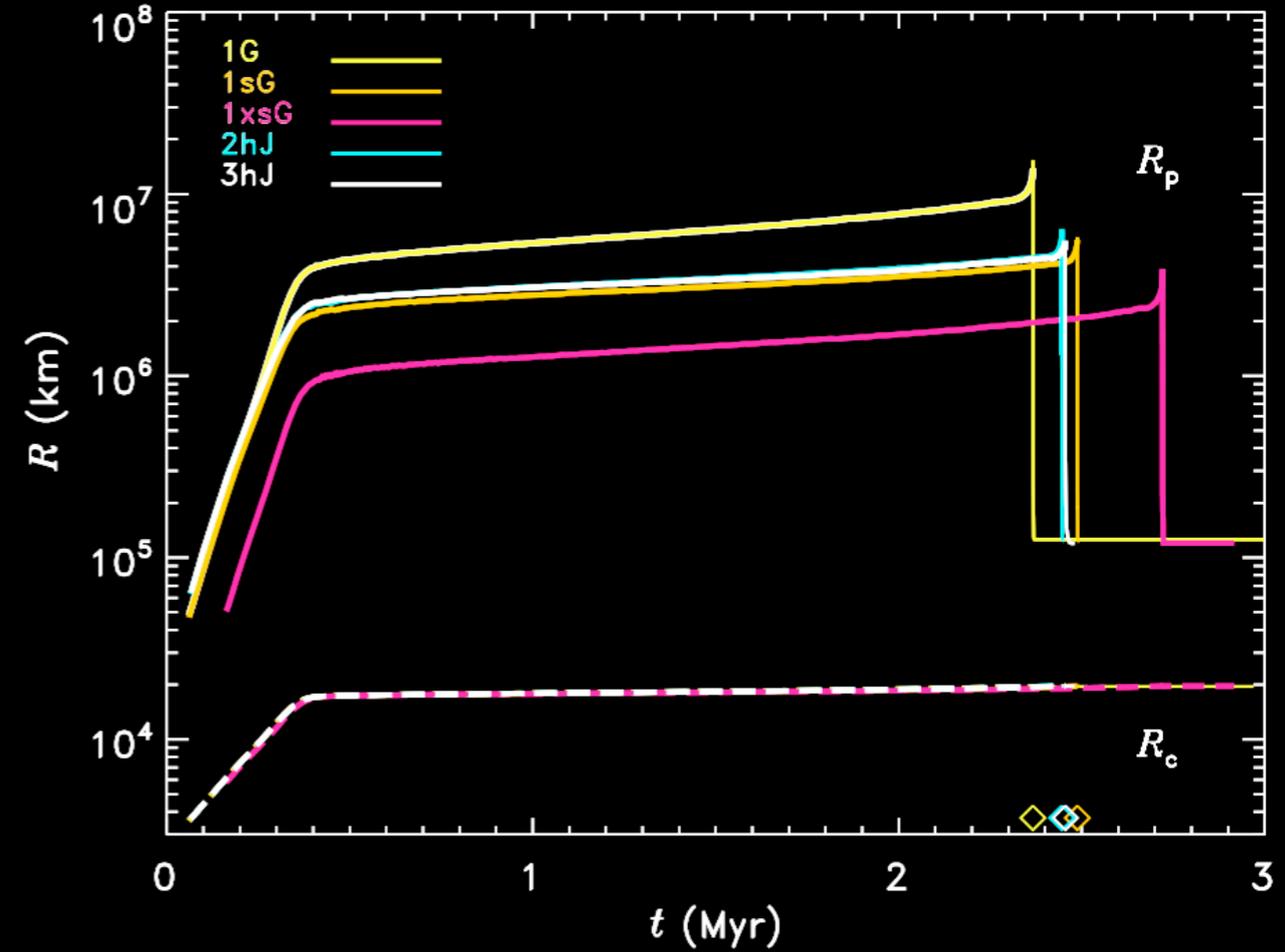
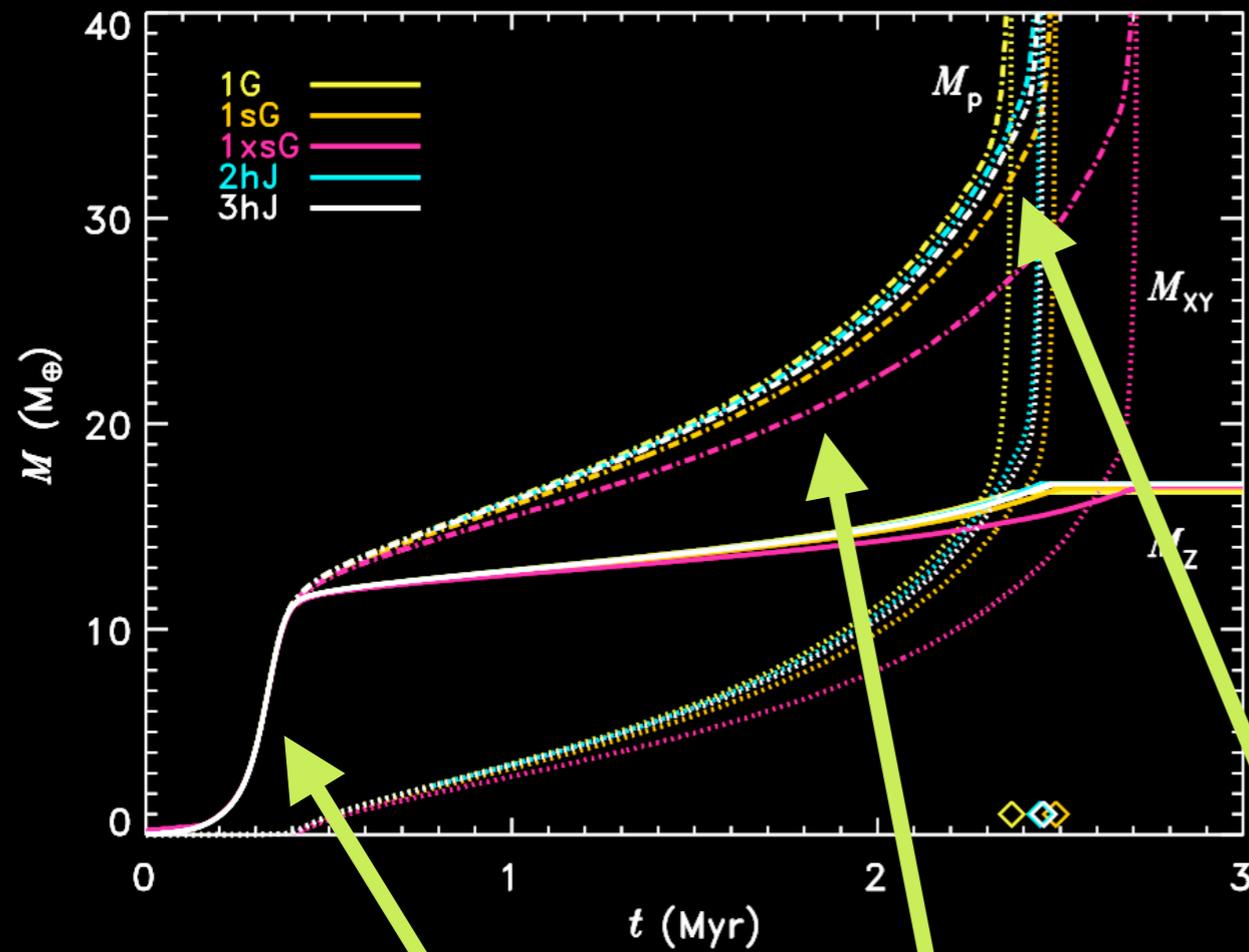
1. Core accretion

2. Gas capture



Formation of Jovian planets

Core accretion gas capture theory



1. Core accretion

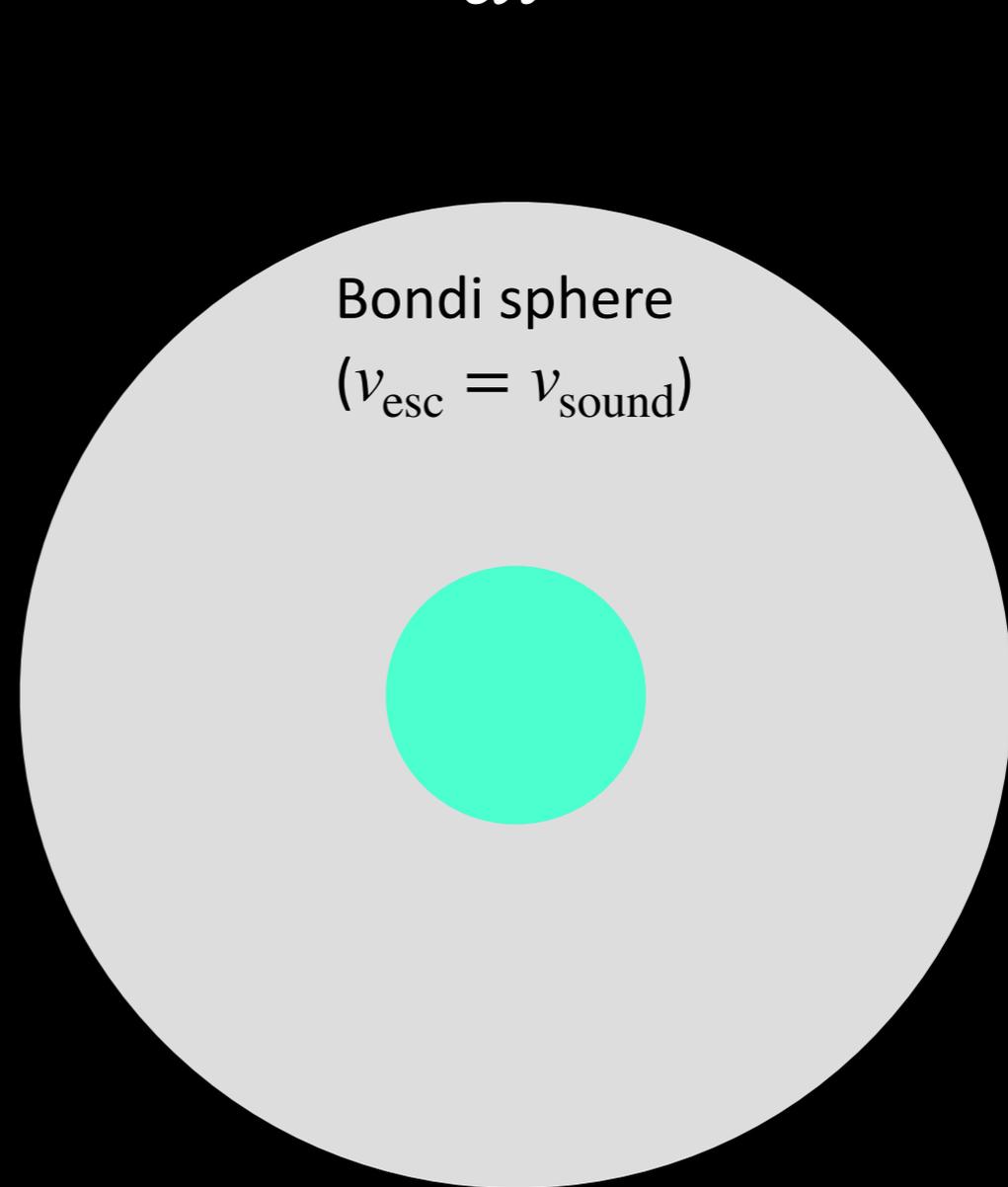
2. Gas capture

3. Runaway

Formation of Jovian planets

- Kelvin-Helmholtz contraction: $\dot{Q} = -\frac{dU}{dt}$

Fills up, gas
needs to contract



Formation of Jovian planets with DM

- Kelvin-Helmholtz contraction: $\dot{Q} - L_{\text{DM}}(R) = -\frac{dU}{dt}$

$$4\pi R^2 \times \sigma_{\text{SB}} T^4 - L_{\text{DM}}(R) = c_1 \frac{GM^2}{R^2} \frac{dR}{dt}$$

Proto-planet will have to
heat up more to radiate
enough energy to contract

Formation of Jovian planets **with DM**

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enough energy to contract

- But... the envelope is made up of light elements which can **evaporate**

A maximum temperature

Flux of escaping particles:

$$\Gamma_J(T) = \frac{nv}{2\sqrt{\pi}} \left(1 + \frac{v_{\text{esc}}^2}{v^2} \right) \exp \left(-\frac{v_{\text{esc}}^2}{v^2} \right) \Big|_T$$

$$v = \sqrt{2T/m}$$


Jeans, the dynamical theory of gases

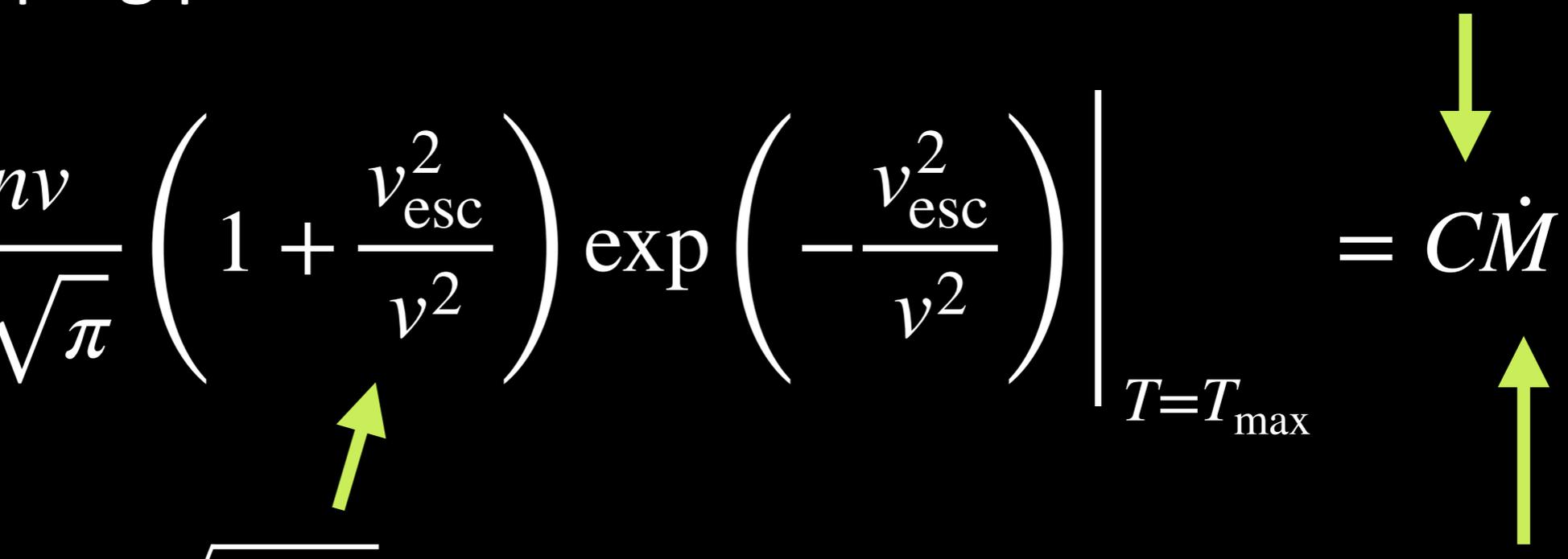
A maximum temperature

Flux of escaping particles:

Conservative assumption: $C = 10$

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Growth of the planet
in the absence of DM heat

e.g. Lissauer et al, Icarus 199, arXiv:0810.5186
d'Angelo et al, Icarus 355, arXiv:2009.05575

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Growth of the planet
in the absence of DM heat

→ for ^1H ,

- In the core $T_{\text{max}} \sim 10^3 \text{ K}$
- In the envelope, $T_{\text{max}} \sim 8 \text{ K}$

*e.g. Lissauer et al, Icarus 199, arXiv:0810.5186
d'Angelo et al, Icarus 355, arXiv:2009.05575*

Dark matter halts accretion

- Then, DM can halt accretion for injections with

$$L_{\text{DM}} \geq 4\pi R^2 \sigma T_{\text{max}}^4$$

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$$\begin{aligned} L_{\text{DM}} &\geq 4\pi R^2 \sigma T_{\text{max}}^4 \\ &\geq 4 \times 10^{-8} \times \left(\frac{R}{10^3 R_p} \right)^2 \left(\frac{T_{\text{max}}}{8\text{K}} \right)^4 L_{\odot} \end{aligned}$$

Can we expect such injections to be reached?

Dark matter halts accretion

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- In capture-annihilation equilibrium,

$$L_{\text{DM}} = m_{\text{DM}} C_{\text{cap}}$$

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- In capture-annihilation equilibrium,

$$L_{\text{DM}} = m_{\text{DM}} C_{\text{cap}} = m_{\text{DM}} f_{\text{cap}} \Phi$$

$$\Phi = v_{\text{DM}} \sqrt{\frac{8}{3\pi}} \frac{\rho_{\text{DM}}}{m_{\text{DM}}} \left(1 + \frac{3}{2} \frac{v_{\text{esc}}^2}{v_{\text{DM}}^2} \right)$$

$$\sim 2 \times 10^{-9} f_{\text{cap}} \left(\frac{R}{10^3 R_p} \right) \left(\frac{M}{10 M_{\oplus}} \right) \left(\frac{v_{\text{DM}}}{270 \text{ km s}^{-1}} \right)^{-1} \left(\frac{\rho_{\text{DM}}}{0.42 \text{ GeV cm}^{-3}} \right) L_{\odot}$$

Dark matter halts accretion

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Capture-annihilation equilibrium

• Boltzmann equation: $\frac{dN}{dt} = C_{\text{cap}} - C_{\text{ann}} N_{\chi}^2$

$$C_{\text{ann}} = \langle \sigma_{\text{ann}} v \rangle / V_{\text{eff}} = \langle \sigma_{\text{ann}} v \rangle \frac{\int_V n_{\chi}^2}{\int_V n_{\chi}}$$


Capture-annihilation equilibrium

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$$C_{\text{ann}} = \langle \sigma_{\text{ann}} v \rangle / V_{\text{eff}} = \langle \sigma_{\text{ann}} v \rangle \frac{\int_V n_{\chi}^2}{\int_V n_{\chi}}$$


- In capture-annihilation equilibrium, $N_{\chi} \sim \sqrt{C_{\text{cap}}/C_{\text{ann}}}$,
reached after

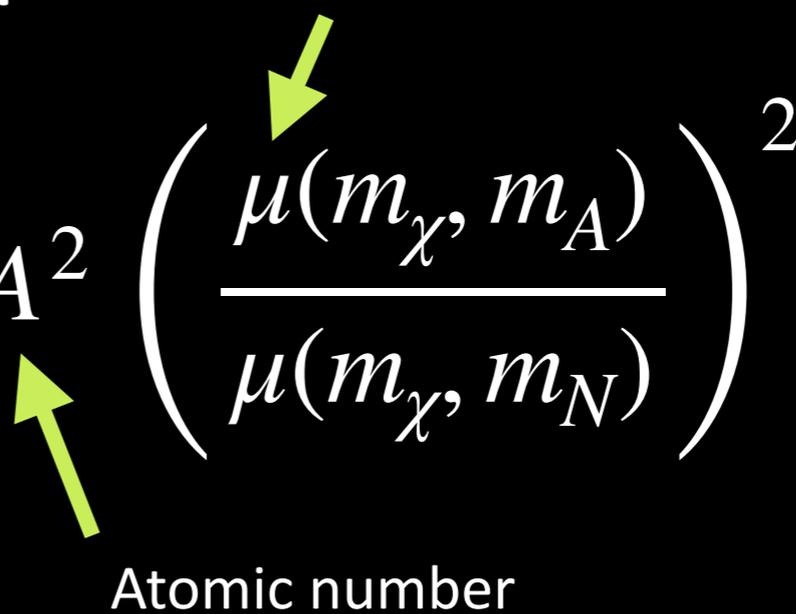
$$\tau \sim (C_{\text{cap}} C_{\text{ann}})^{-1/2} \approx \sqrt{\frac{m_{\chi}}{\text{GeV}} \frac{10^{-30} \text{cm}^3/\text{s}}{\langle \sigma_{\text{ann}} v \rangle}} \text{Myr}$$

The capture fraction

- Spin-independent: $\sigma_{\text{SI}} = \sigma_{\chi N}^{\text{SI}} A^2 \left(\frac{\mu(m_\chi, m_A)}{\mu(m_\chi, m_N)} \right)^2$

Reduced mass

Atomic number



The capture fraction

- Spin-independent: $\sigma_{\text{SI}} = \sigma_{\chi N}^{\text{SI}} A^2 \left(\frac{\mu(m_\chi, m_A)}{\mu(m_\chi, m_N)} \right)^2$

- Spin-dependent:

$$\sigma_{SD} = \sigma_{\chi N}^{\text{SD}} \frac{4(J_A + 1)}{3J_A} \left[a_p \langle S_p \rangle + a_n \langle S_n \rangle \right]^2 \left(\frac{\mu(m_\chi, m_A)}{\mu(m_\chi, m_N)} \right)^2$$

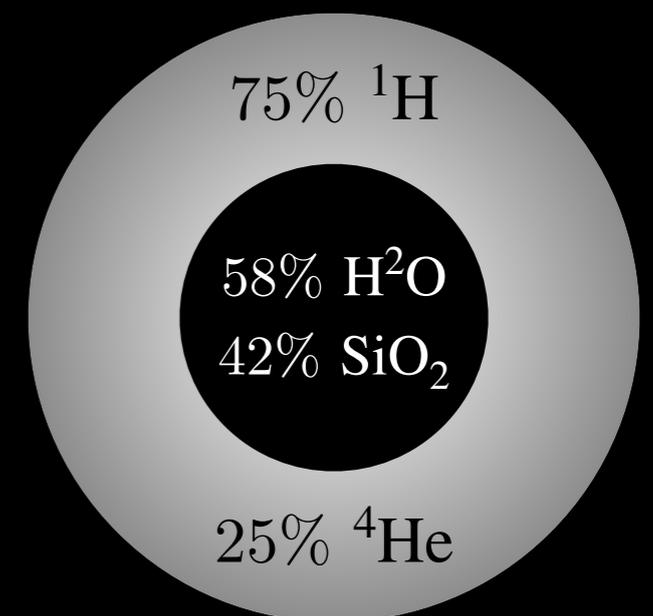
Nuclear spin

Average proton,
neutron spin

The capture fraction

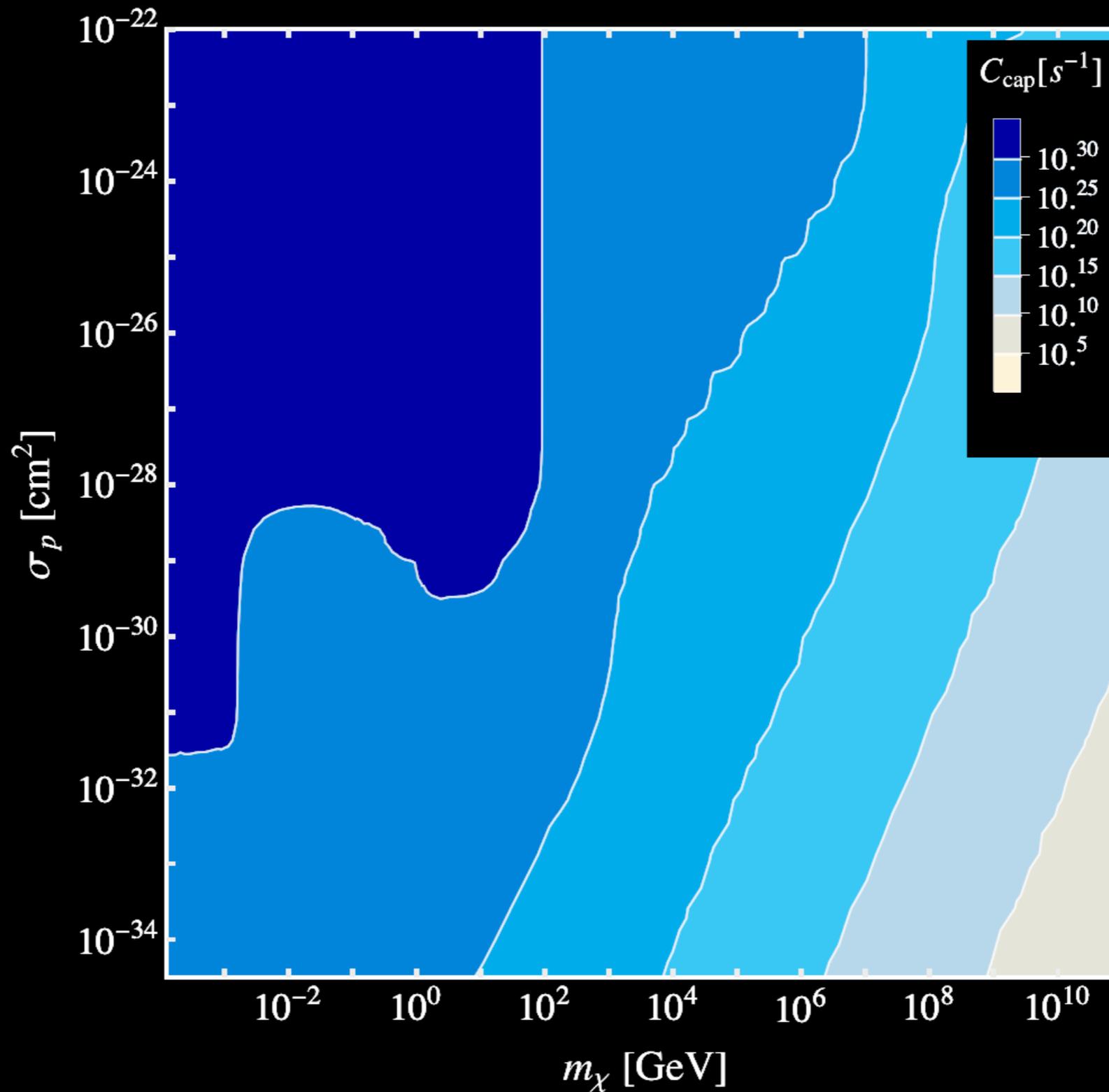
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 $a_p = 1, a_n = 0$

Isotopes	^{17}O	^{29}Si	^1H
Abundance [%]	~ 0.4	~ 4.7	~ 100
J	$5/2$	$1/2$	$1/2$
$\langle S_p \rangle$	-0.036	0.054	0.5
$\langle S_n \rangle$	0.508	0.204	0

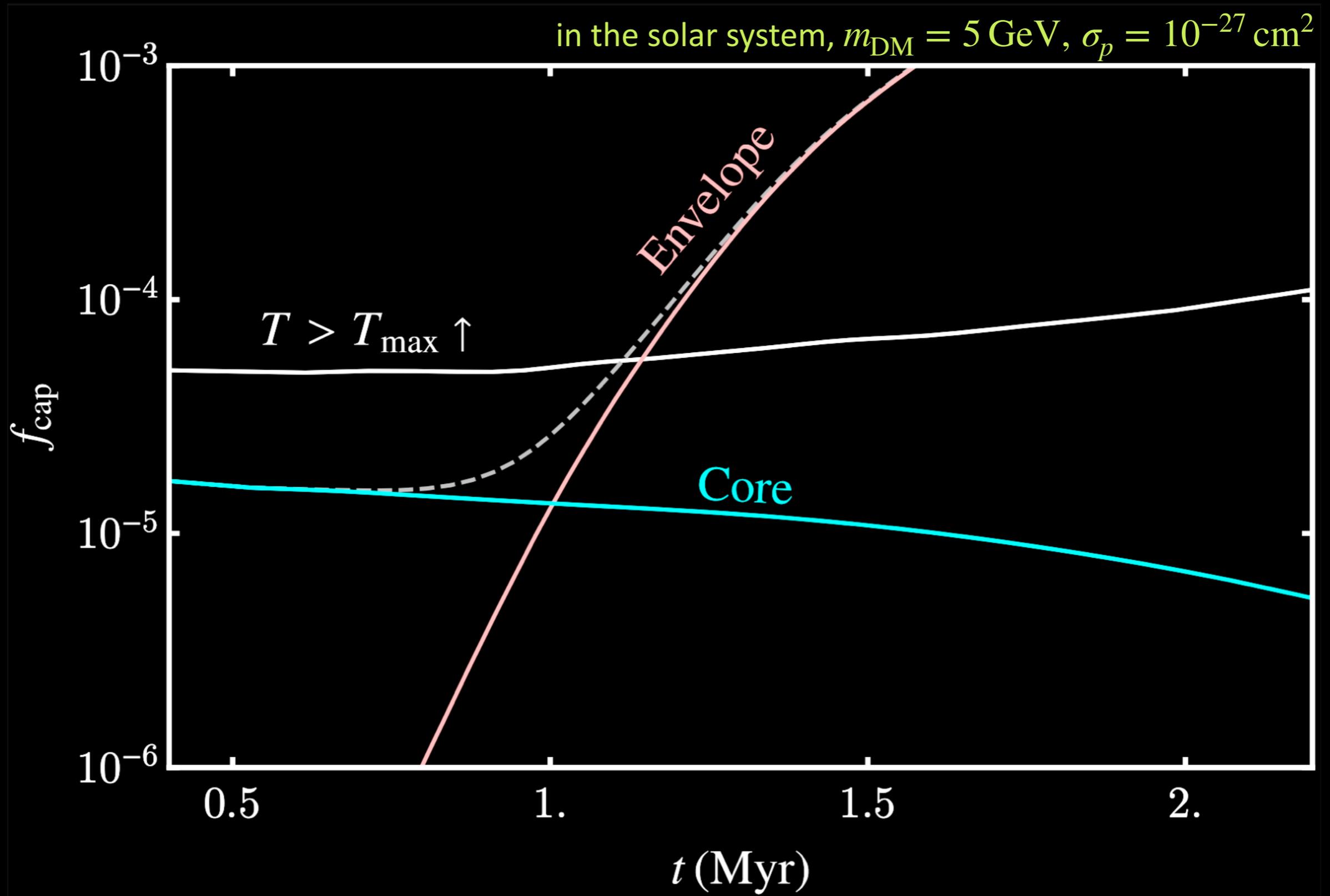


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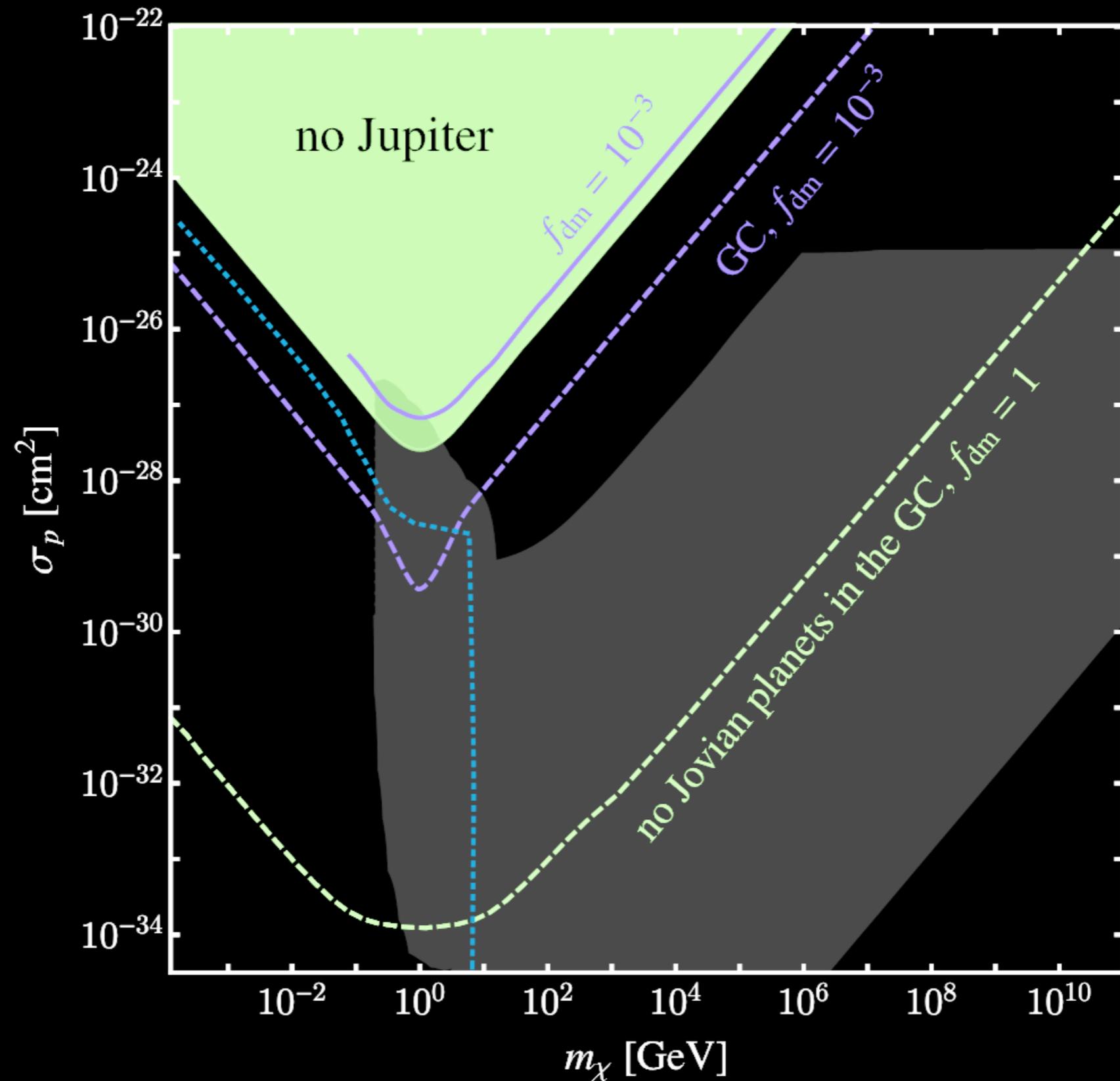
Spin-dependent example



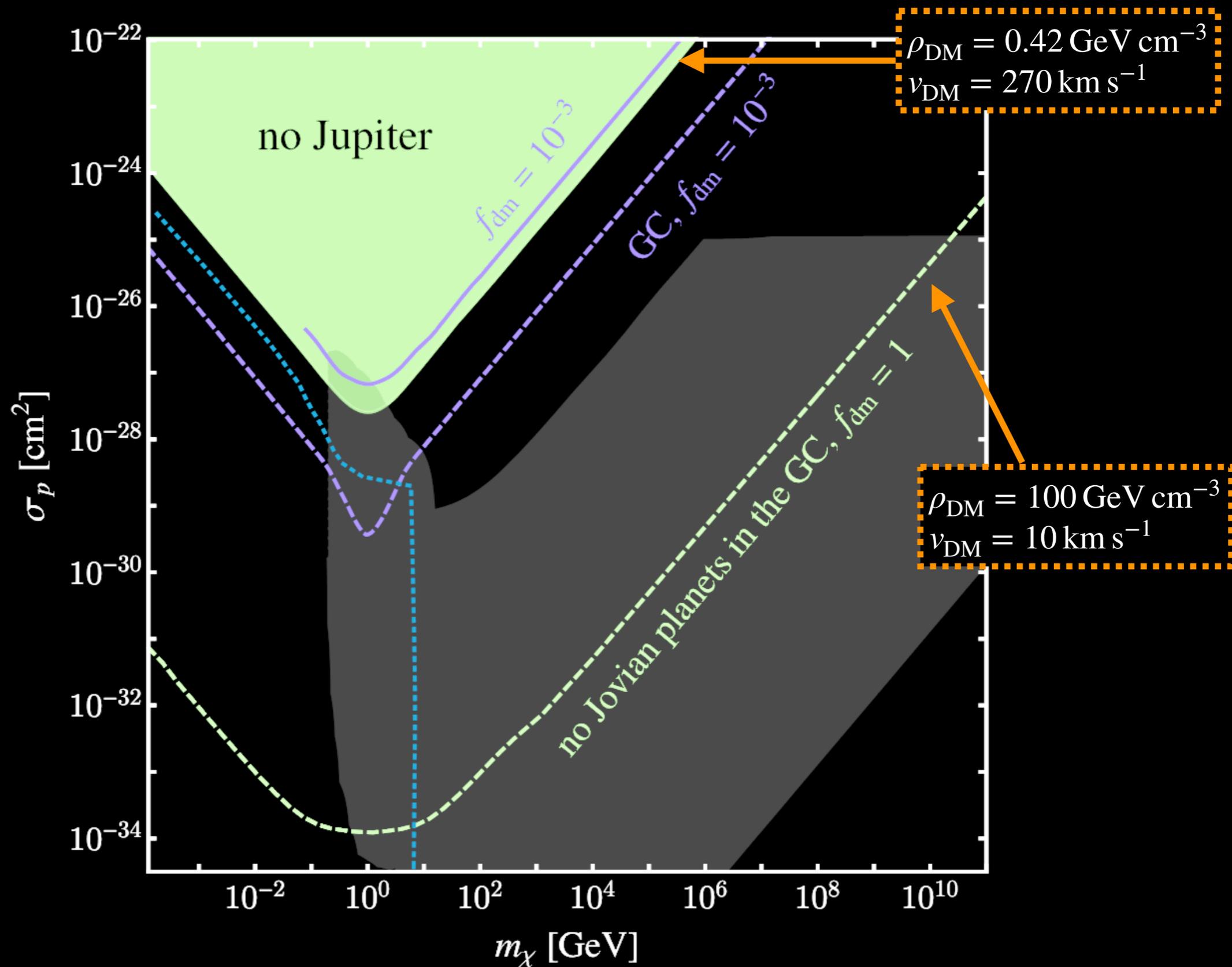
Formation of Jovian planets



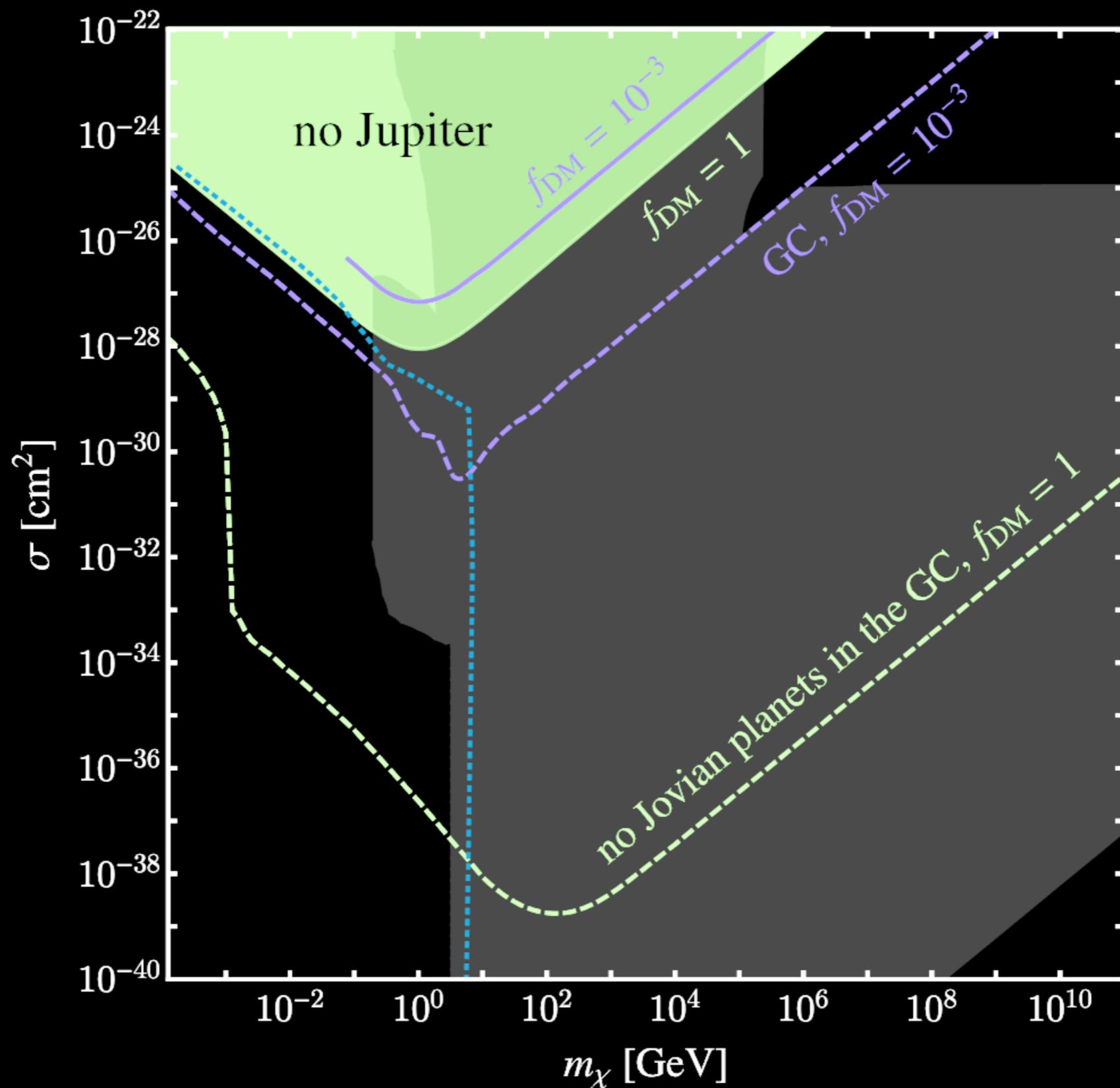
Constraints: spin-dependent DM



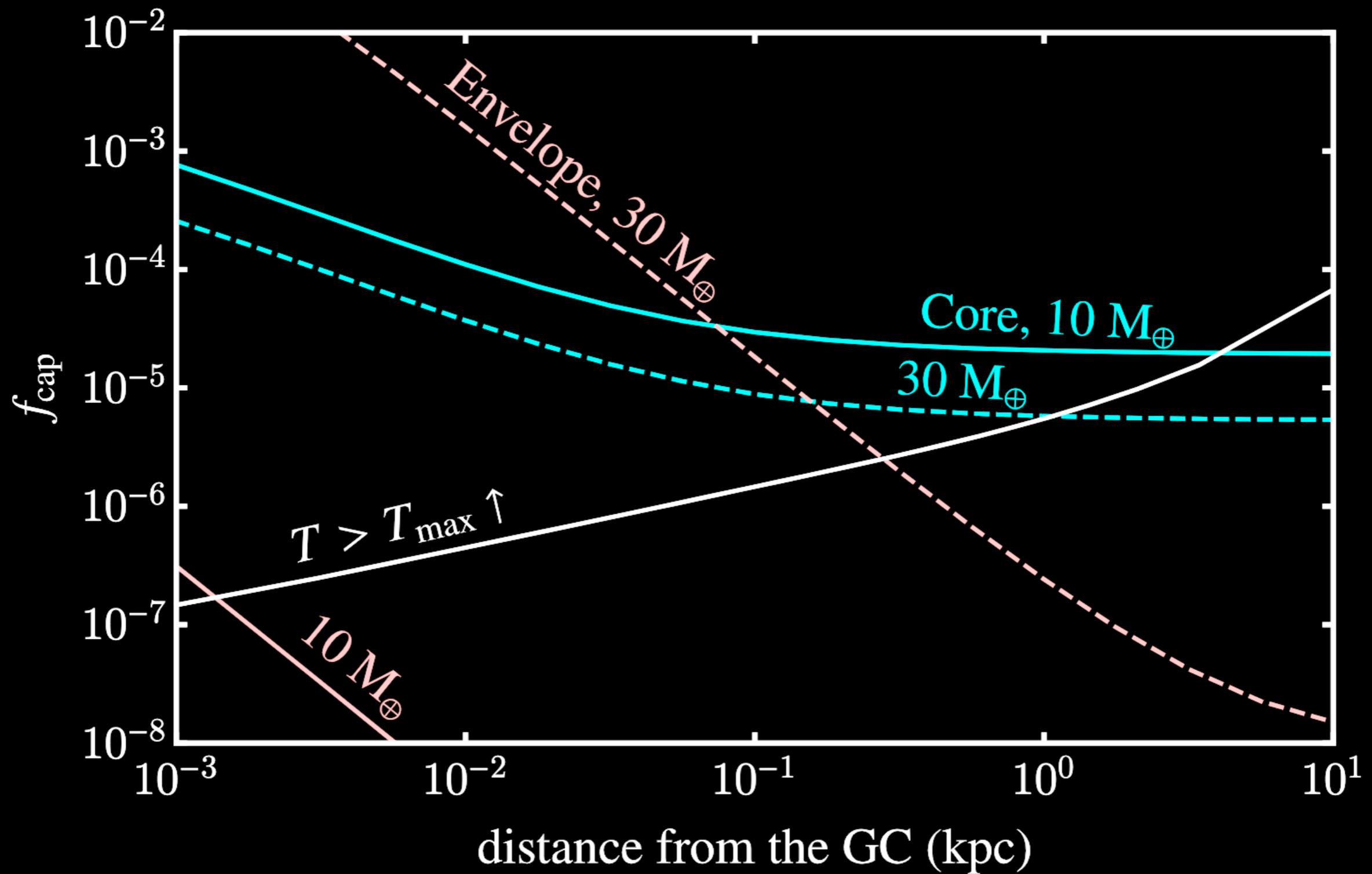
Constraints: spin-dependent DM



Constraints: spin-independent DM



Variation with distance from the GC



To conclude

- The formation of Jovian planets is very sensitive to extra heat sources
- (Relatively) strongly interacting dark matter may disrupt this formation at the onset of gas accretion, or at some point during its growth
 - The existence of Jupiter in our solar system can be used to constraint dark matter
 - Observations of Jovian planets in the Galactic Center lead to even stronger constraints
- Future work: simulations + direct observation of planet formation in the presence of DM heating

Thank you!

...ask me anything you like!

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