

SUB-GEV DARK MATTER IN THE LAB

NEW IDEAS AND NEW TOOLS

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OUTLINE

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- Searching for keV-GeV dark matter

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- Down to the MeV: Migdal effect

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- Down to the MeV: Migdal effect
- Down to the keV: collective excitations

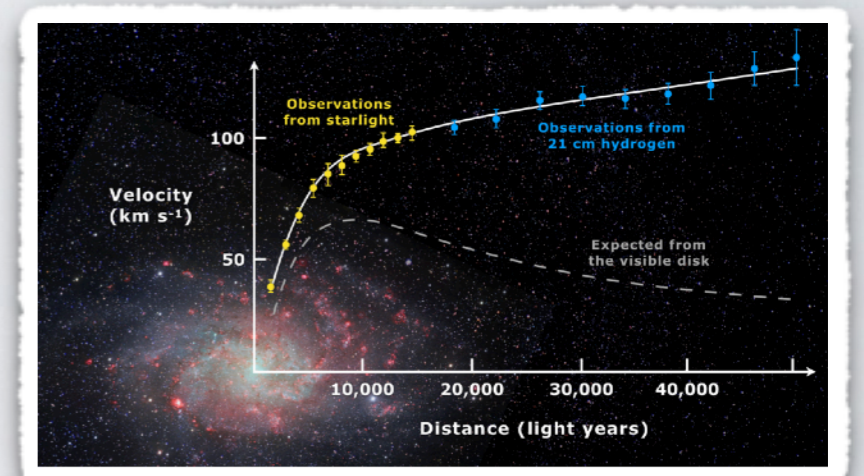
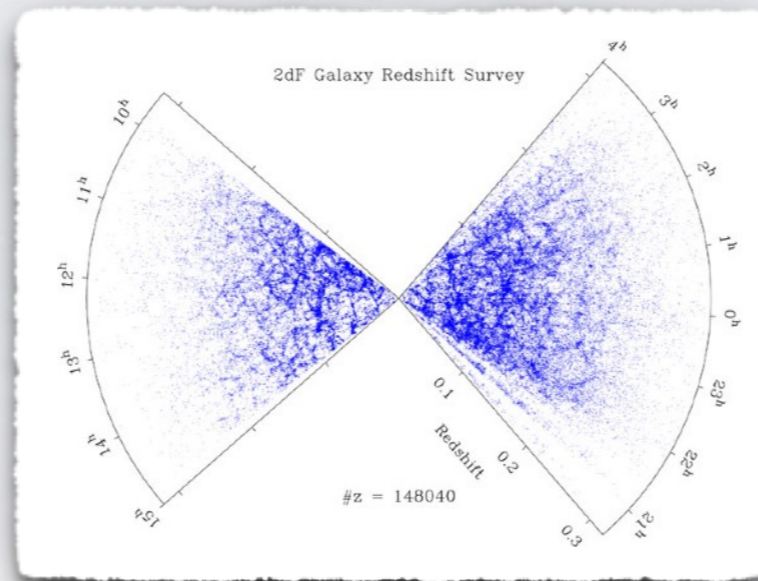
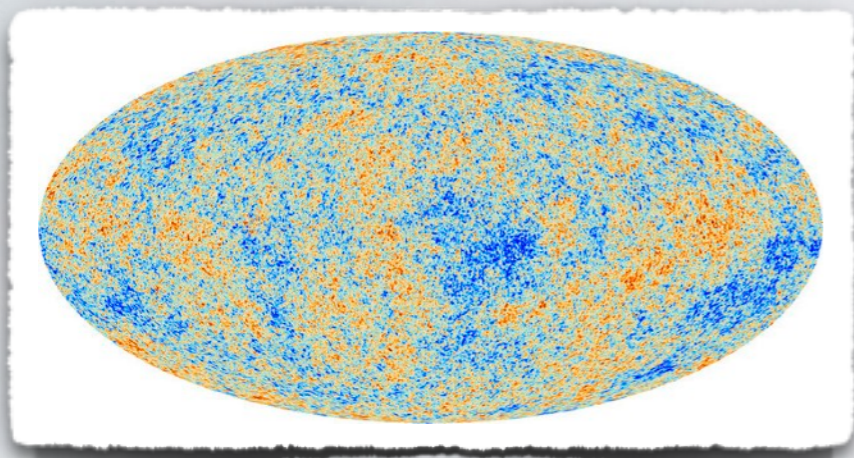
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- Searching for keV-GeV dark matter
- Down to the MeV: Migdal effect
- Down to the keV: collective excitations
- Outlook

SUB-GEV DARK MATTER

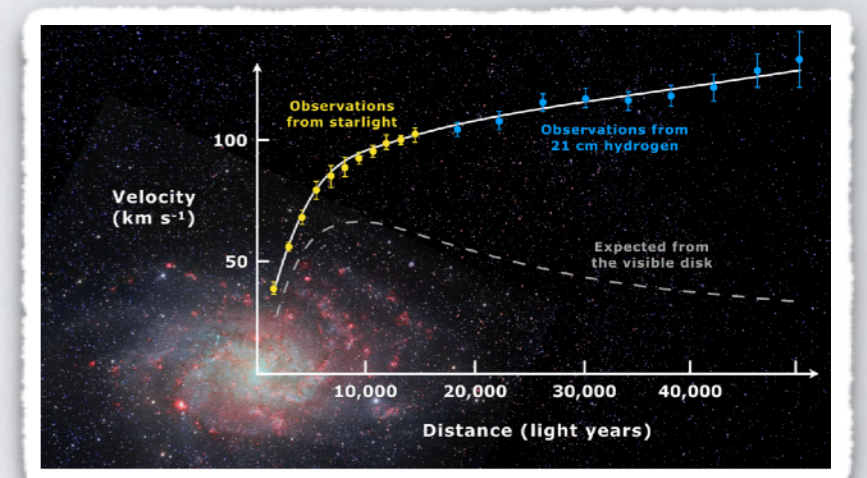
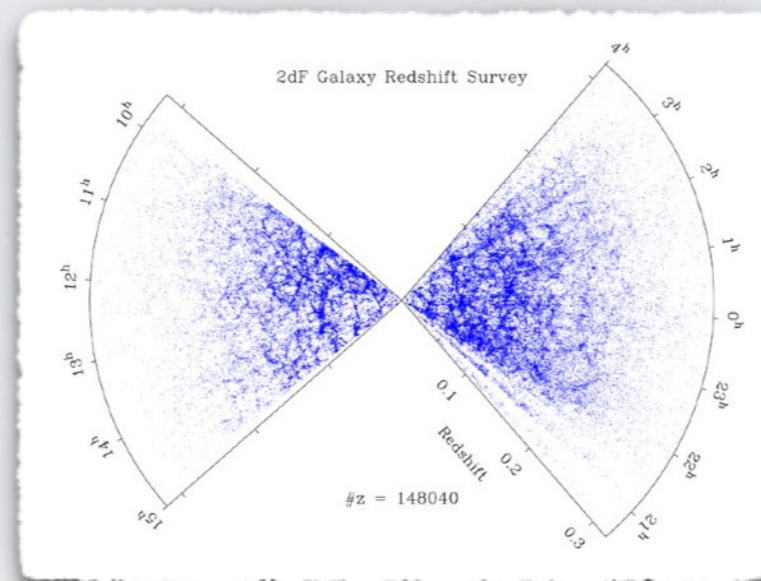
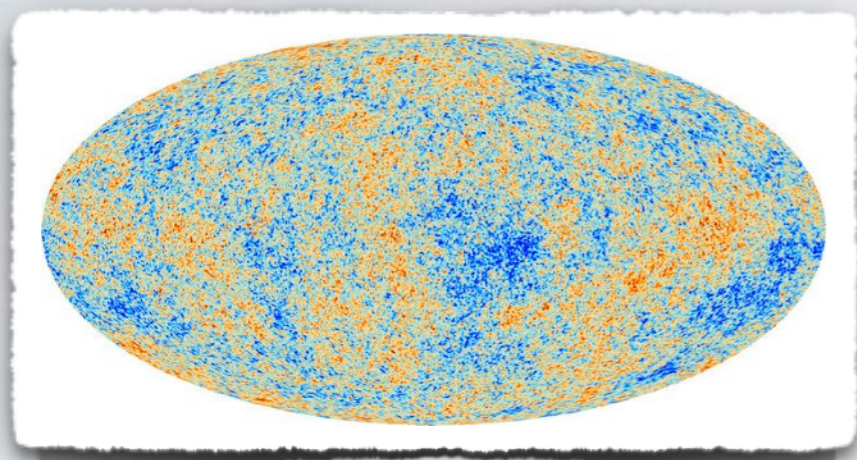
SUB-GEV DARK MATTER

- Most of the matter ($\sim 80\%$) that interacts gravitationally is dark



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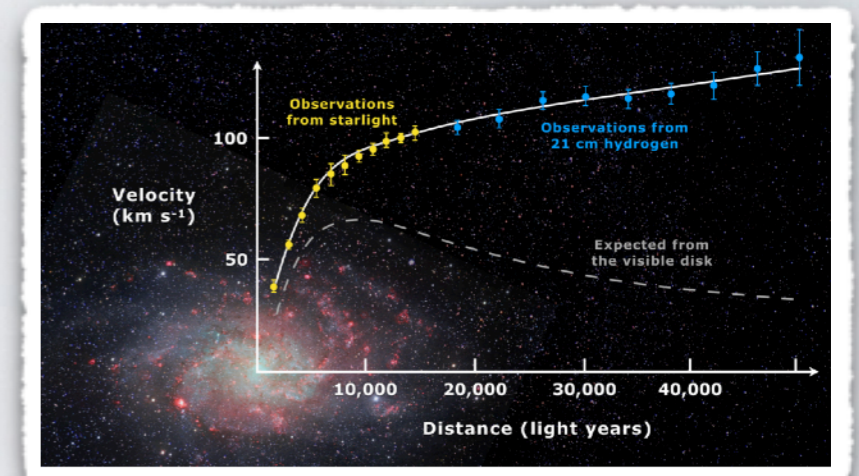
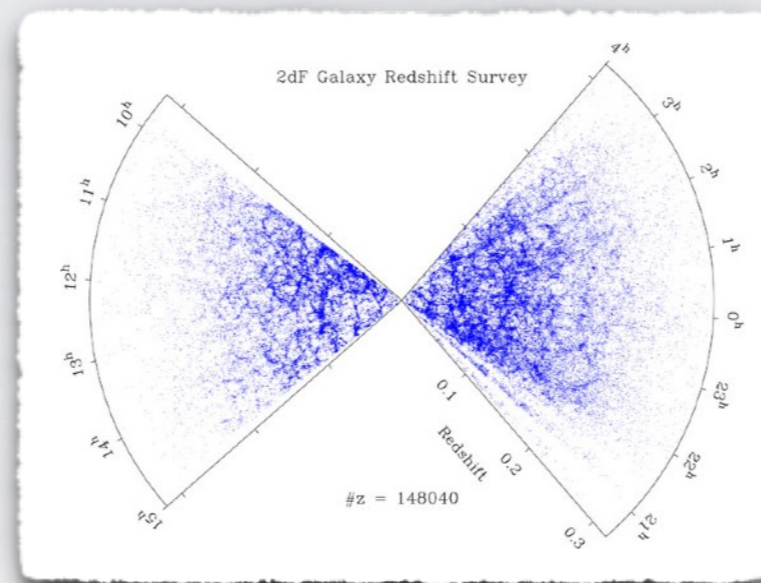
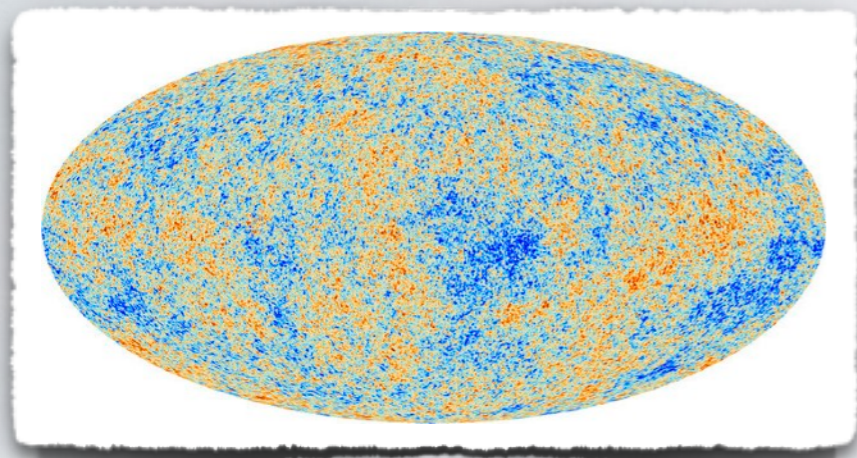
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- One of the strongest evidences for [physics beyond the Standard Model](#)

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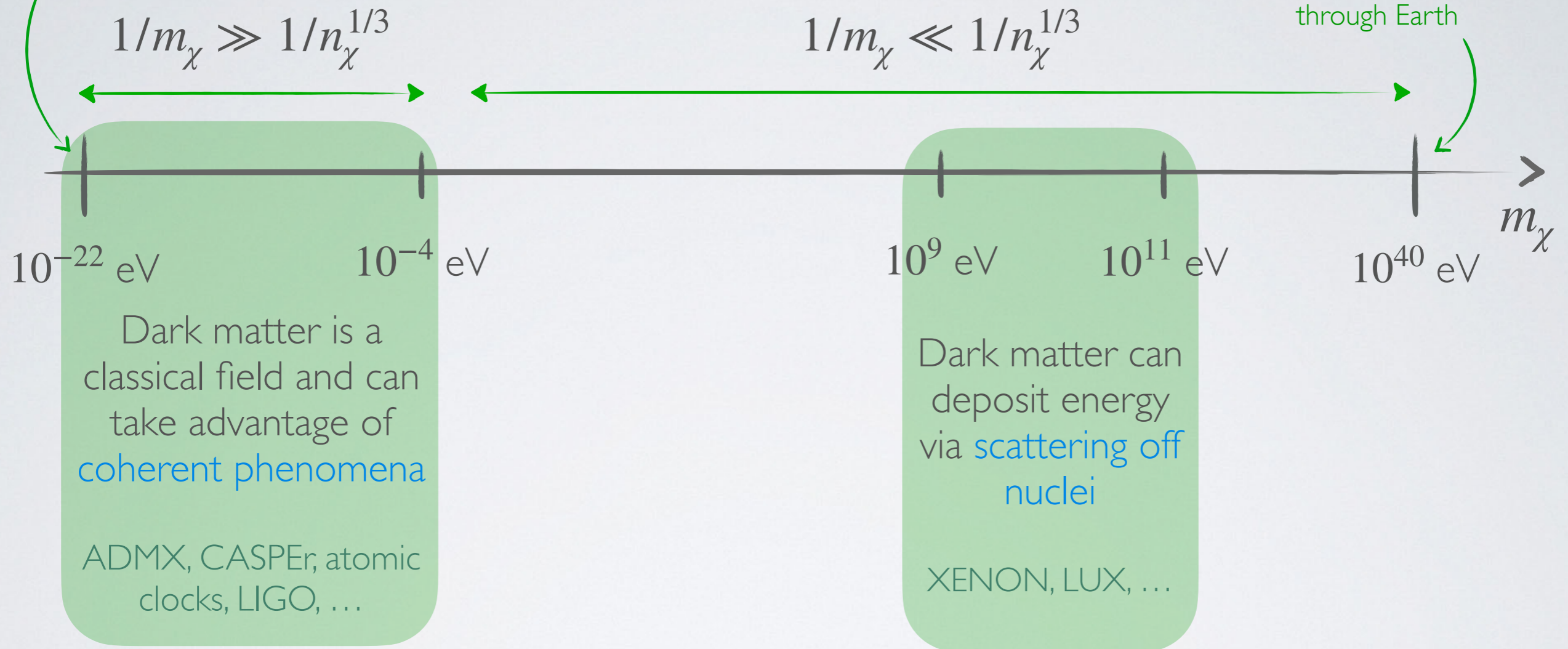
- One of the strongest evidences for physics beyond the Standard Model
- However... huge possible mass range → detection techniques vary widely depending on the dark matter mass

SUB-GEV DARK MATTER

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too light to explain halo structure

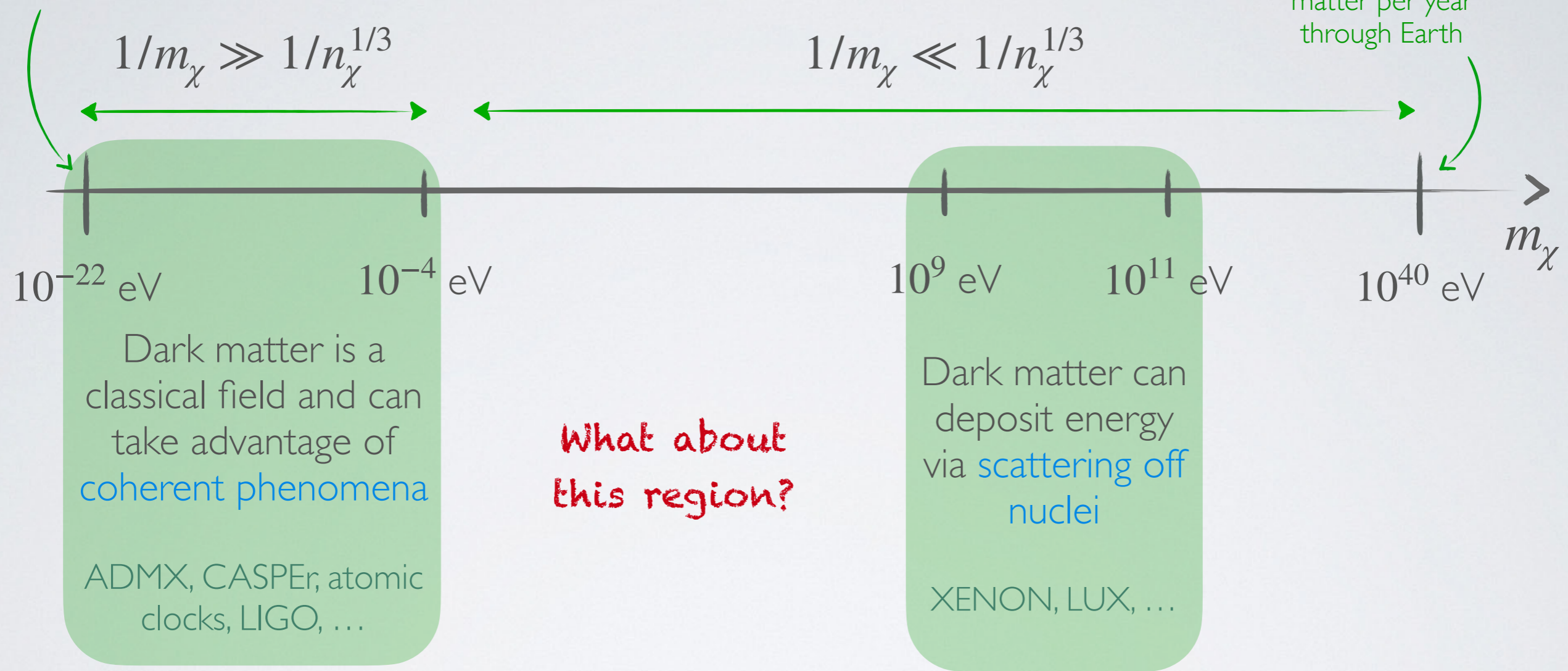
less than 1 dark matter per year through Earth



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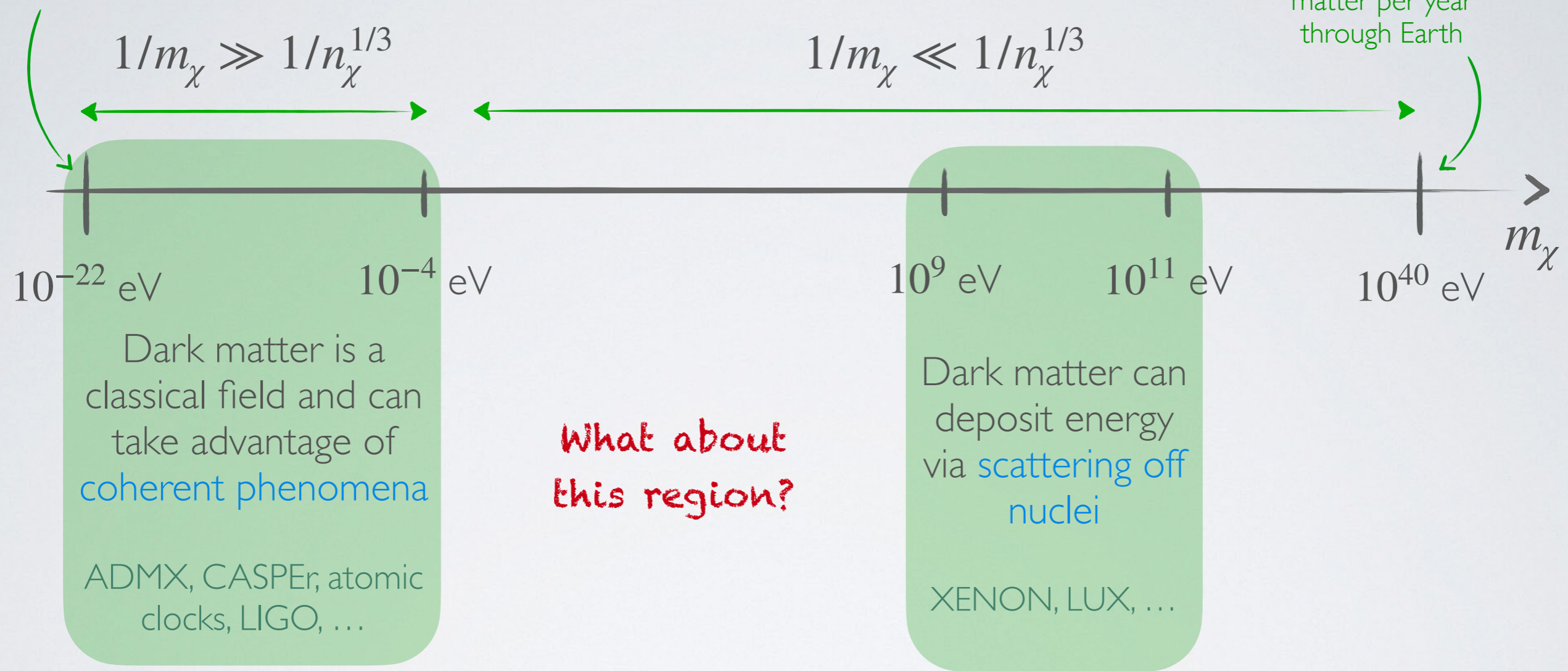
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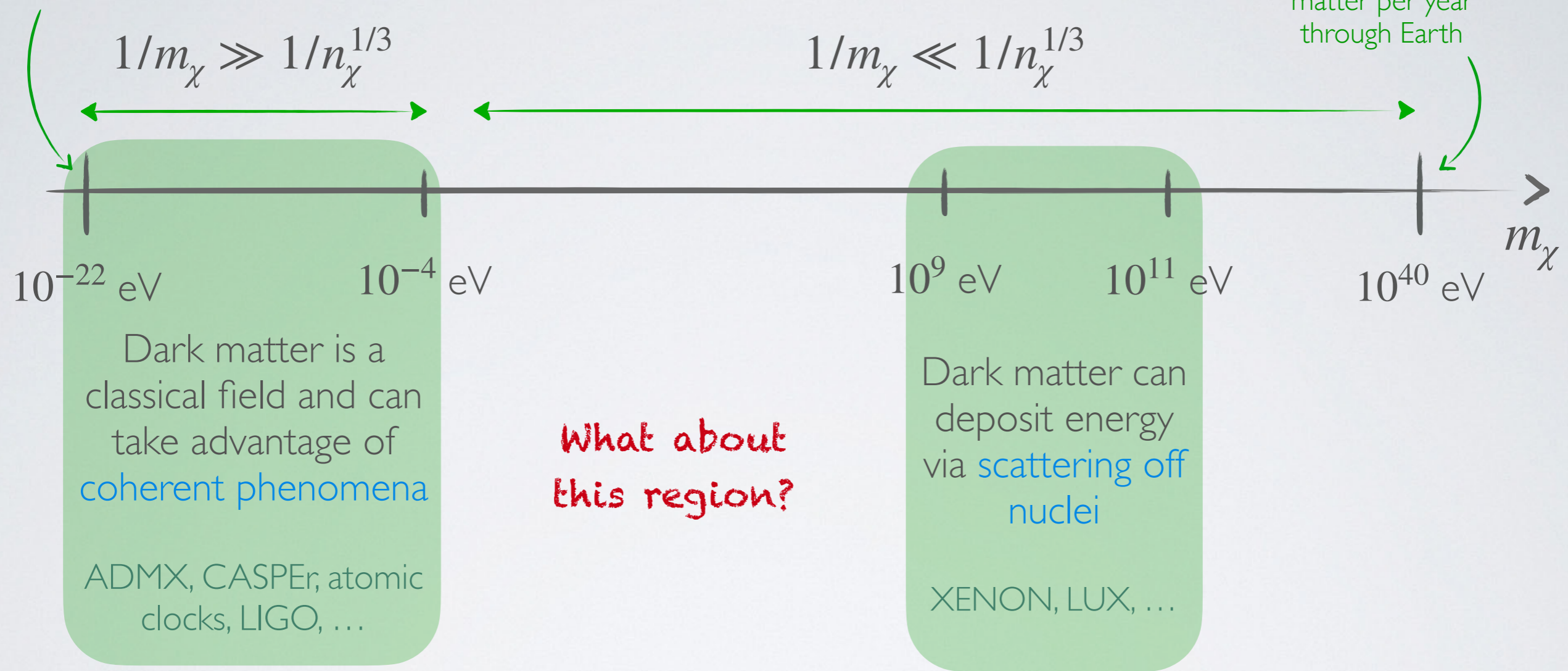


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- Dark matter is a particle but too light for elastic nuclear recoil
- Need new materials and/or observables

SUB-GEV DARK MATTER

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- For an **elastic scattering**, it must be

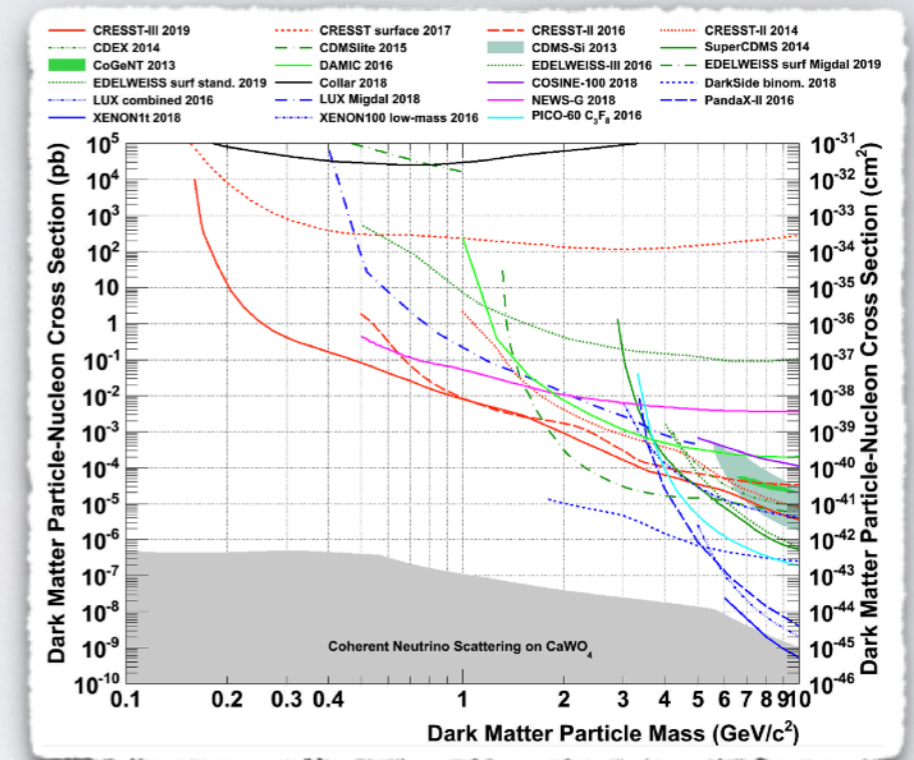
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[CRESST – PRD 2019, 1904.00498]

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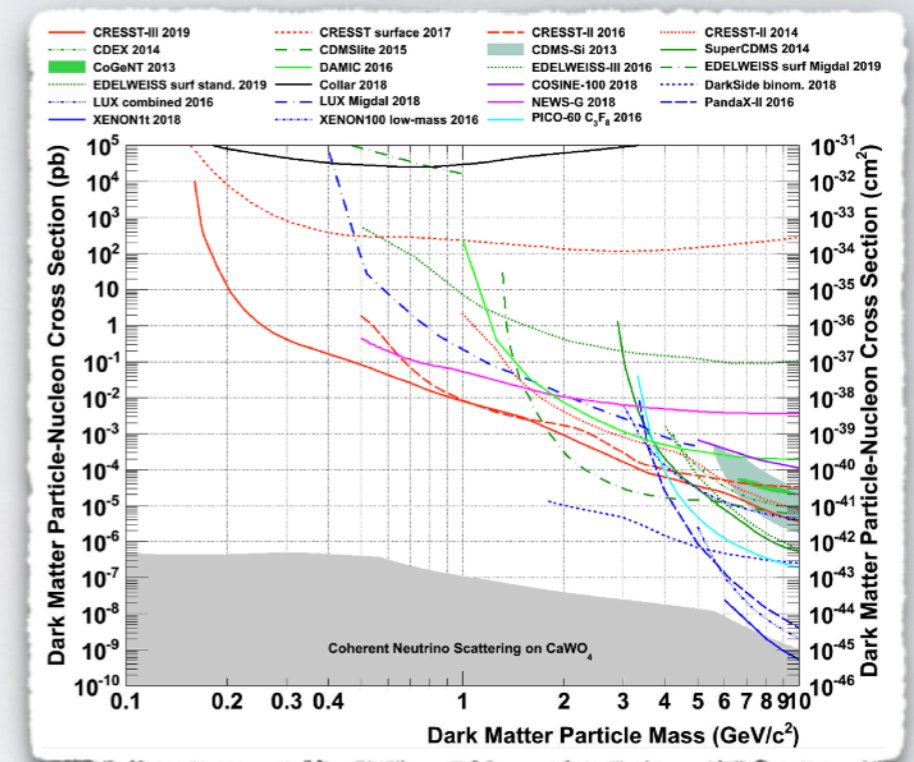
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- Two possibilities:

1. Look into lighter scattering targets
2. Look into inelastic processes

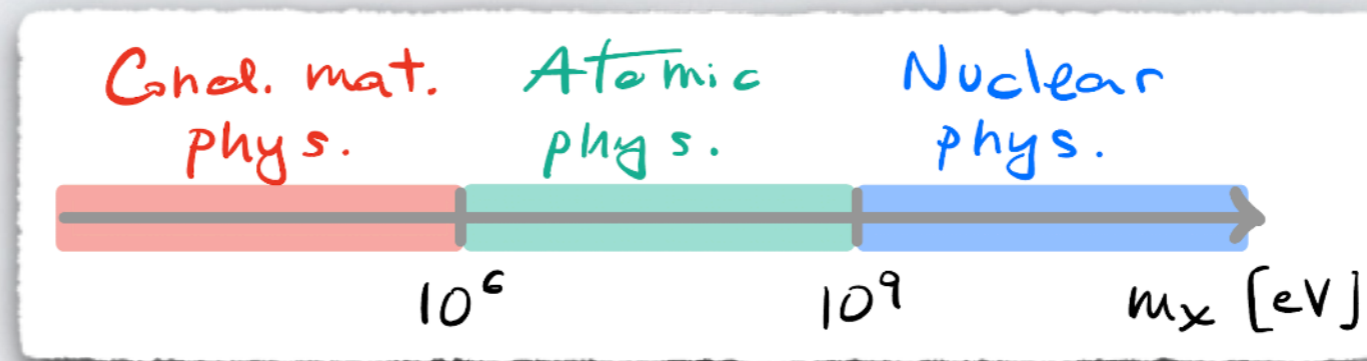


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NASTY STUFF

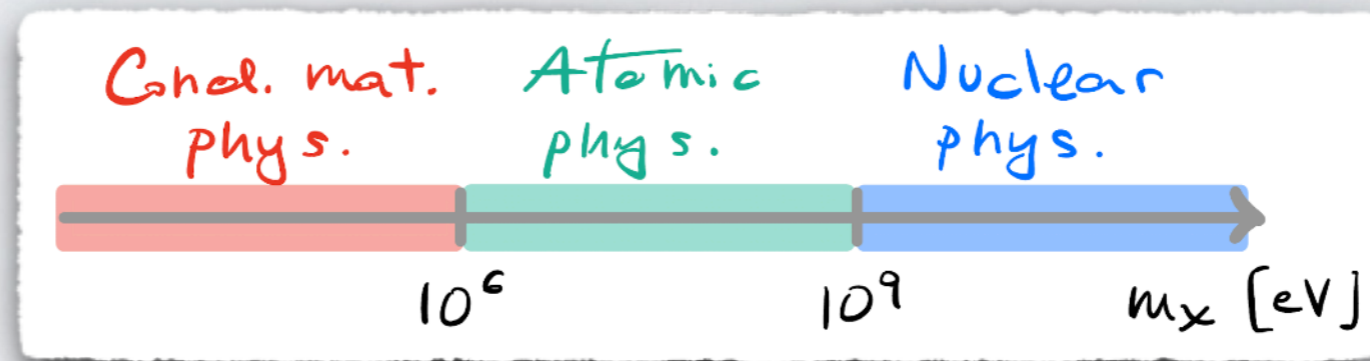
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- For sub-GeV dark matter one needs to delve into the condensed matter world

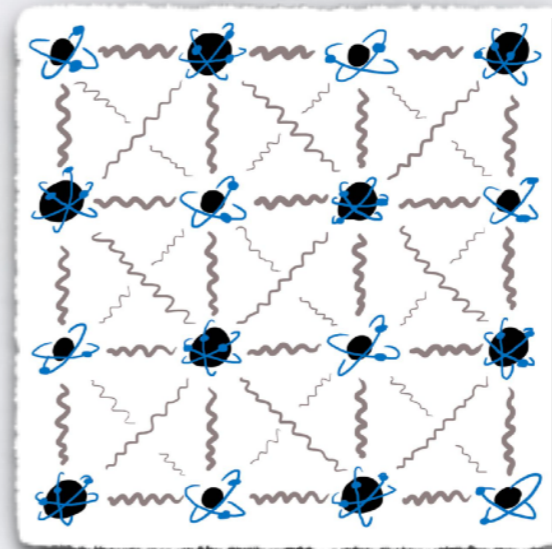


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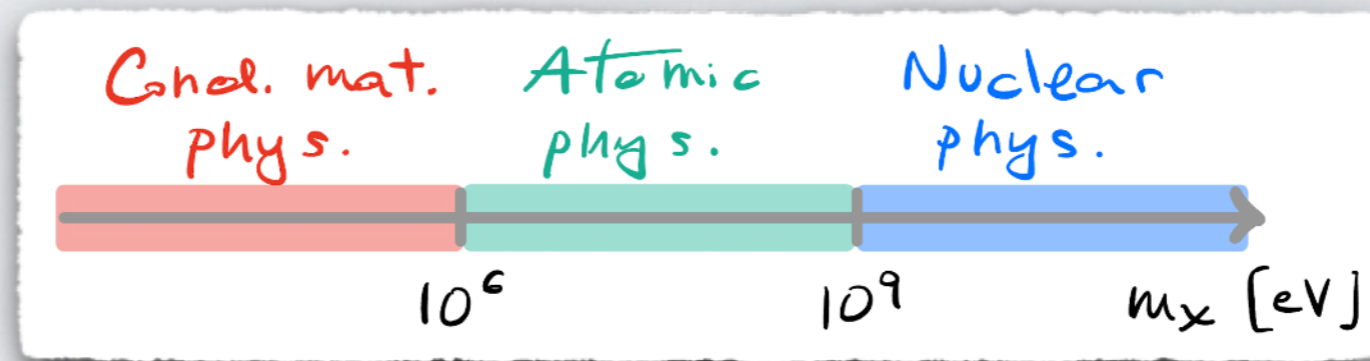


- Must **account for the complicated many-body physics** (correlations, strong coupling, ...)

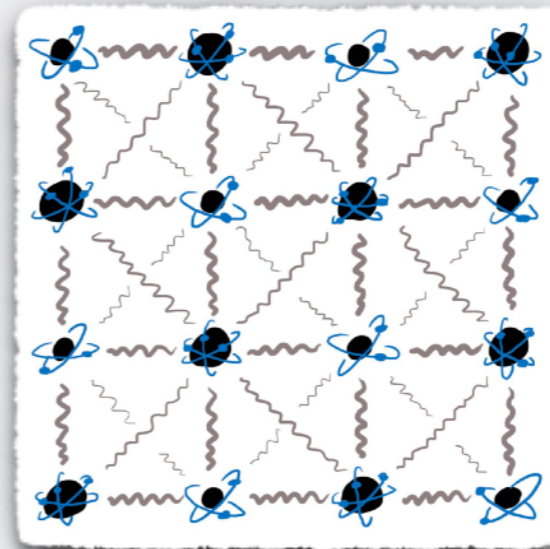


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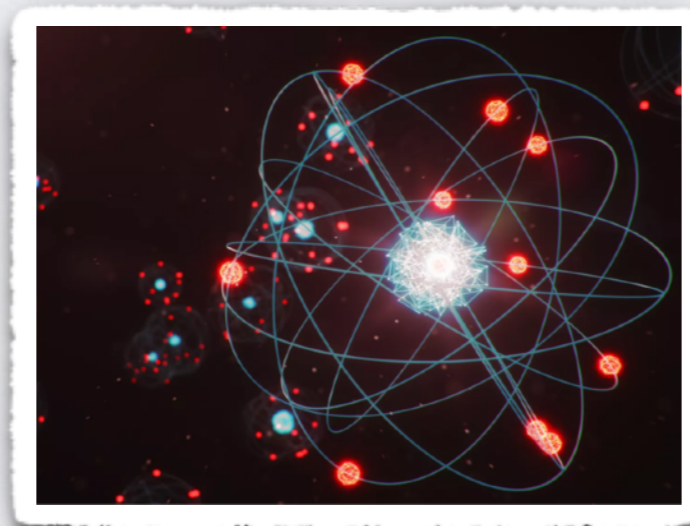


- Must **account for the complicated many-body physics** (correlations, strong coupling, ...)



- **Need to find theoretical tools** that allow to solve or bypass these problems (measured correlation functions, EFTs, ...)

Down to the MeV Migdal effect in semiconductors



MIGDAL EFFECT

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- For sub-GeV dark matter nuclear recoil signals become challenging
→ sensitivity can be lowered by **looking for inelastic processes**

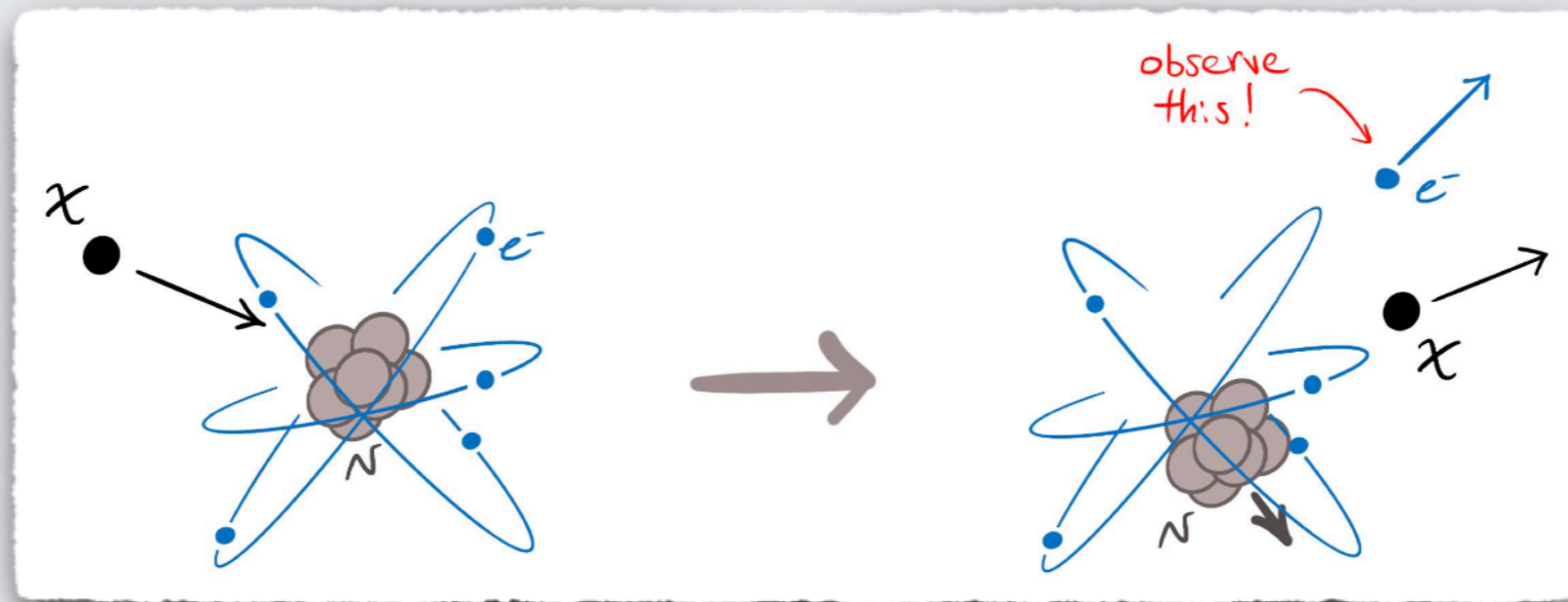
[e.g., Essig, Mardon, Volansky – PRD 2012, 1108.5383; Kouvaris, Pradler – PRL 2017, 1607.01789]

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- Hadrophilic dark matter on free atoms → **Migdal effect**

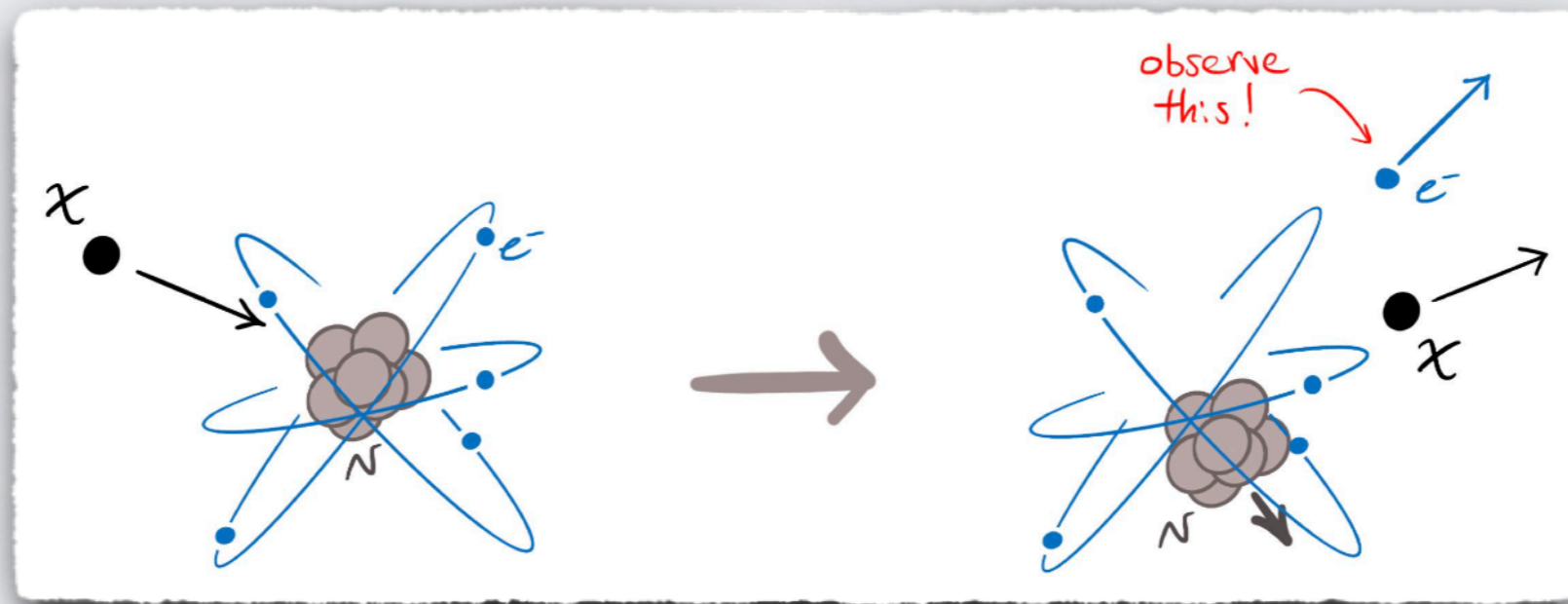


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- Less likely... but lower threshold! → sensitivity **down to**

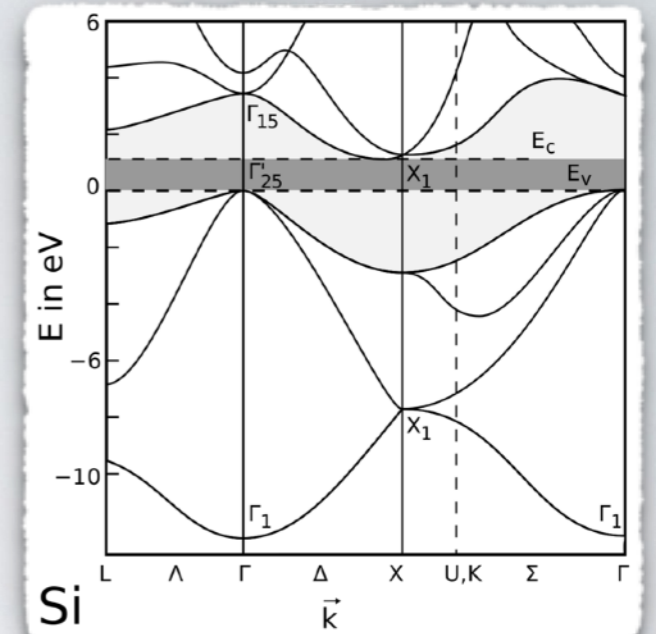
@(100 MeV) masses

[e.g., Ibe, Nakano, Shoji, Suzuki – JHEP 2018, 1707.07258; DarkSide – 2207.11967]

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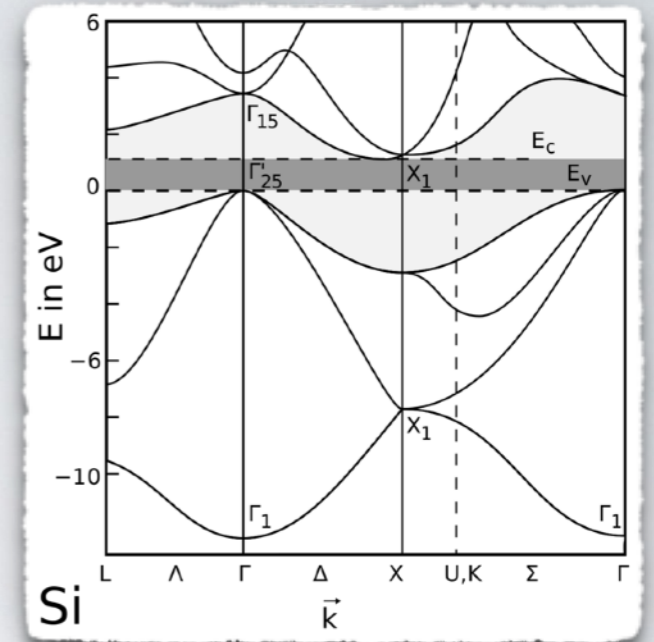
MIGDAL EFFECT

- Semiconductors (Si, Ge, ...) have small $\mathcal{O}(\text{eV})$ bandgaps \rightarrow Migdal effect should allow to probe down to $\mathcal{O}(\text{MeV})$ masses

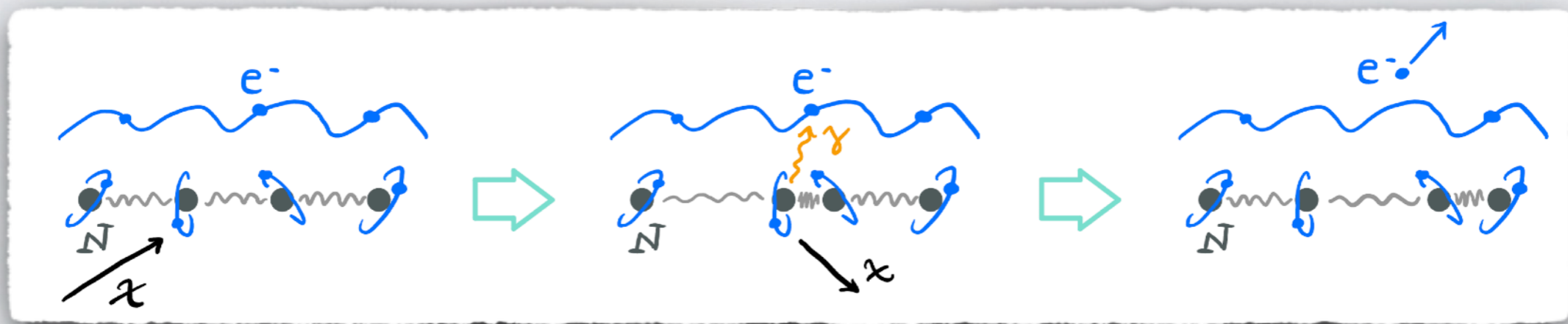


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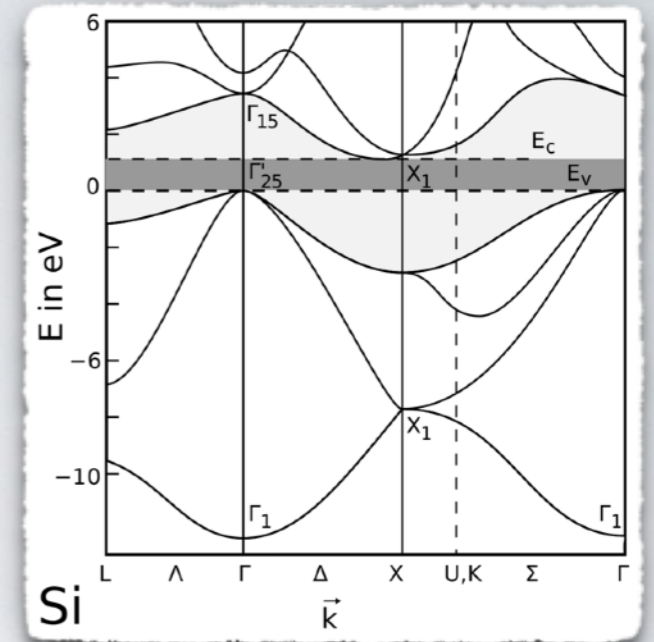


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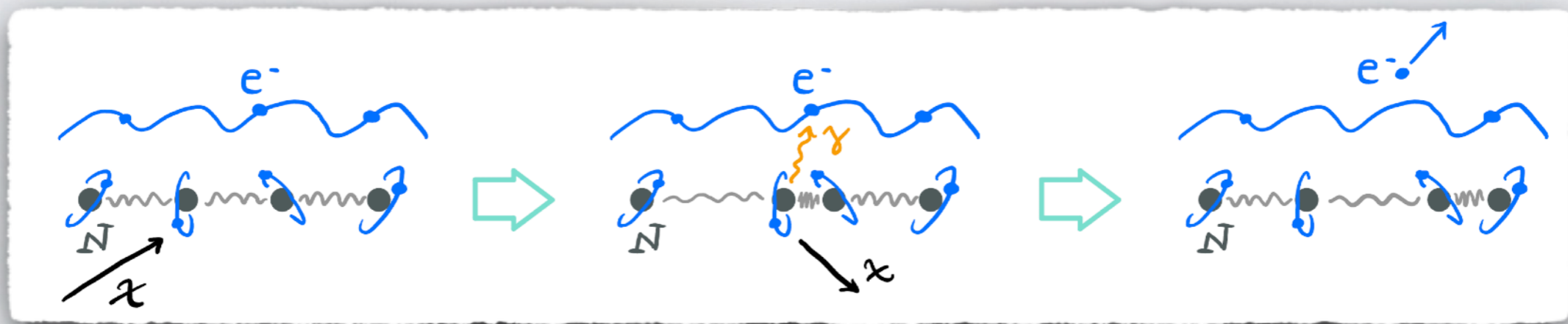


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- How to describe nucleus-nucleus and nucleus-electron interactions in a strongly correlated system?

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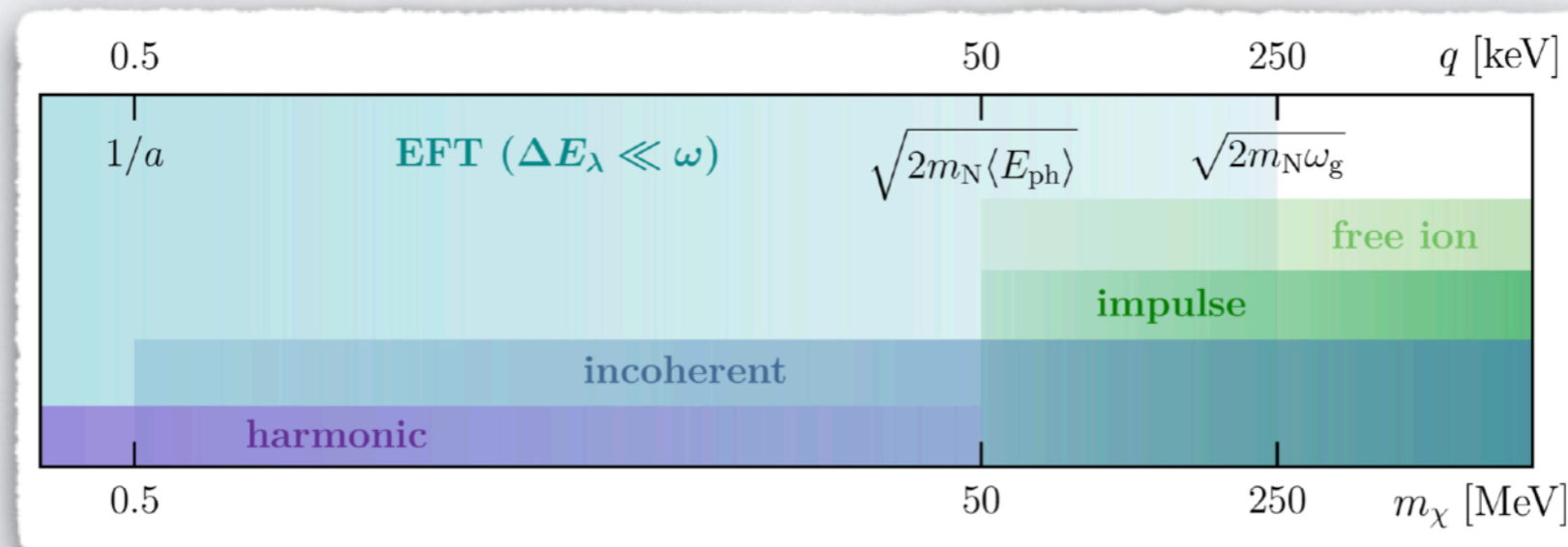
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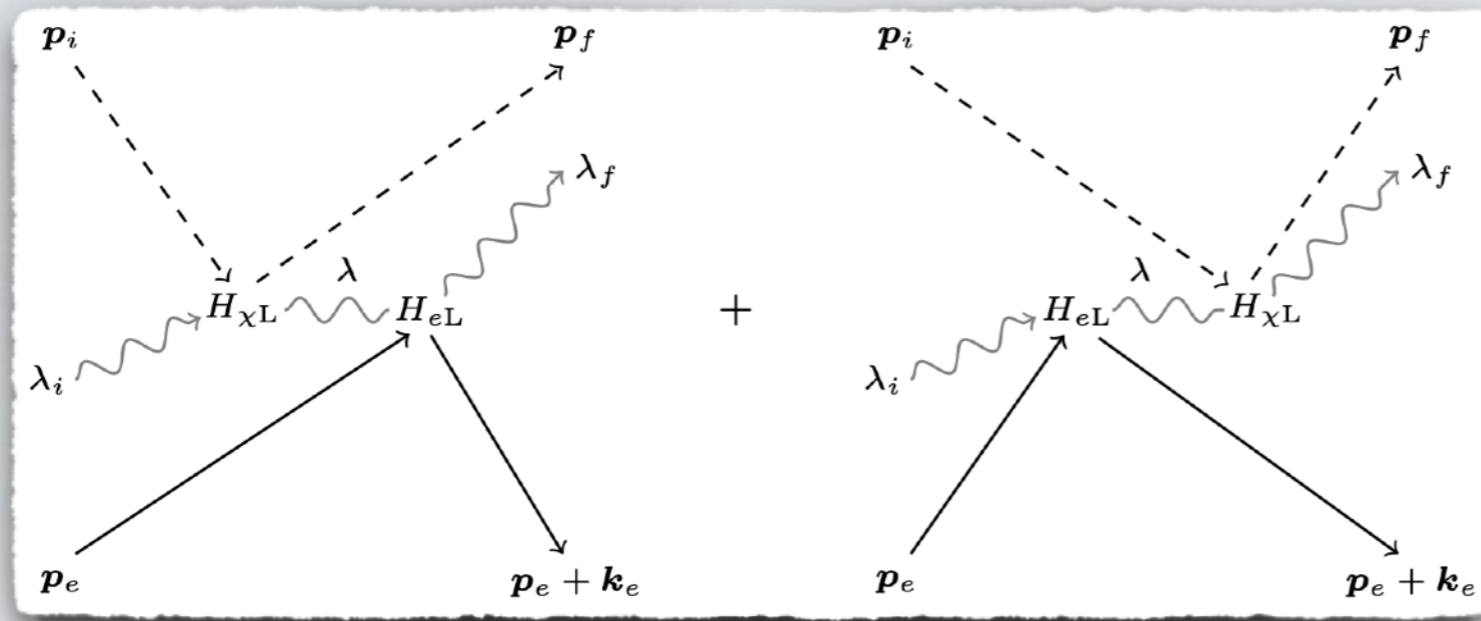
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EFT

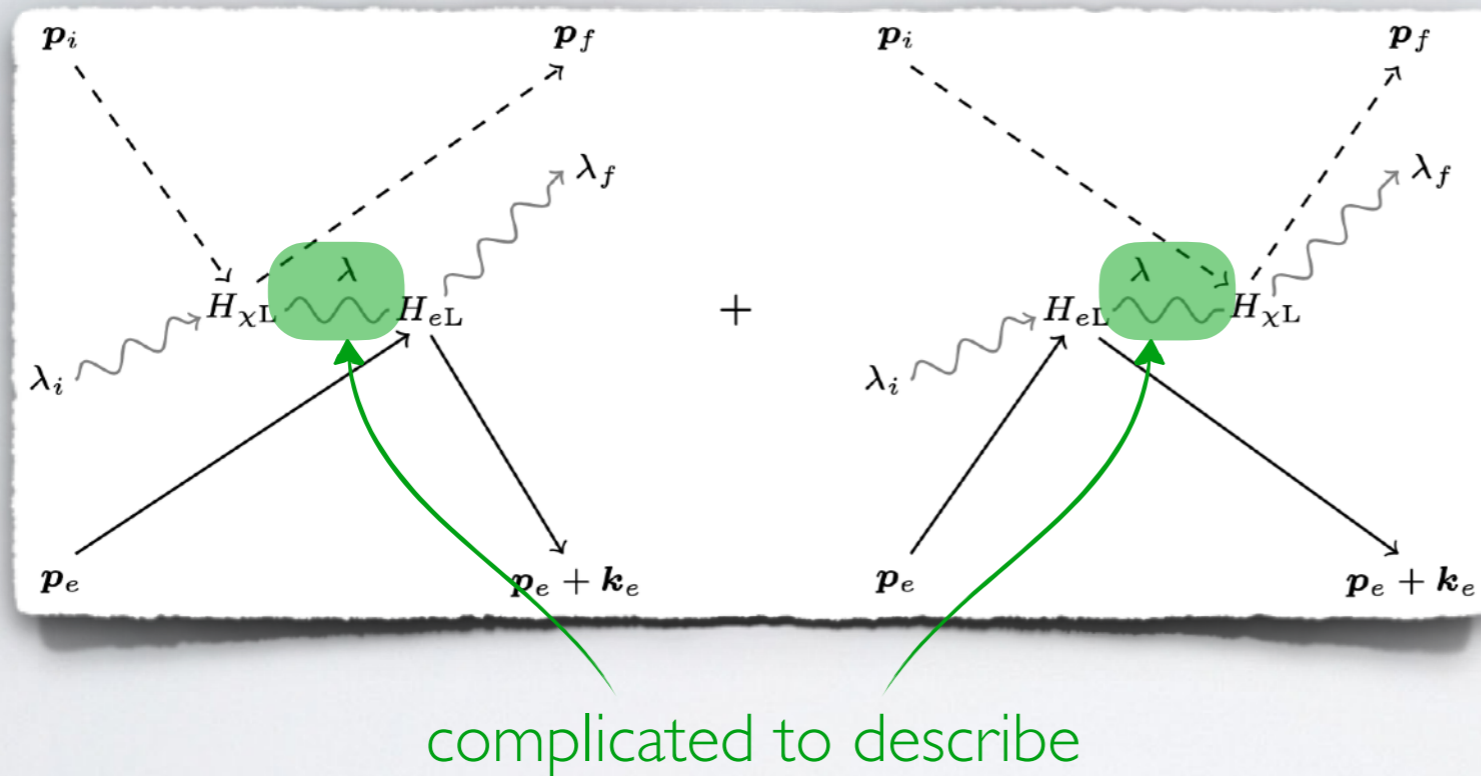
EFT

- Migdal effect in old-fashioned perturbation theory



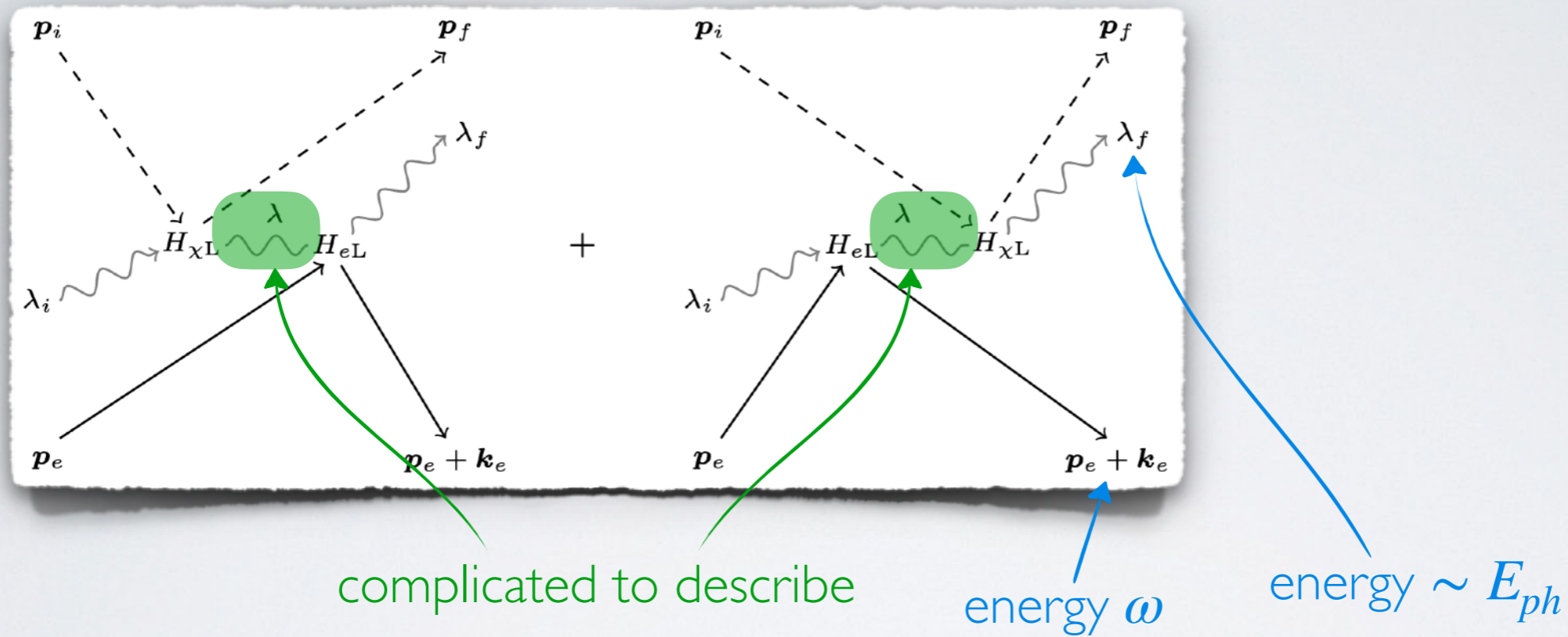
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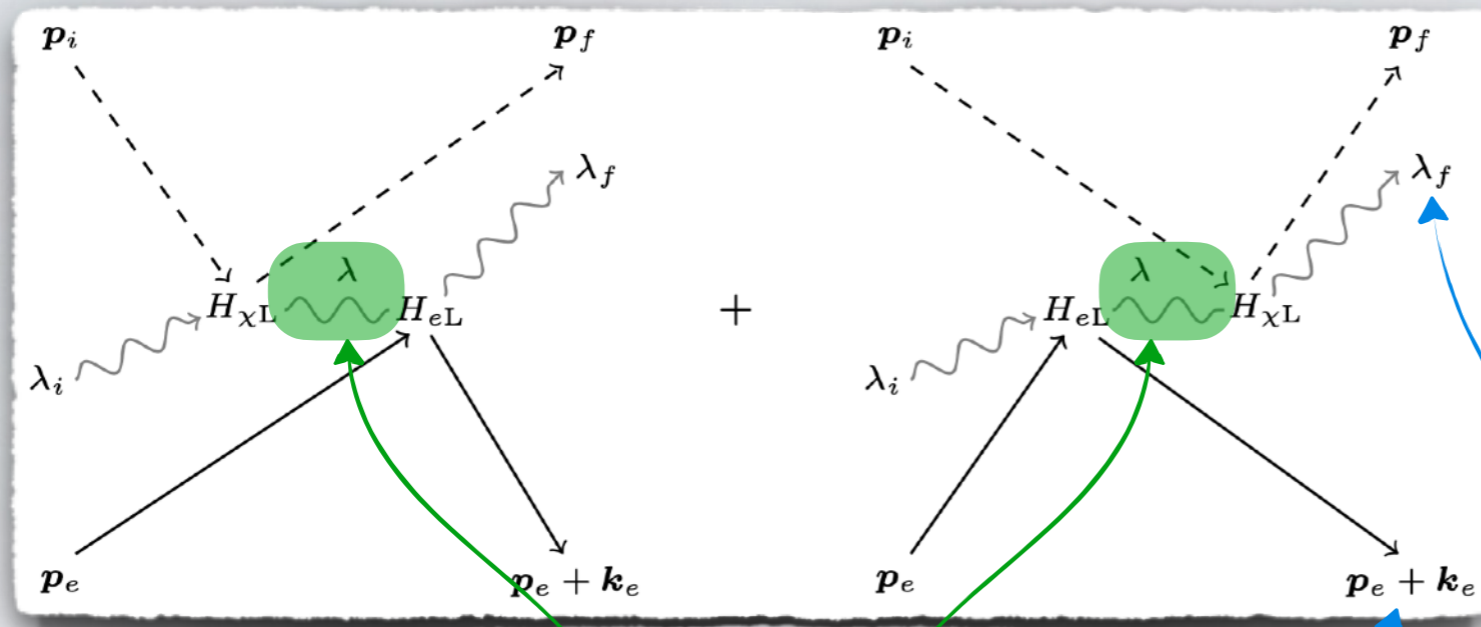
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complicated to describe

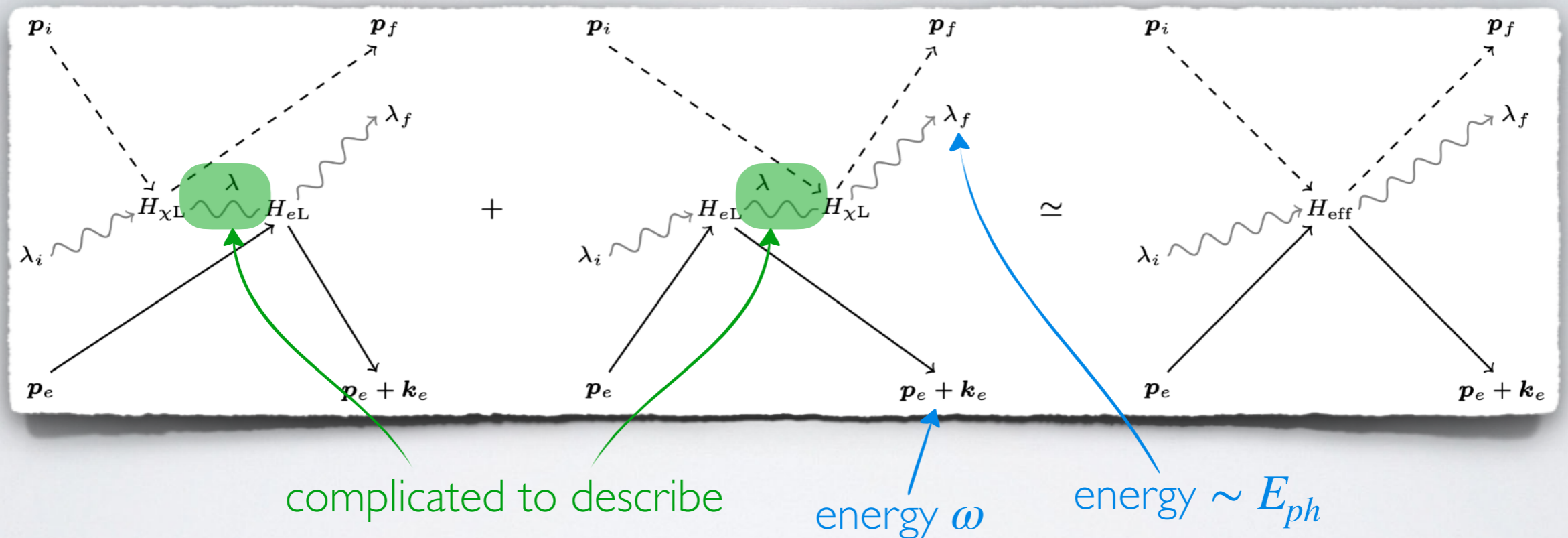
energy ω

energy $\sim E_{ph}$

- Separation of scales ($\omega \sim \text{eV} \gg E_{ph} \sim 10 \text{ meV}$) allows to integrate out the intermediate lattice mode

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$$H_{eff} = \frac{1}{m_N \omega^2} \vec{\nabla} H_{\chi L} \cdot \vec{\nabla} H_{eL} + \mathcal{O}\left(\frac{1}{\omega^3}\right)$$

[Berghaus, **AE**, Essig, Sholapurkar – JHEP 2020, 2210.06490]

MIGDAL RATE

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- Now simple to determine the **rate for Migdal emission**

$$\frac{d^2\Gamma}{d\omega dE_{ph}} \propto \sum_{\mathbf{k}} \sum_{\mathbf{K}, \mathbf{Q}} \frac{\mathbf{q} \cdot (\mathbf{k} + \mathbf{K}) \mathbf{q} \cdot (\mathbf{k} + \mathbf{K})}{|\mathbf{k} + \mathbf{K}| |\mathbf{k} + \mathbf{Q}|} \text{Im}(-\epsilon_{\mathbf{KQ}}^{-1}(\mathbf{k}, \omega)) S(\mathbf{q} - \mathbf{k} - \mathbf{K}, E_{ph})$$

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[e.g., Knapen, Kozaczuk, Lin — PRD 2021, 2101.08275; Hochberg et al. — PRL 2021, 2101.08263; Knapen, Kozaczuk, Lin — PRD 2022, 2104.12786]

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- No data yet** in the range of interest ($q \simeq 10 \text{ keV} - 100 \text{ keV}$)

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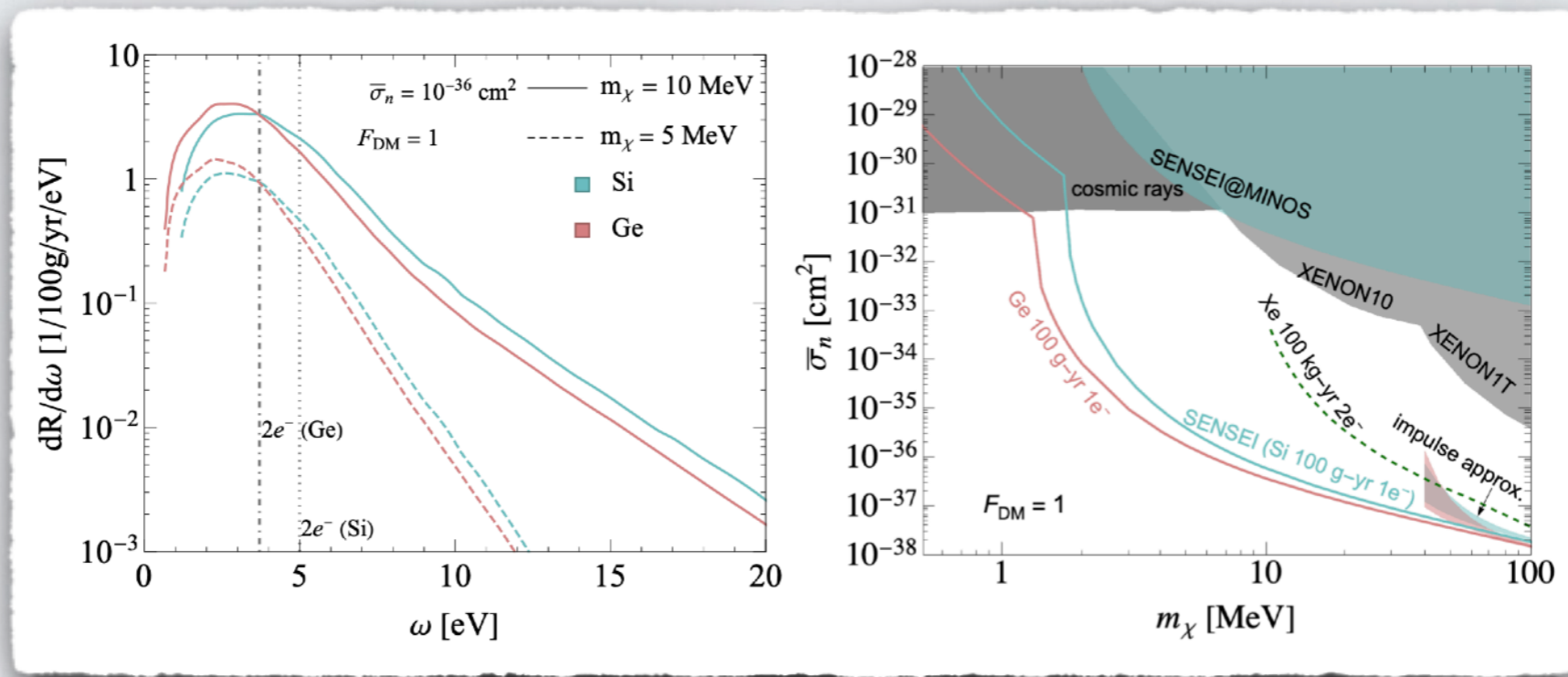
- If **only** interested in electron energy, the rate is **independent** on the details of the crystal lattice

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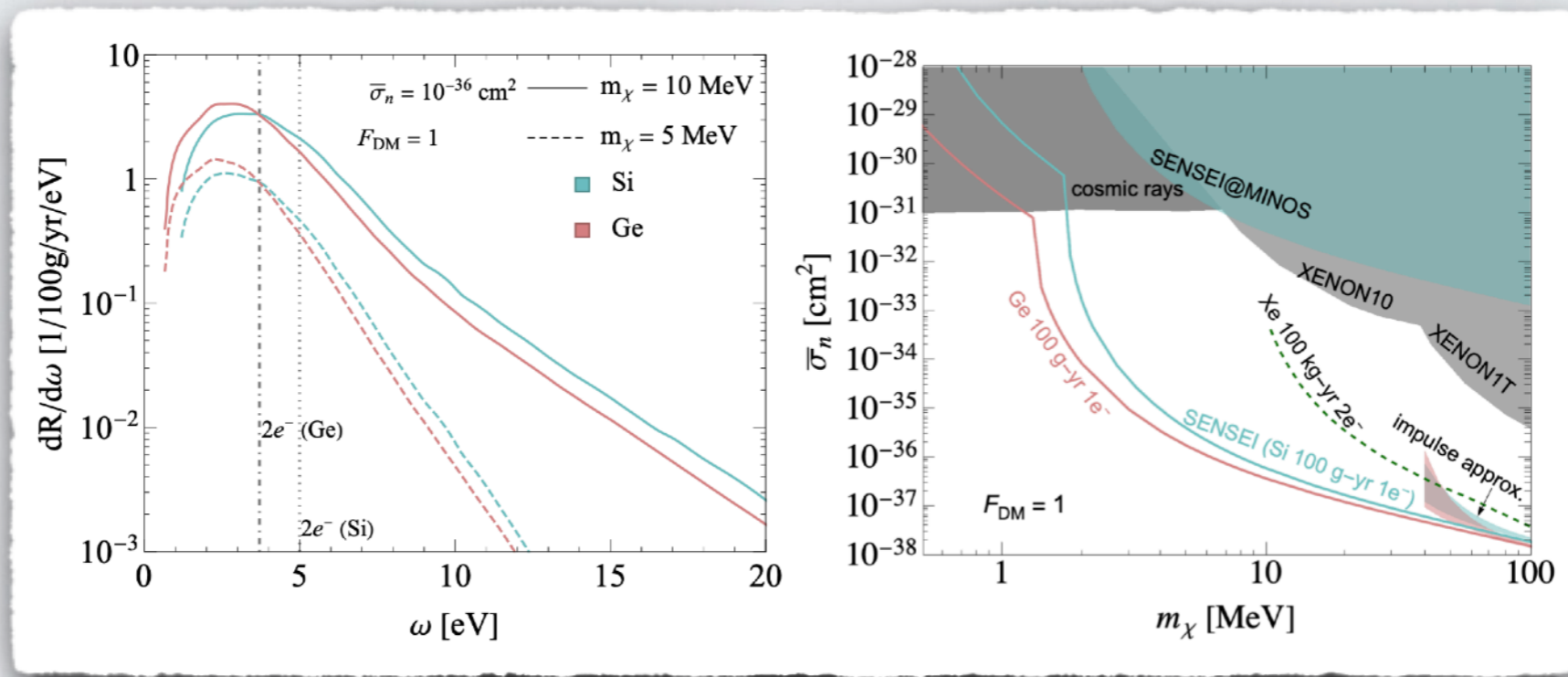


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- Description of Migdal effect in semiconductor extended to all masses

EXPERIMENTAL PUZZLE

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- Migdal effect recently measured in liquid Xenon

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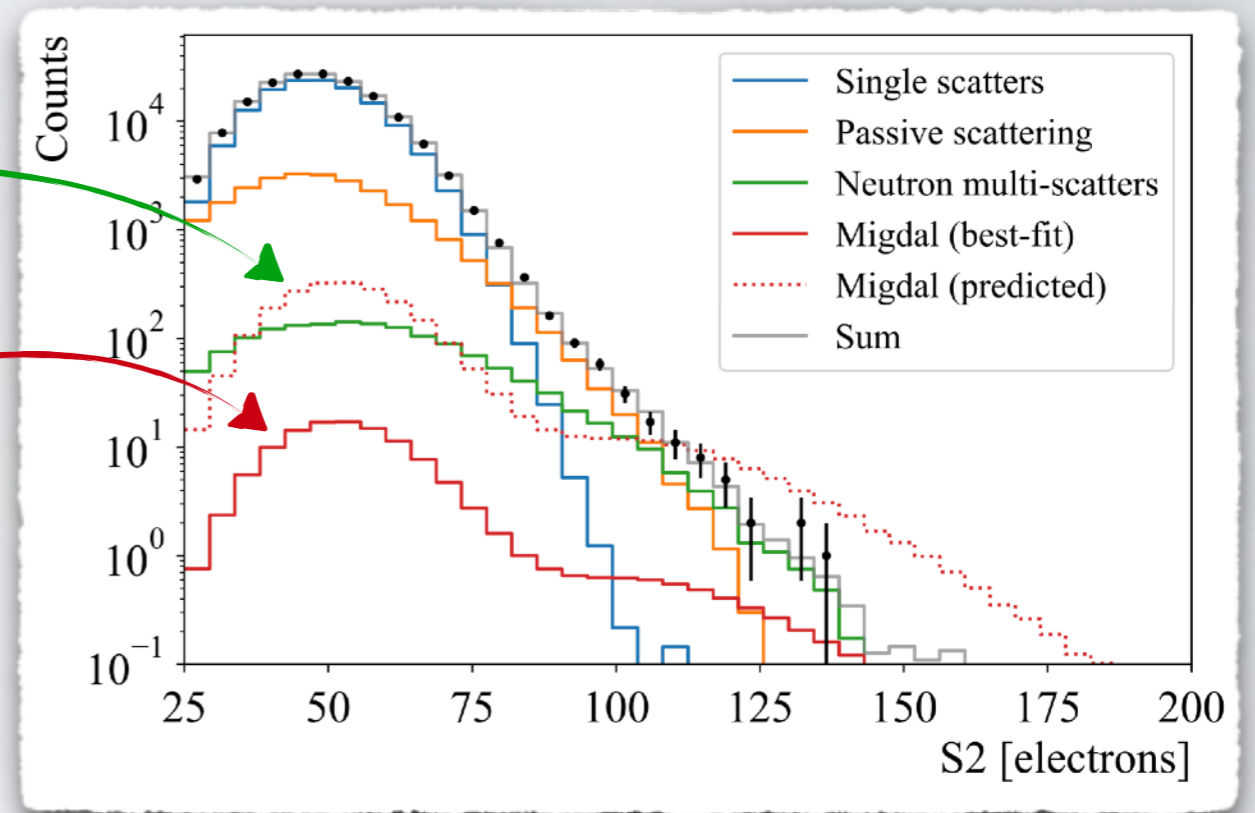
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theory

experiment



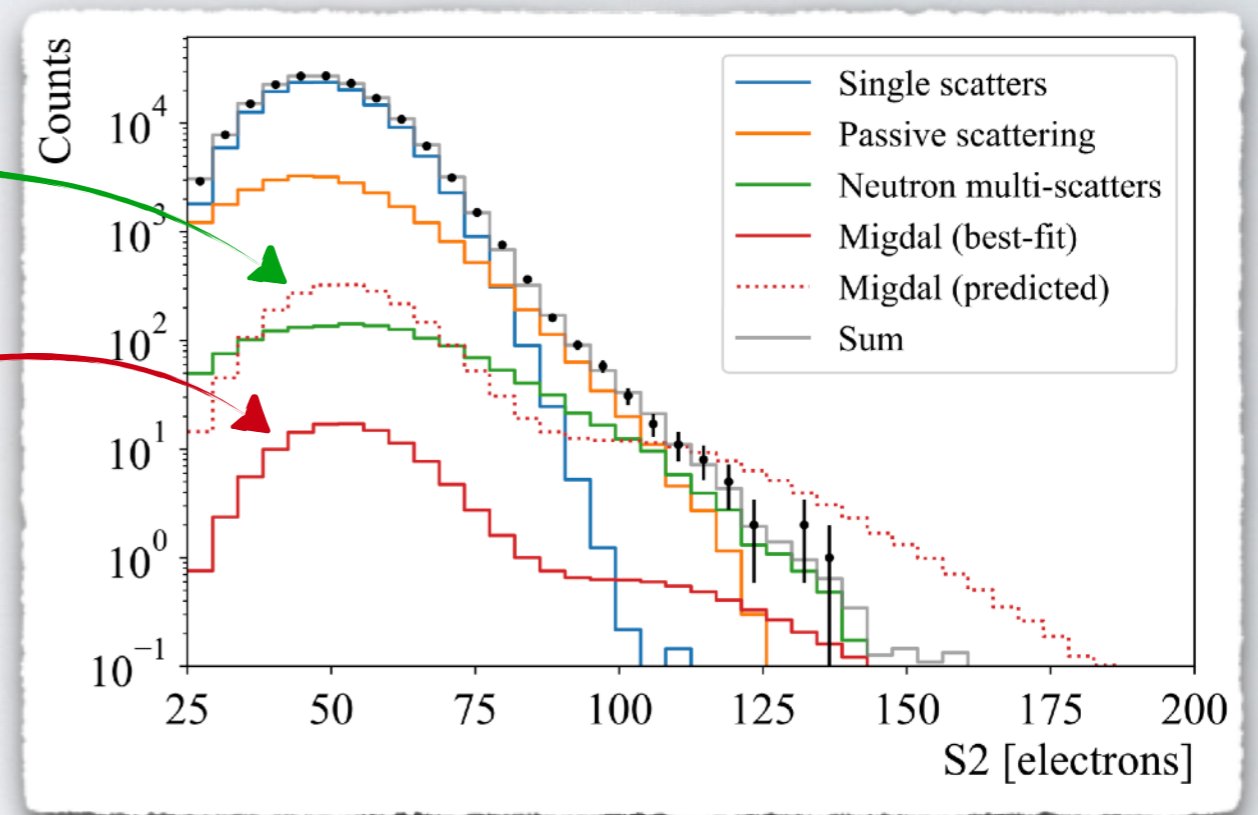
[Xu et al. - 2307.12952]

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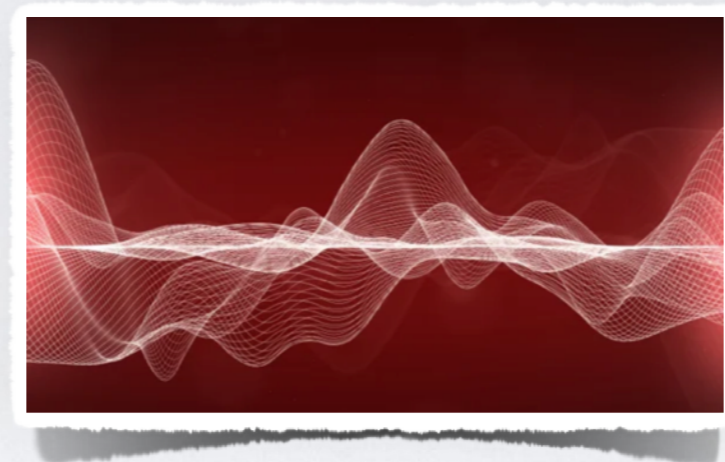
experiment



[Xu et al. - 2307.12952]

- Theory assumes **free atoms** → could the difference be explained by **condensed matter effects?** [work in progress w/ G. Grilli di Cortona]

Down to the keV collective excitations



COLLECTIVE EXCITATIONS

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- For $m_\chi \lesssim \mathcal{O}(\text{MeV})$, dark matter scattering can transfer a momentum

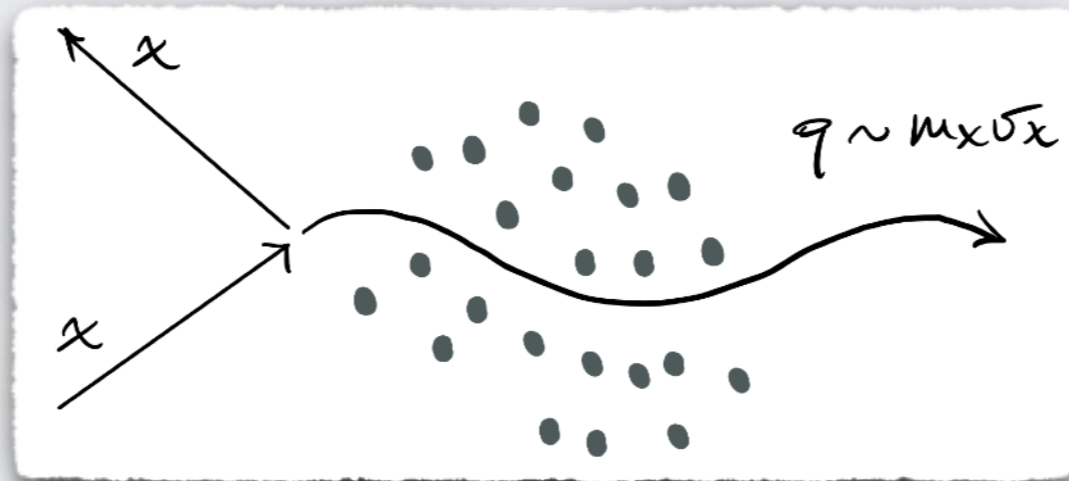
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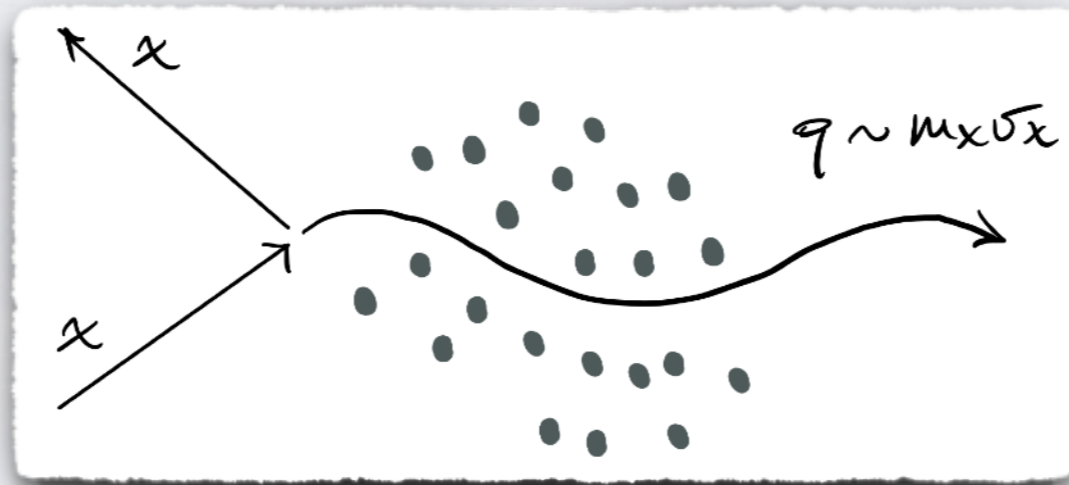


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- Typically, no more single particle final states \rightarrow signatures

involve **collective excitation**

[see e.g., Trickle et al. – JHEP 2020, 1910.08092; Griffin et al. – PRD 2020, 1910.10716; Coskuner et al. – PRD 2022, 2102.09567]

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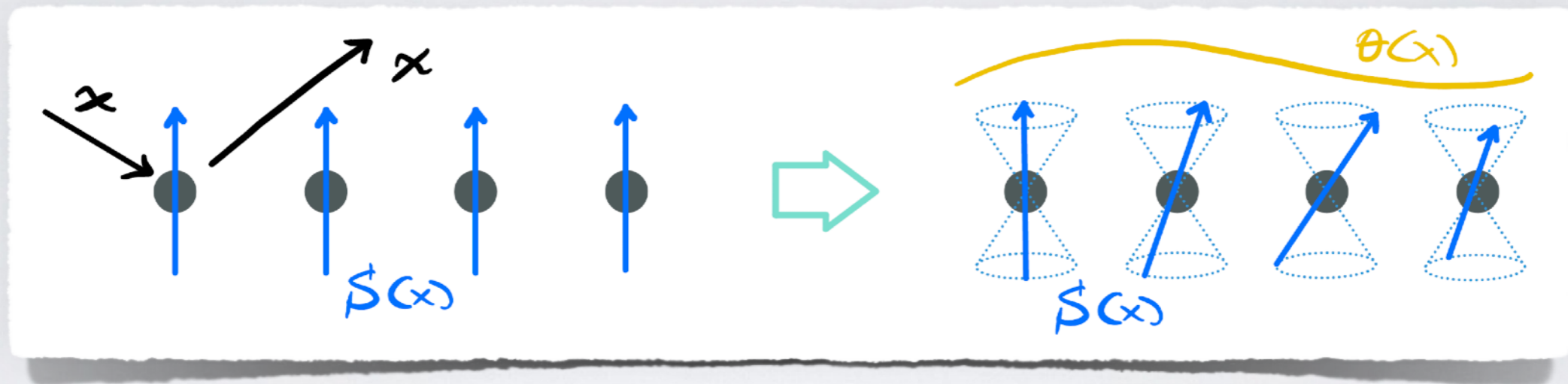
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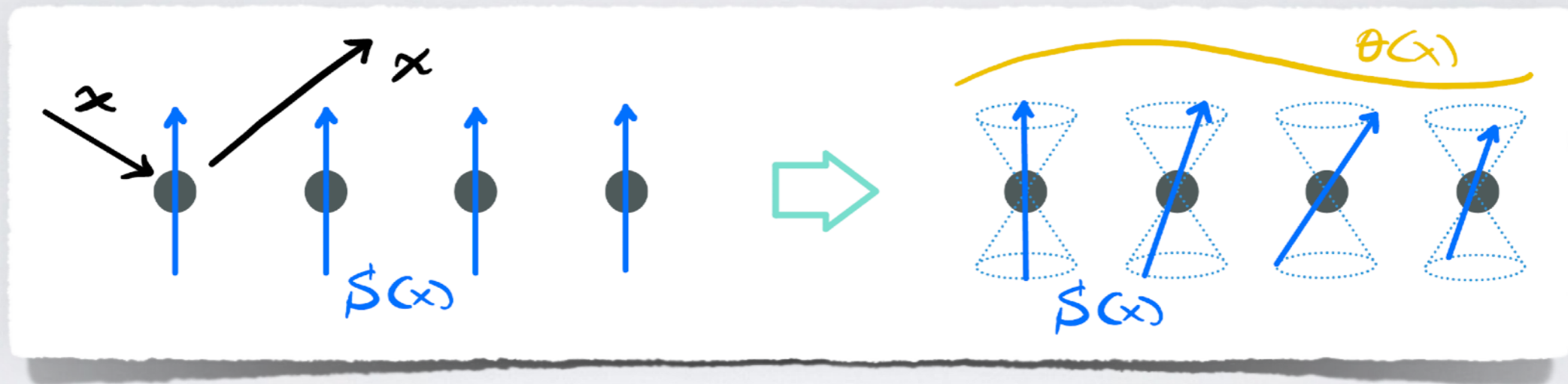


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- Ways to detect few magnons have been proposed and under work (TES, MKID, quantum sensors)

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FERROMAGNETS

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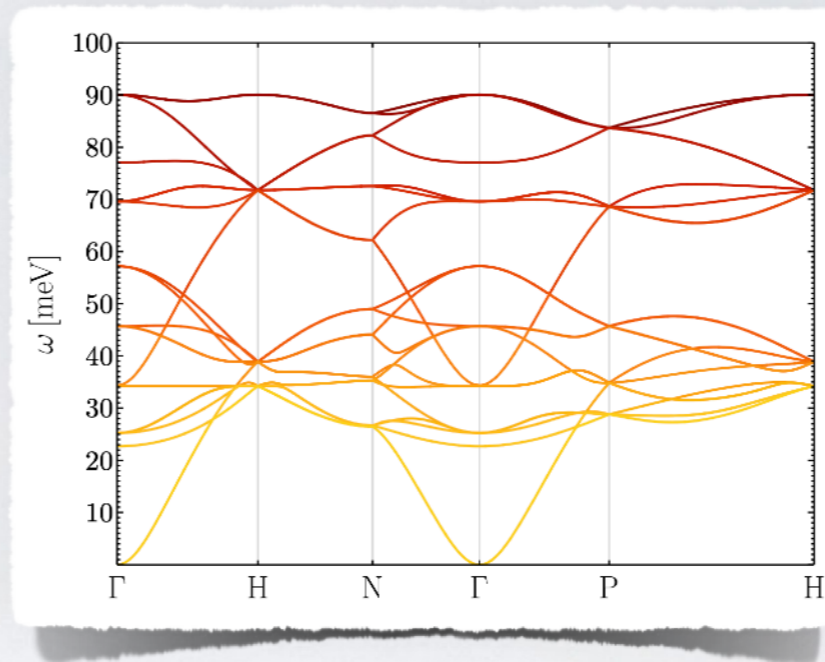
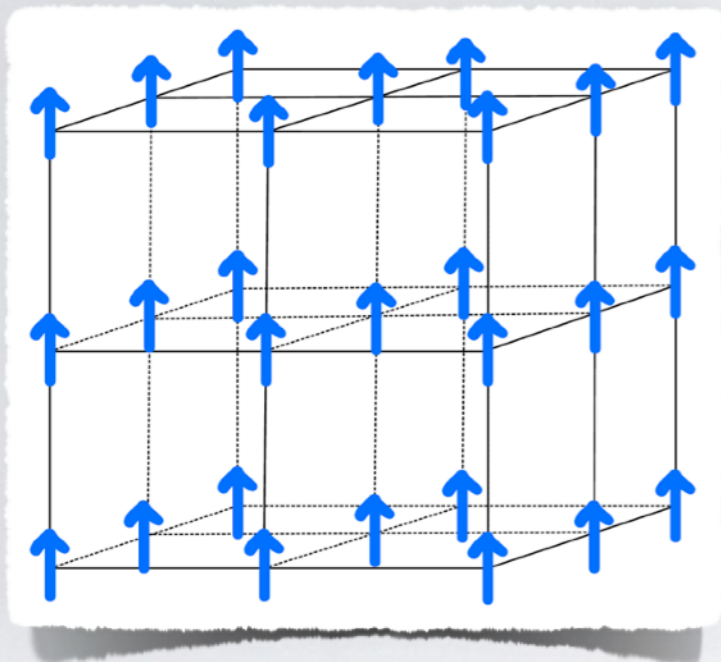
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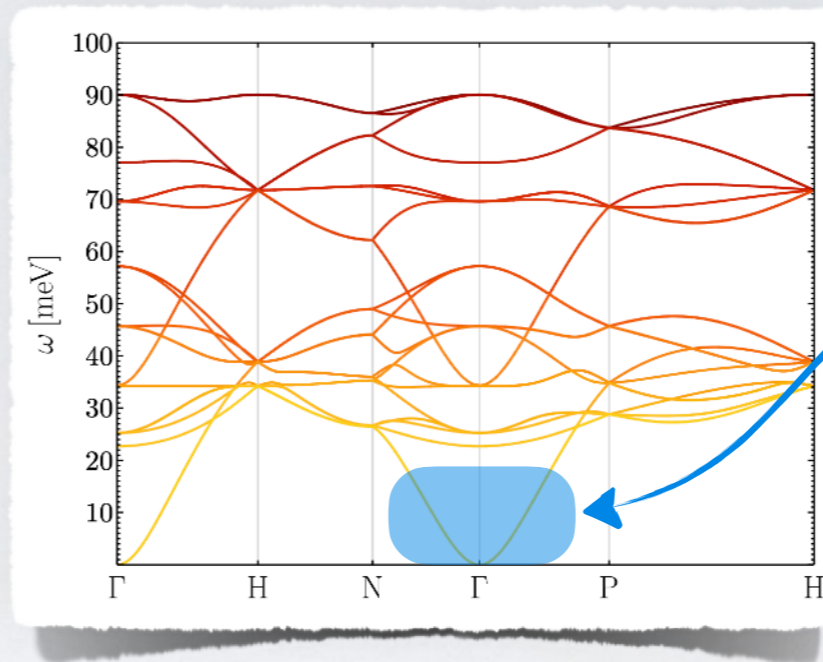
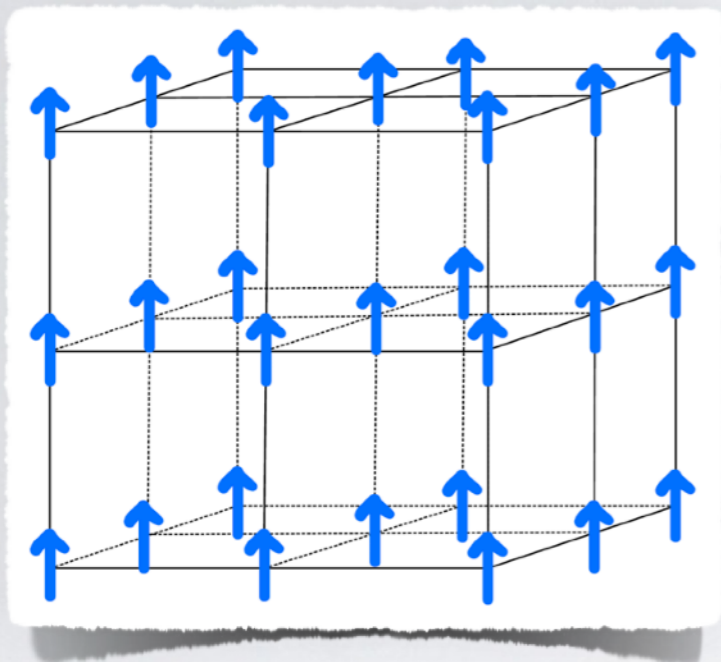
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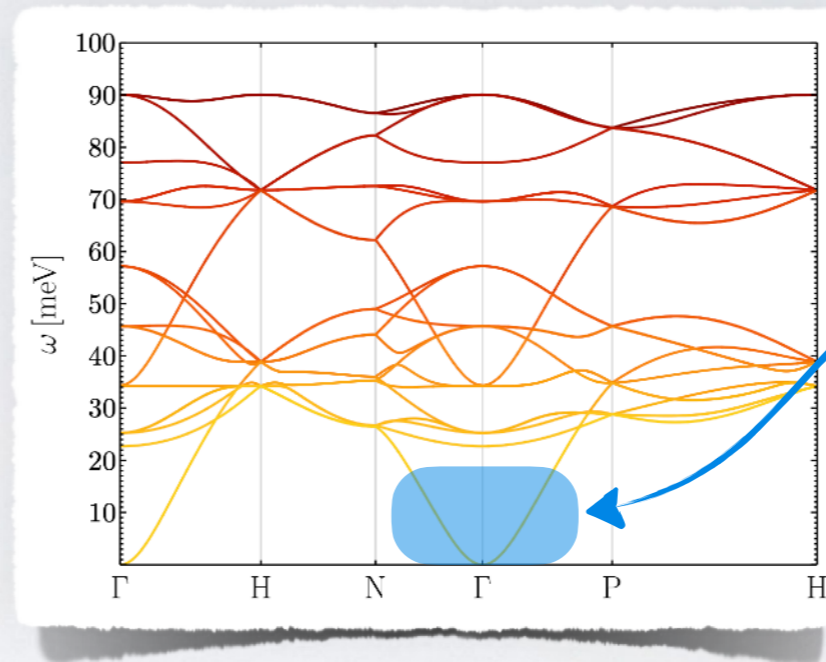
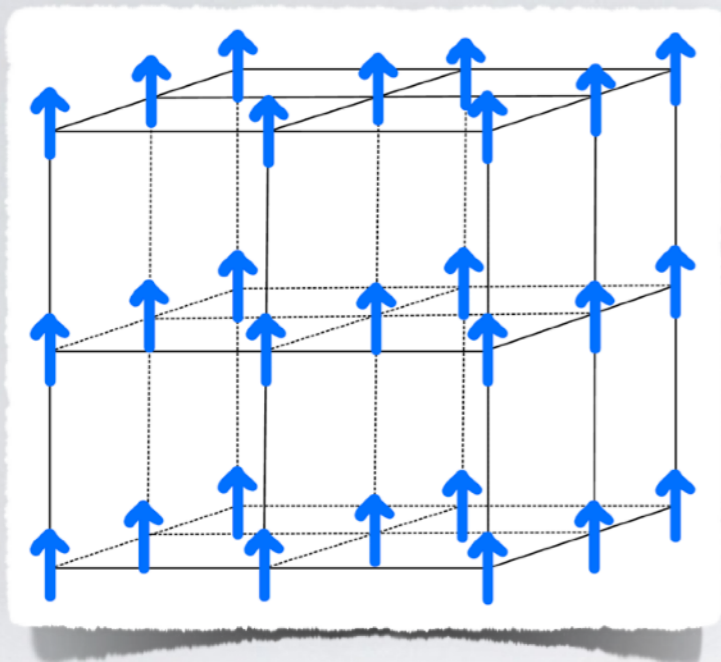


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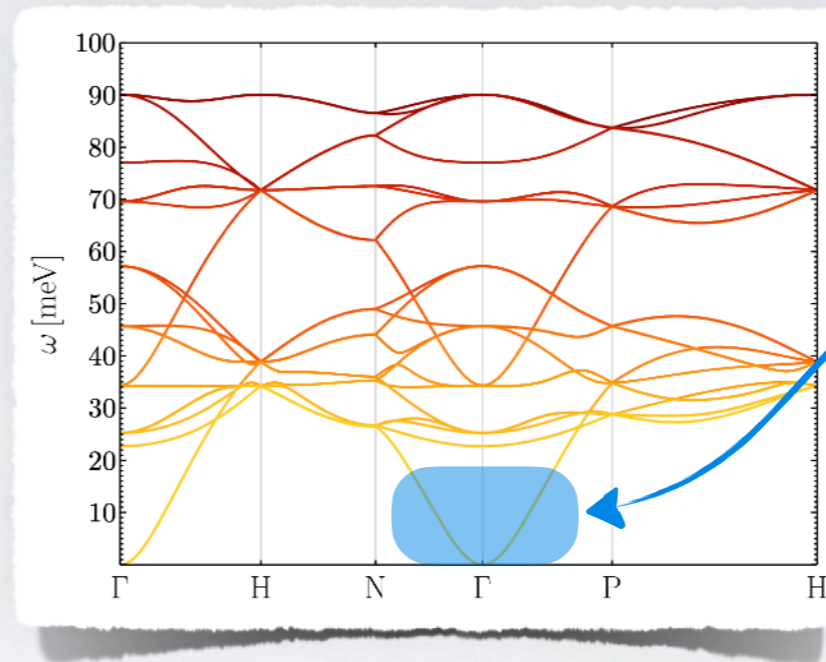
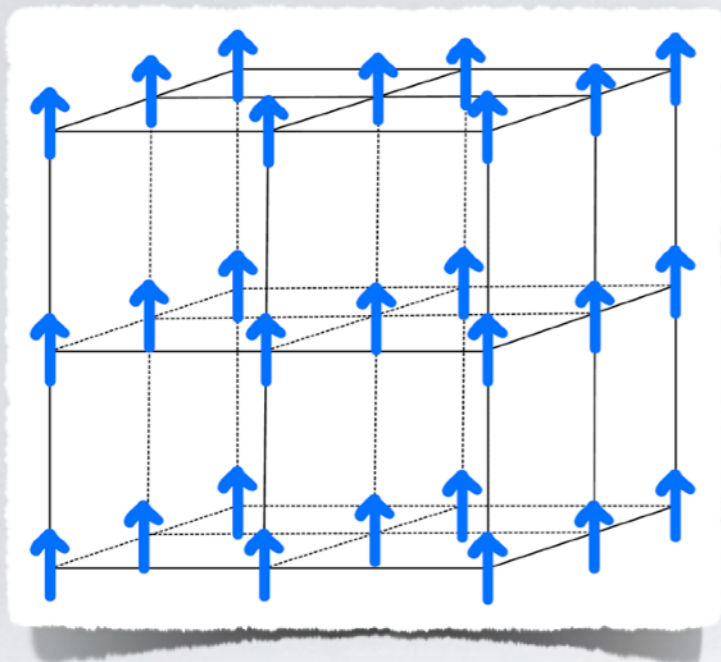
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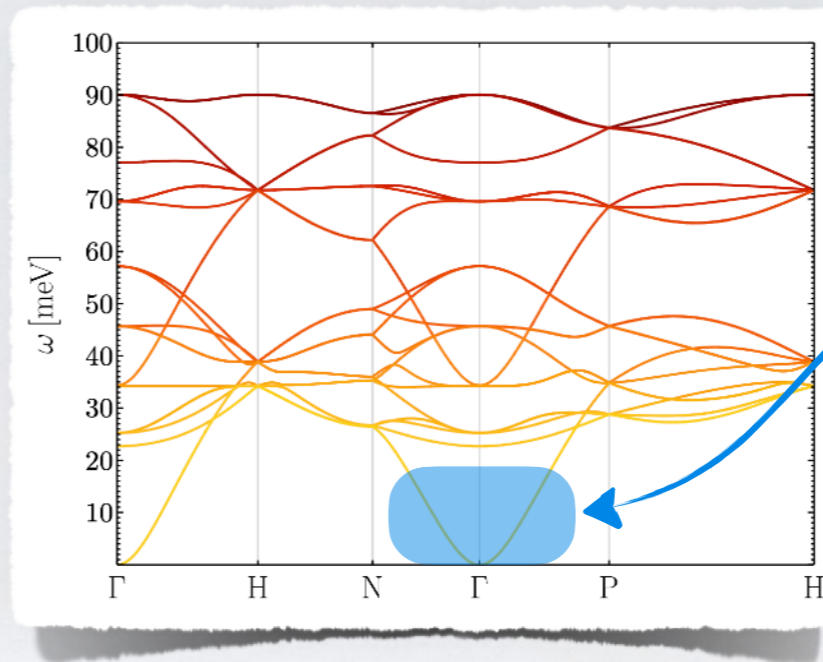
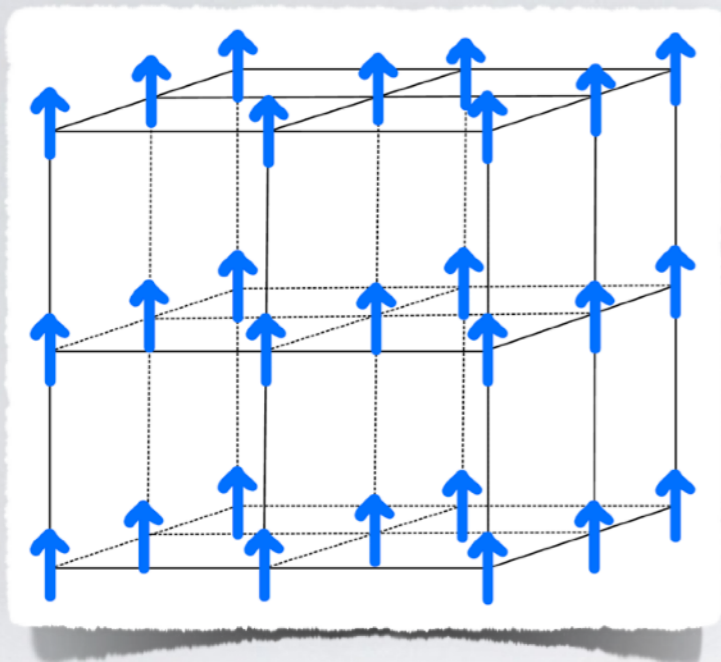
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FERROMAGNETS

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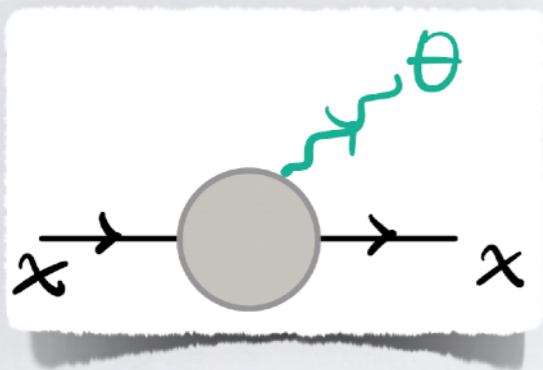
- Compute the magnon emission rate
- **Traditional approach:** quantize the Heisenberg model

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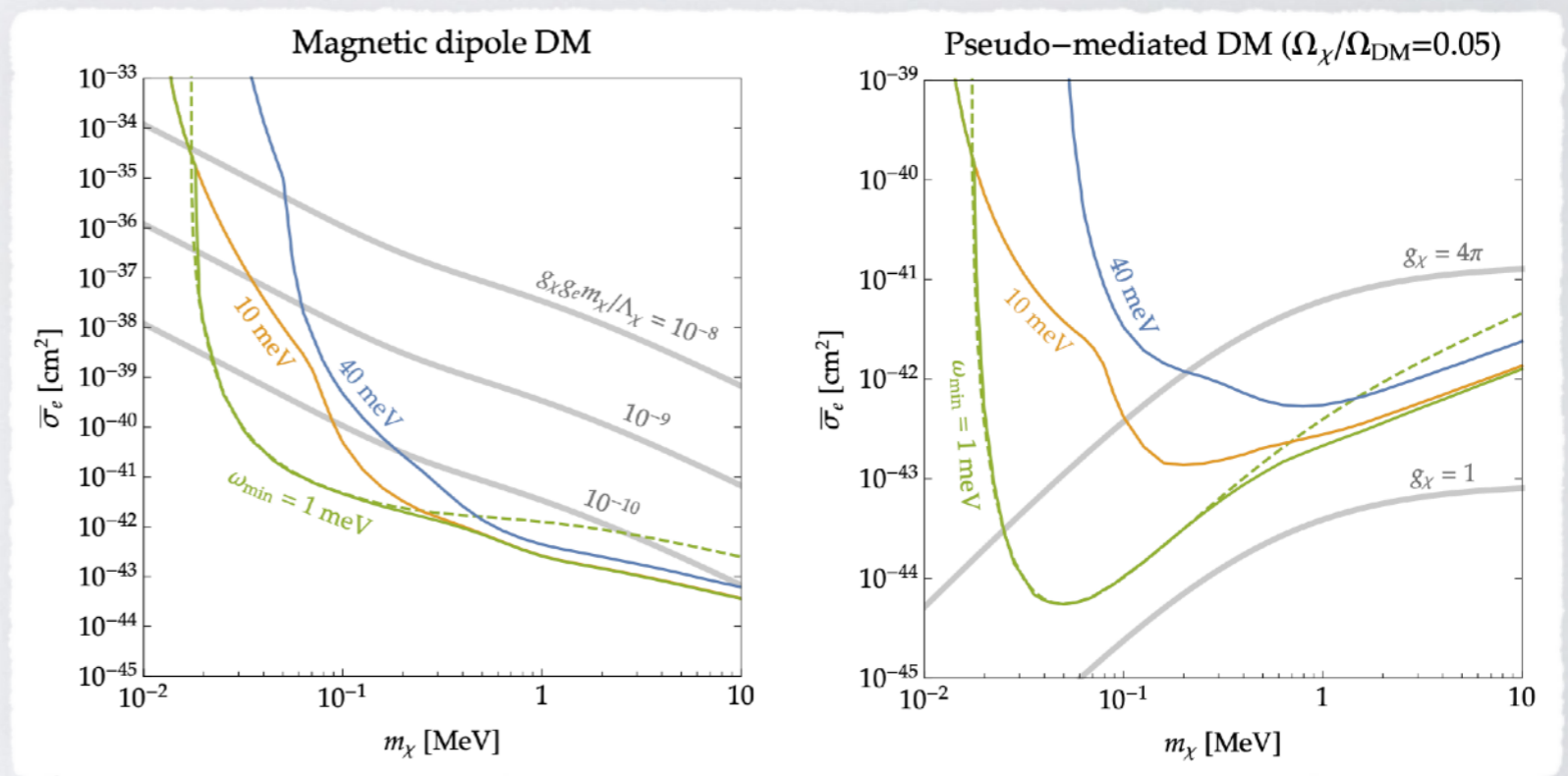
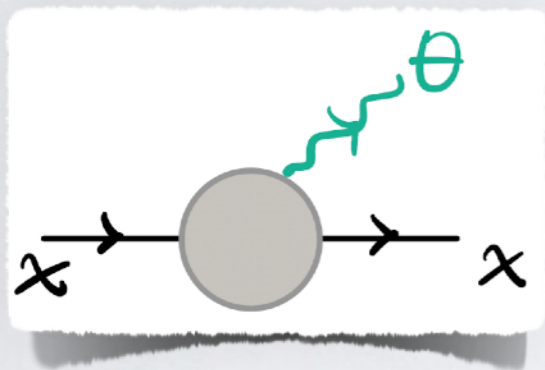
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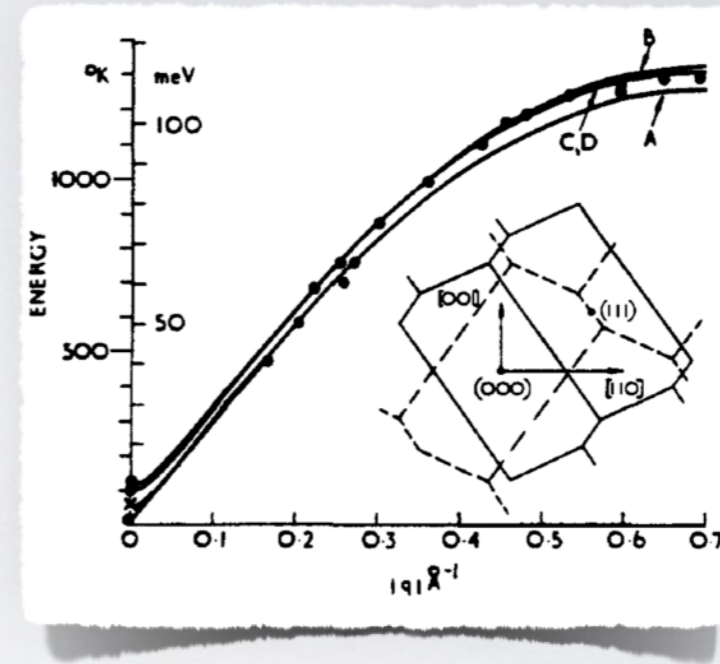
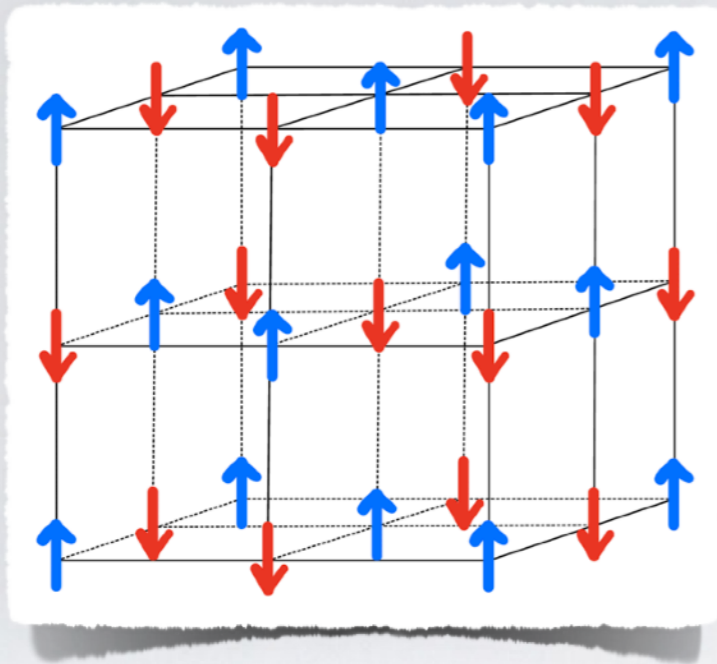
ANTI-FERROMAGNETS

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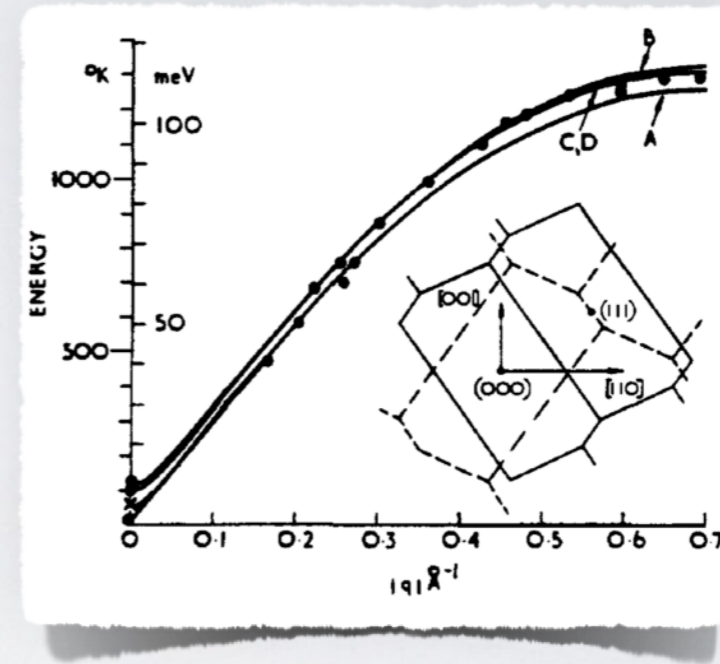
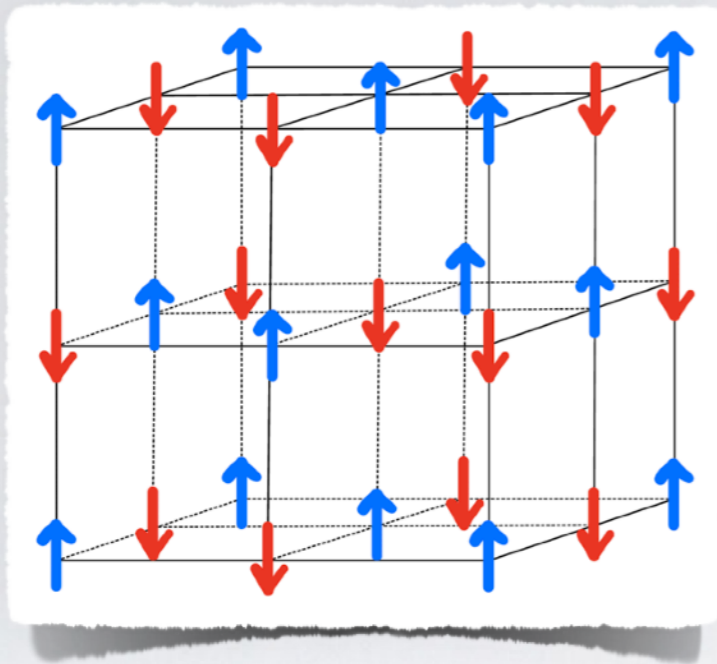
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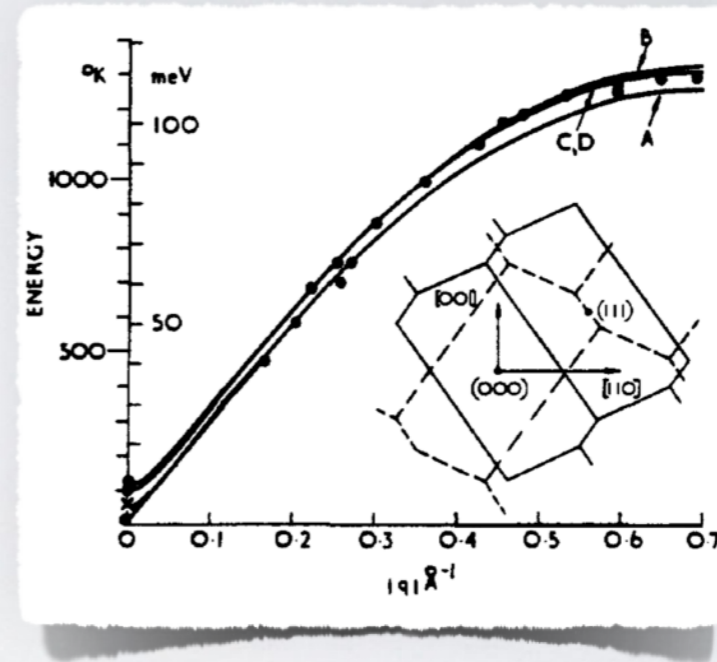
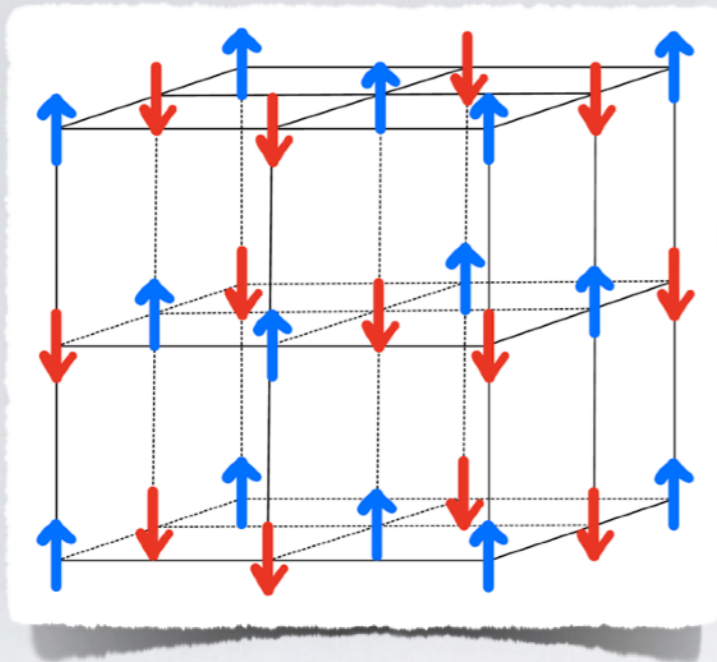
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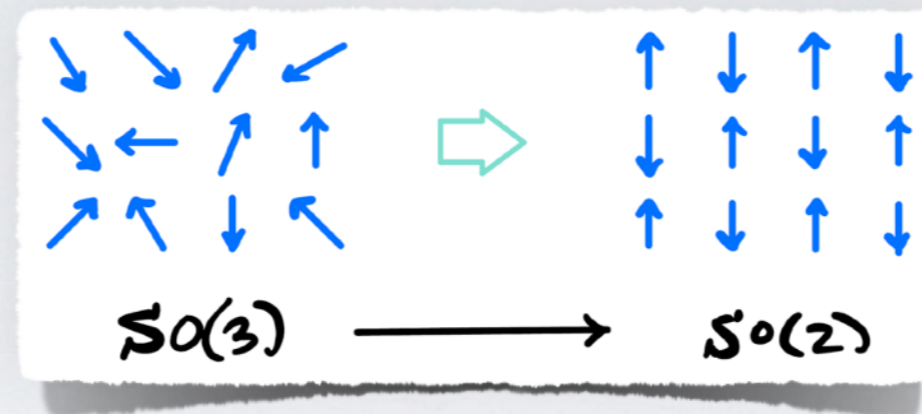


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- **Nickel-oxide** has $v_\theta \simeq v_\chi$ → **very efficient at absorbing dark matter energy** [AE, Pavaskar – PRD (2023), 2210.13516]

ANTI-FERROMAGNETS

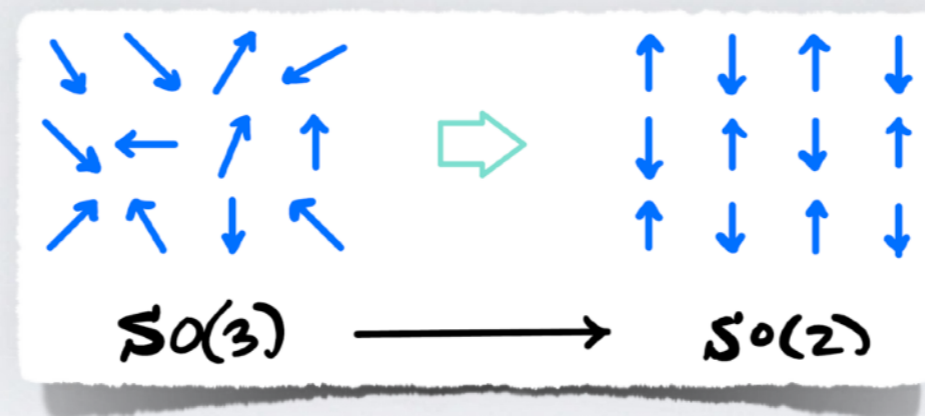
ANTI-FERROMAGNETS

- Anti-ferromagnet spontaneously break internal spin symmetry



ANTI-FERROMAGNETS

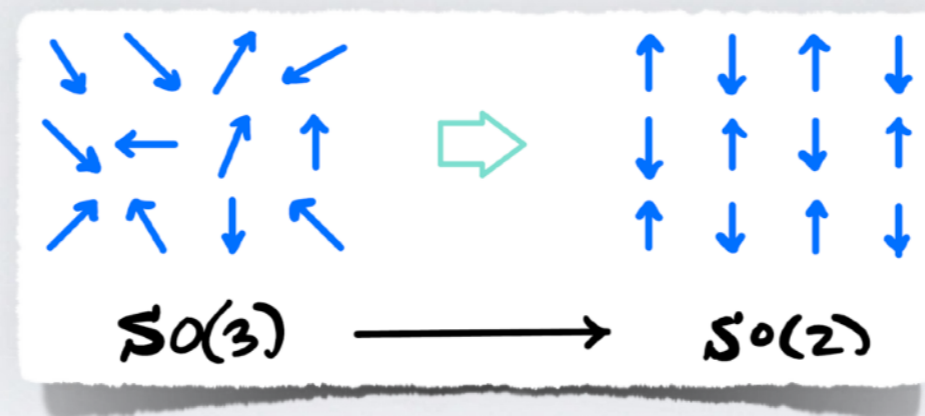
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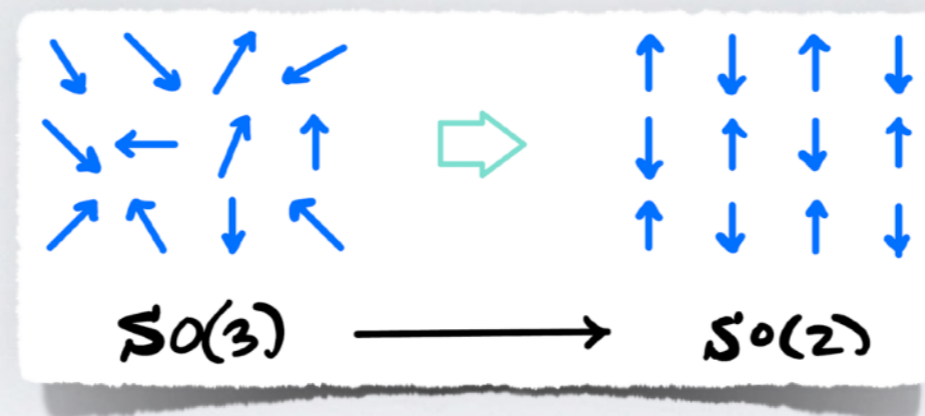


Write a low energy EFT: $\mathcal{L}_{EFT} = \frac{c_1}{2} \dot{\mathbf{n}}^2 - \frac{c_2}{2} (\partial_i \mathbf{n})^2$

[Pavaskar, Penco, Rothstein – SciPost Phys. (2022), 2112.13873; **AE**, Pavaskar – PRD (2023), 2210.13516]

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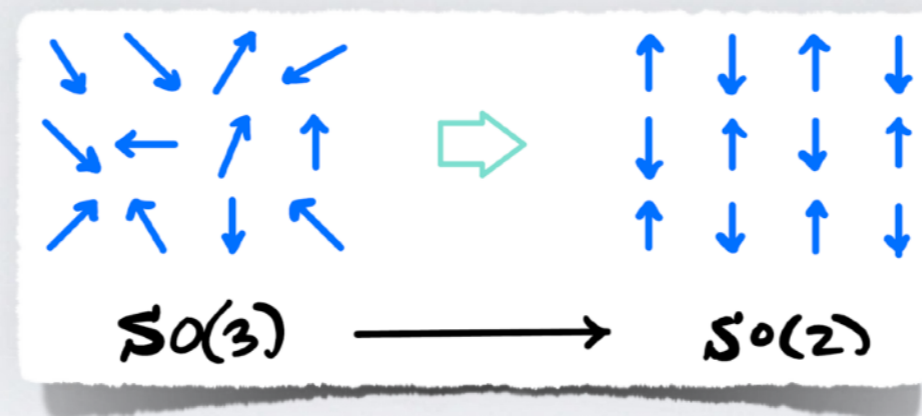
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Bypass standard difficulties in computing multi-magnon processes

[Dyson – Phys. Rev. 1956]

ANTI-FERROMAGNETS

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- With an EFT at hand → use [standard QFT methods](#) to compute event rates [\[AE, Pavaskar – PRD \(2023\), 2210.13516\]](#)

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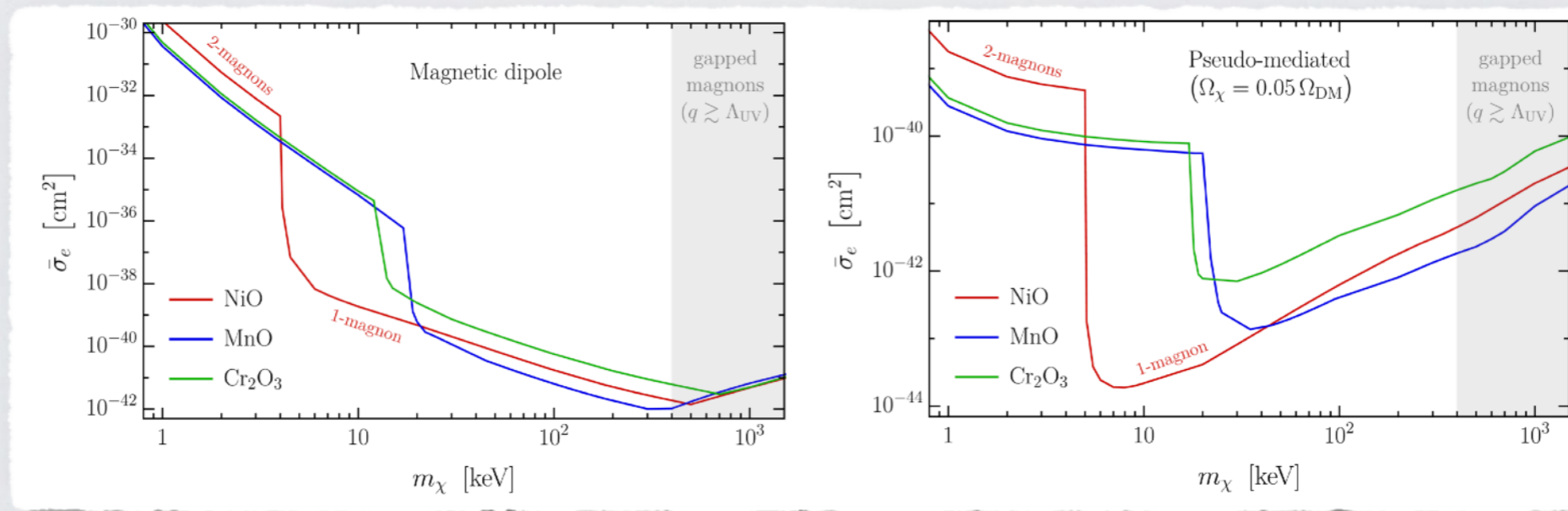
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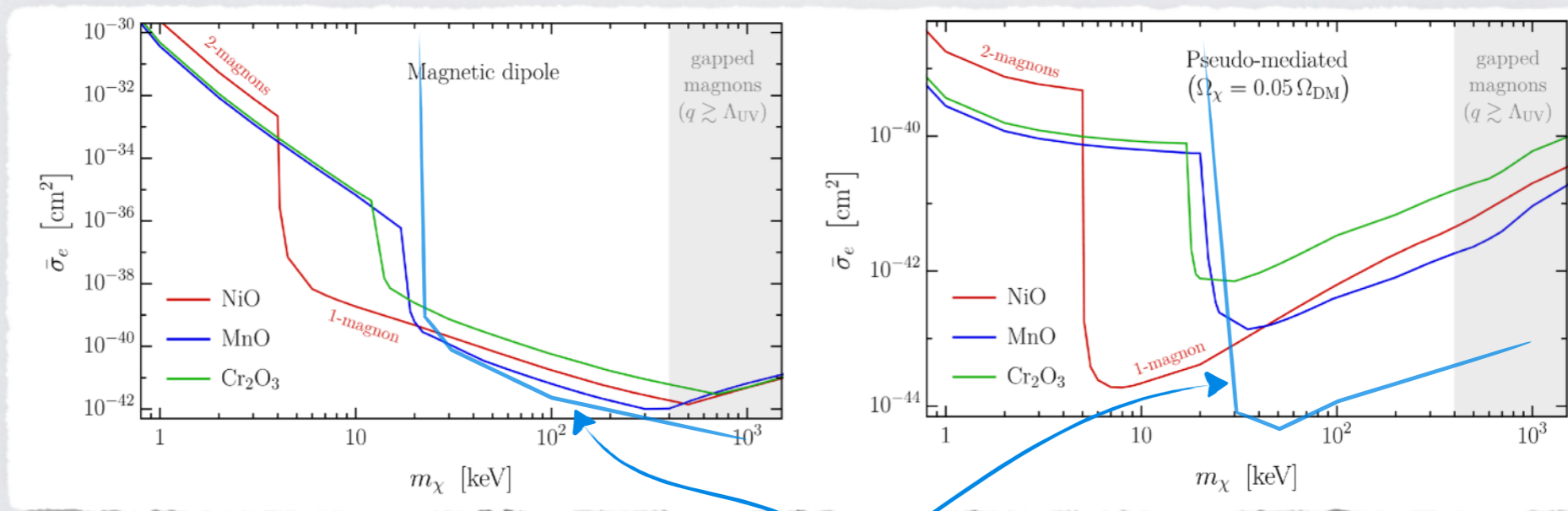


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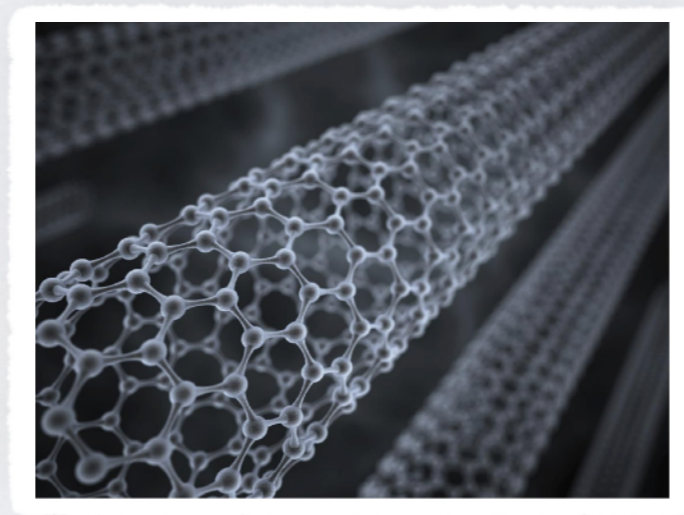
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Honorable mention: carbon nanotubes



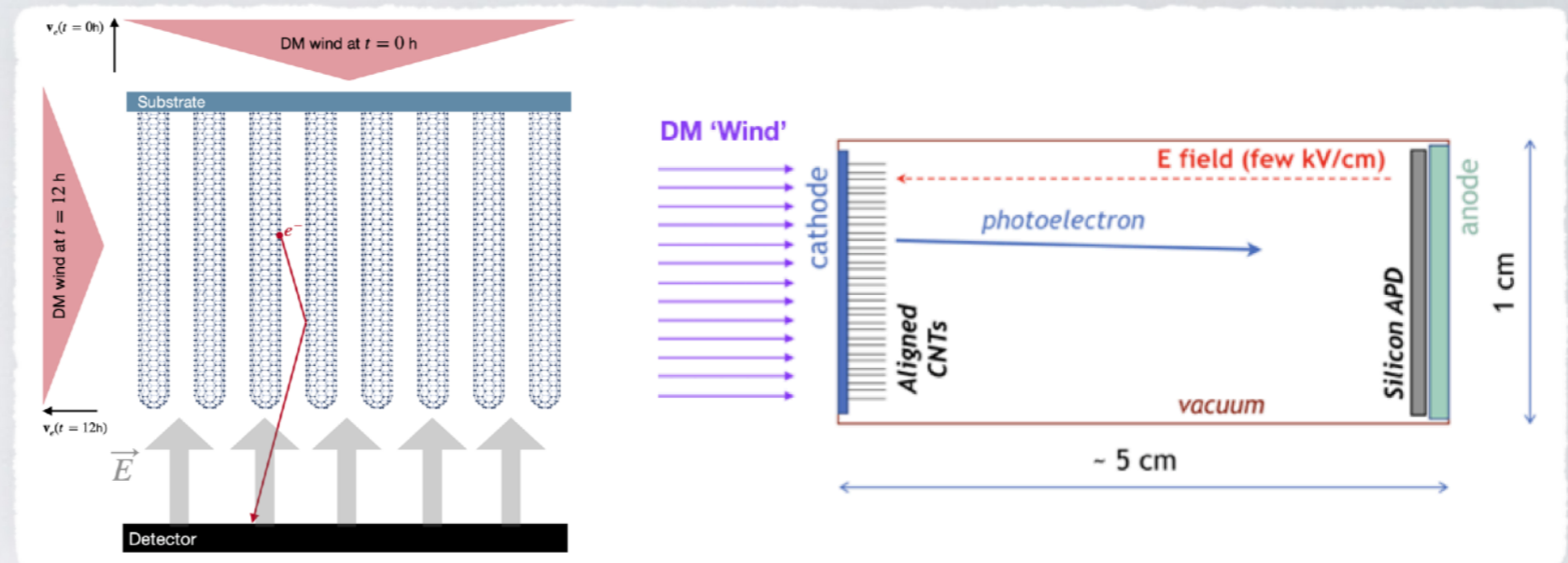
CARBON NANOTUBES

CARBON NANOTUBES

- Another promising proposal for sub-GeV dark matter searches are

carbon nanotubes

[Capparelli, Cavoto, Mazzilli, Polosa – Phys. Dark. Univ. 2015, 1412.8213;
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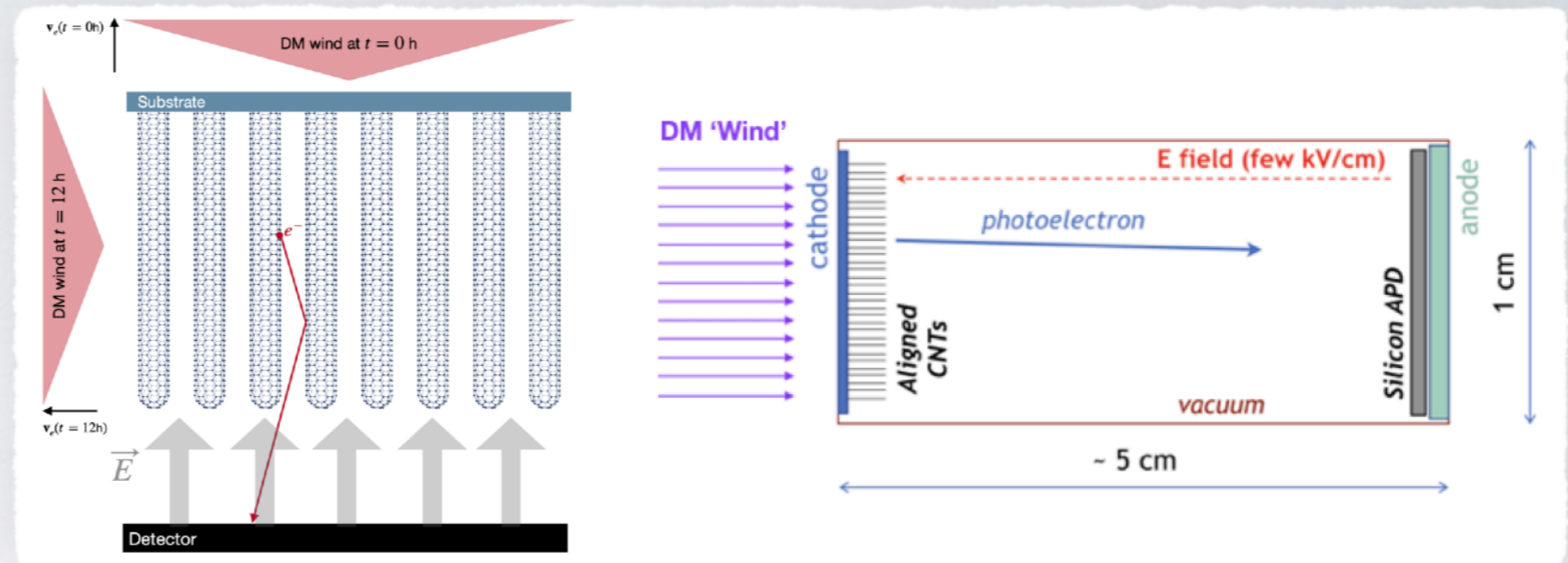


CARBON NANOTUBES

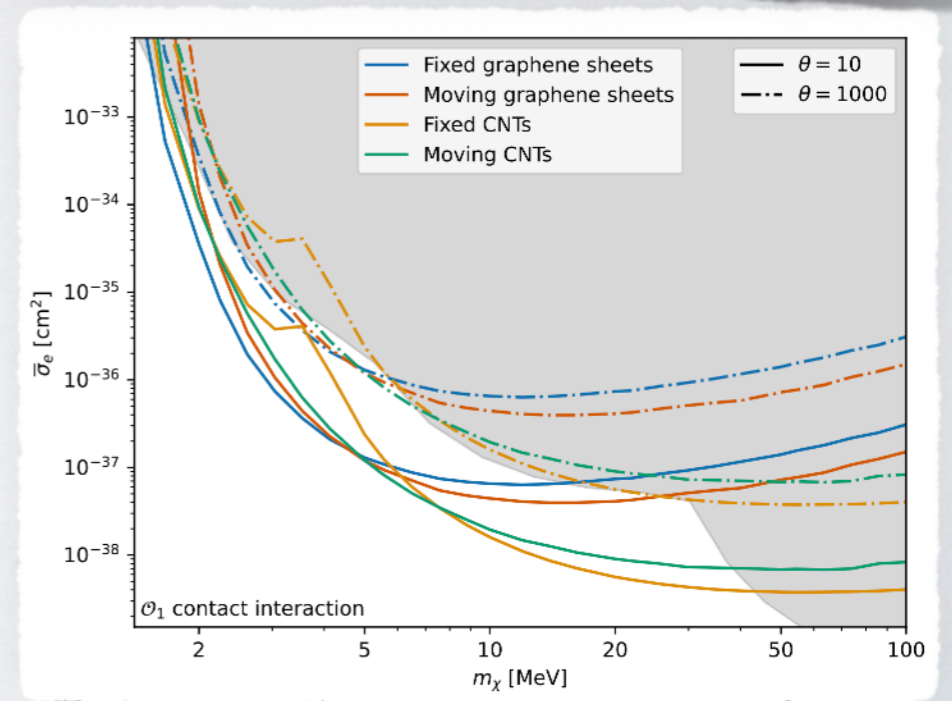
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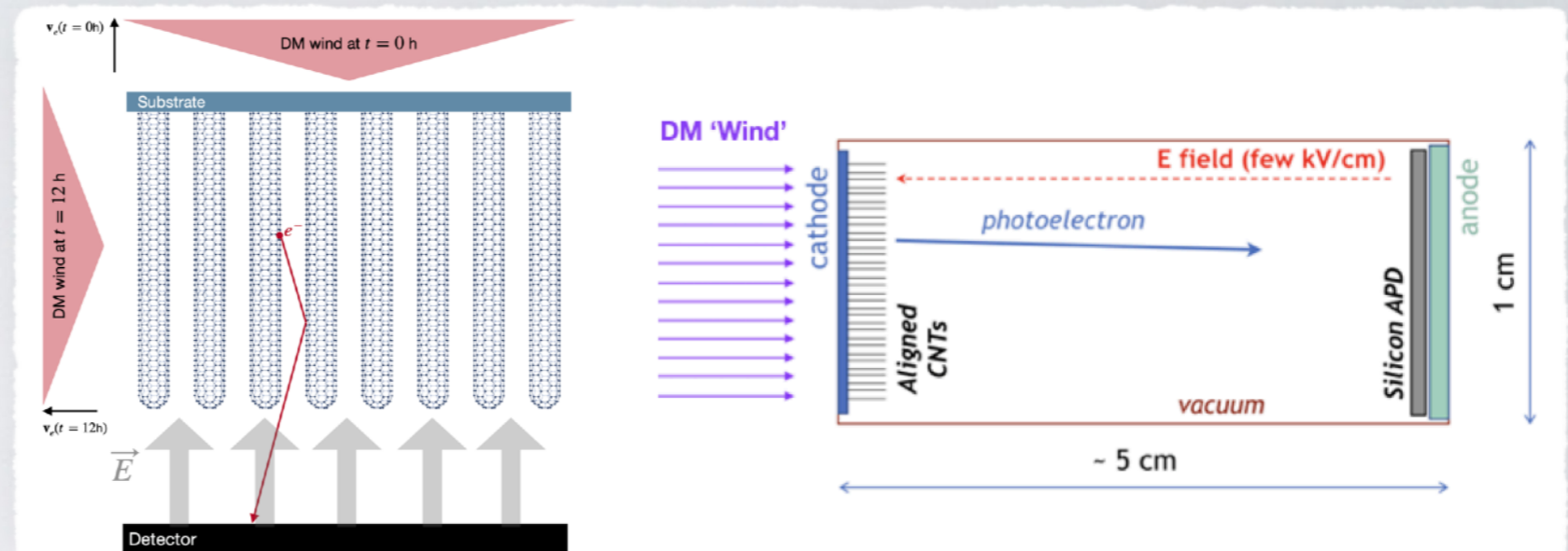


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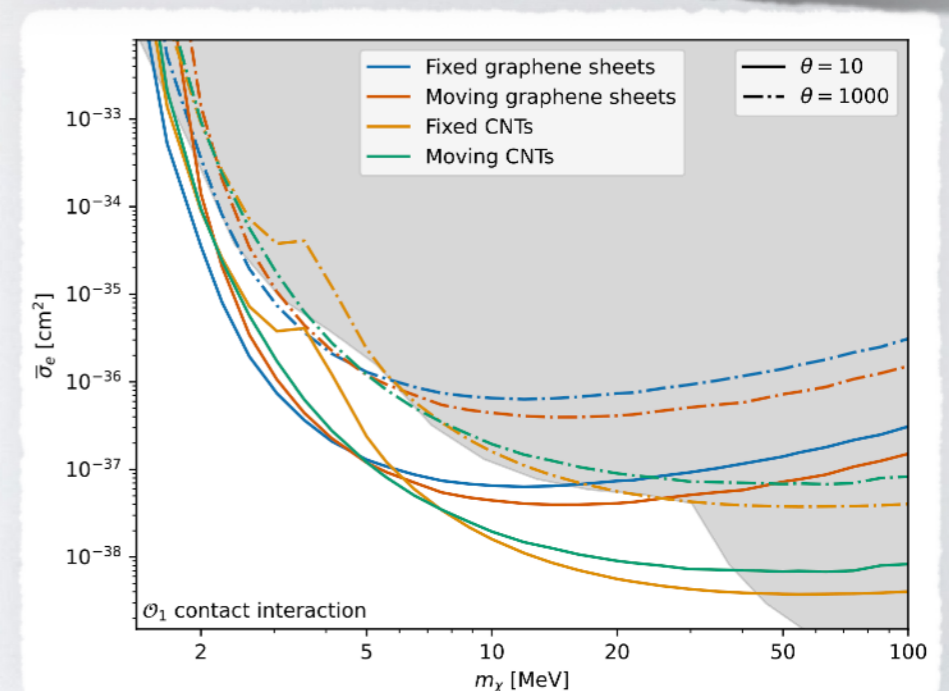
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- Might be a good probe for DM-nucleon interactions as well

[Cavoto, AE, Pandolfi, Papiri, Polosa, Tarquini – work in progress]



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Thank you for the attention!