



UNIVERSITÀ
DEGLI STUDI
DI PADOVA



Neutrino Phenomenology from Flavour Deconstruction

Andrea Sainaghi

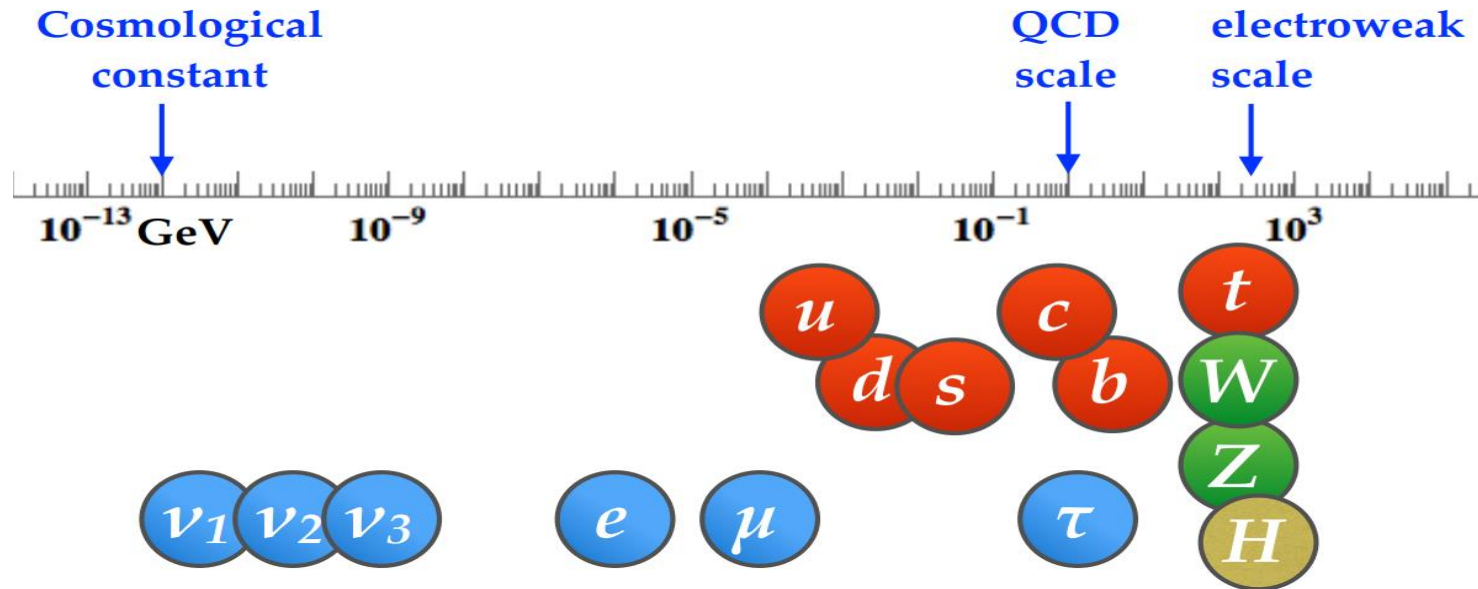
In collaboration with Gino Isidori, Paride Paradisi and Nudžeim Selimović



PLANCK 2025

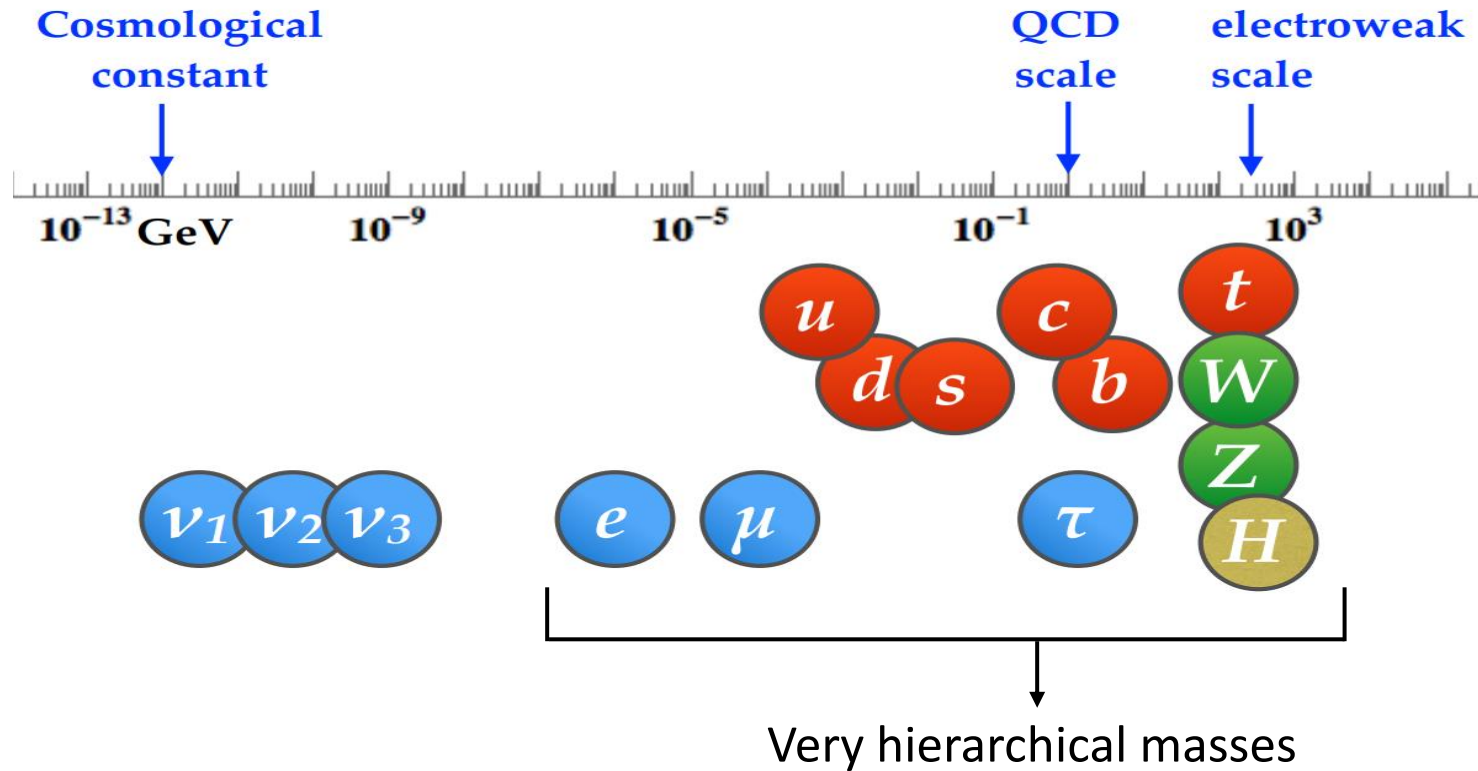
The Flavour Puzzle

Why are the SM-fermion masses so different?



The Flavour Puzzle

Why are the SM-fermion masses so different?

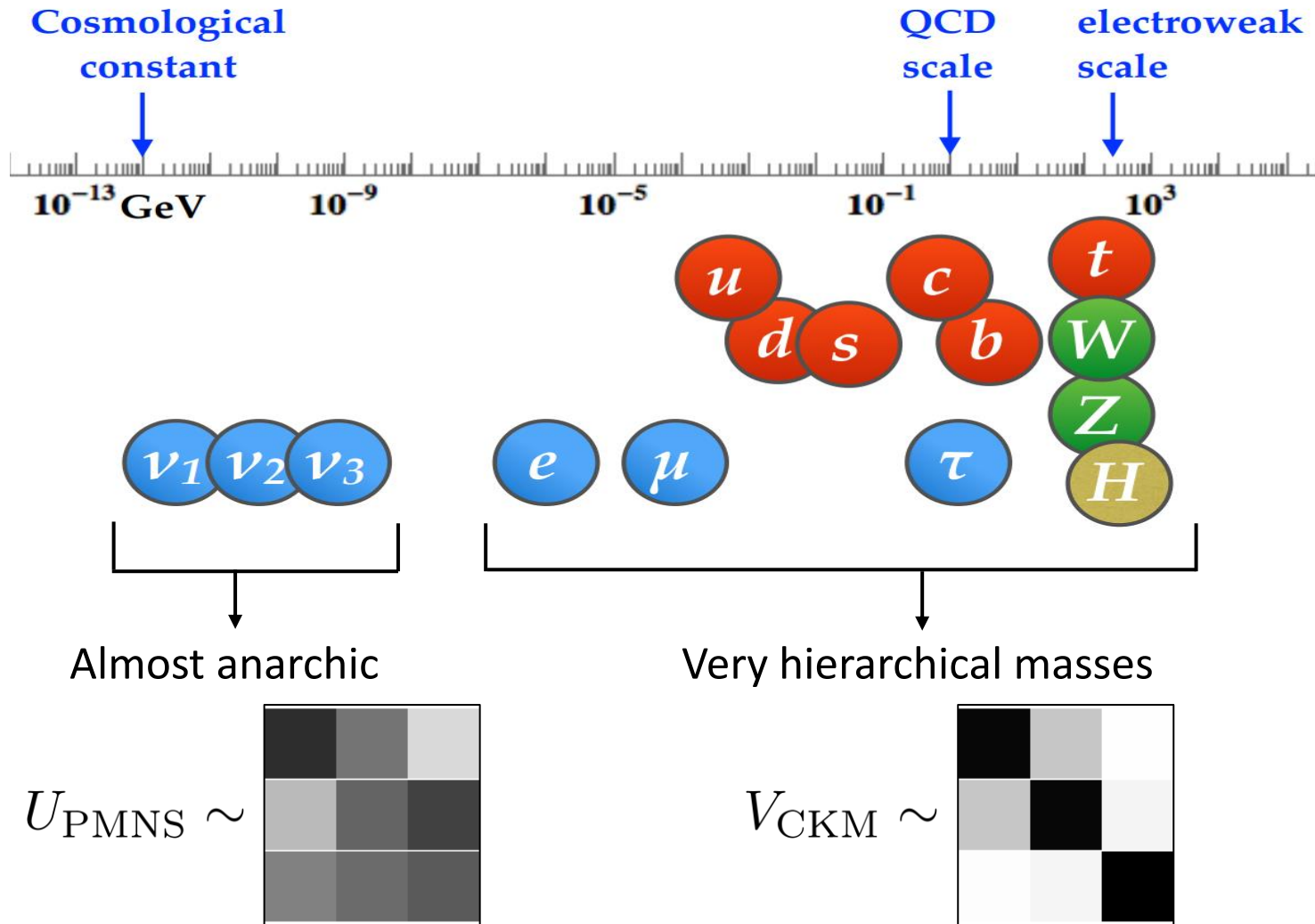


$$V_{\text{CKM}} \sim$$



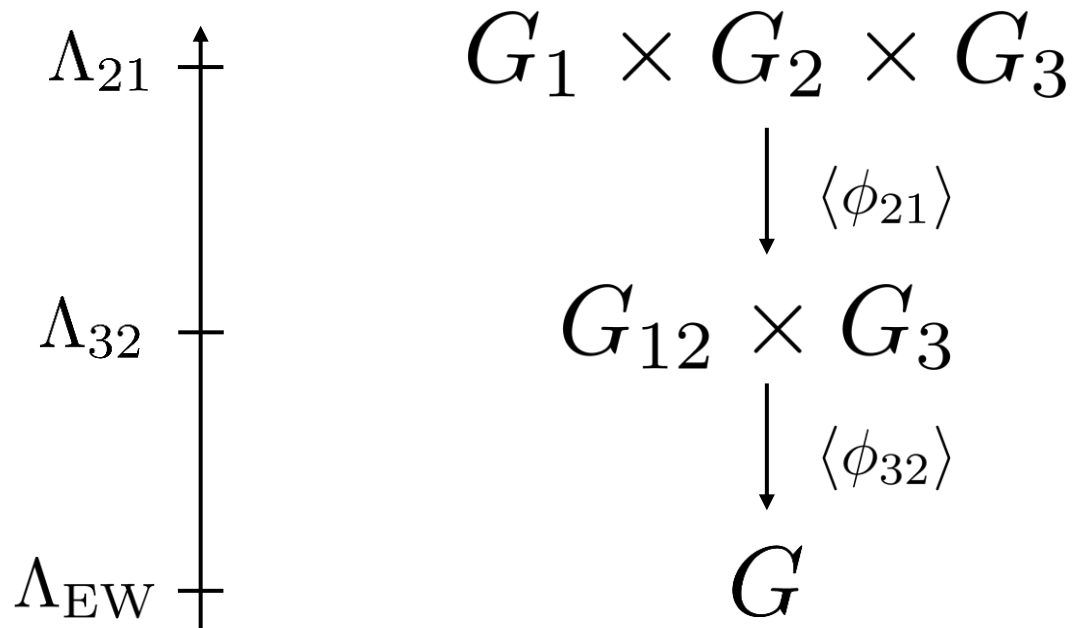
The Flavour Puzzle

Why are the SM-fermion masses so different?



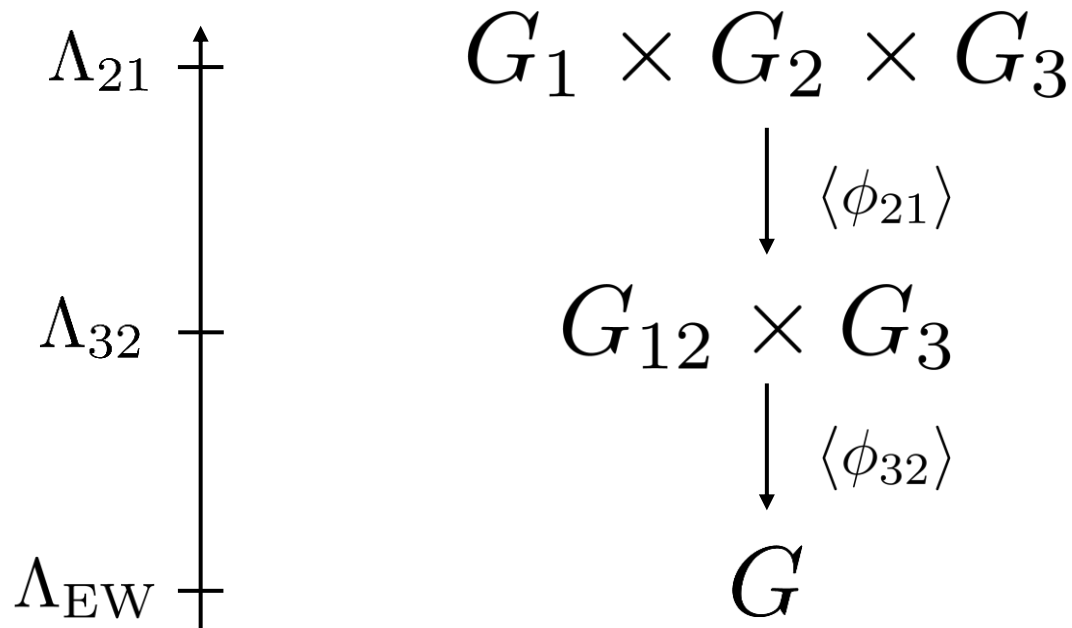
The Flavour Puzzle

Flavour deconstruction refers to a framework wherein the SM gauge group G is extended in the UV to G^3 , one for each fermion generation



The Flavour Puzzle

Flavour deconstruction refers to a framework wherein the SM gauge group G is extended in the UV to G^3 , one for each fermion generation



The hierarchies in the charged fermion masses are reproduced as long as

$$\langle \phi_{32} \rangle / \Lambda_{32} \ll 1 \quad \langle \phi_{21} \rangle / \Lambda_{21} \ll 1$$

However, it fails in explaining the anarchic neutrino sector

Theory Setup

Recently, [Greljo, Isidori, 2024] showed how to generate neutrino masses in a given flavour-deconstructed model using an Inverse Seesaw mechanism

$$-\mathcal{L} \supset \bar{\ell}_i Y_\nu^{ij} \tilde{H} \nu_j + \bar{s}_i M_R^{ij} \nu_j + \frac{1}{2} \bar{s}_i \mu^{ij} s_j^c + \text{h.c.}$$

Y_ν , M_R , μ are 3x3 matrices with $M_R \gg v Y_\nu \gg \mu$ $v \equiv \langle H \rangle$

$$Y_\nu \sim \begin{pmatrix} \varepsilon_1 \varepsilon_2 & & \\ & \varepsilon_1 & \\ & & 1 \end{pmatrix} \quad M_R \sim \Lambda \begin{pmatrix} \eta_1 \eta_2 & \eta_1 & 1 \\ \eta_1 \eta_2 & \eta_1 & 1 \\ \eta_1 \eta_2 & \eta_1 & 1 \end{pmatrix}$$

$\mu \longrightarrow$ Anarchic

$\Lambda \equiv \langle \chi \rangle$, where χ is a scalar which is charged under the flavour gauge sector G_3

The flavour non-universal gauge group ensures the hierarchies $\varepsilon_{2,1}, \eta_{2,1} \ll 1$

Theory Setup

Below the EW scale we have as mass eigenstates:

- 3 light active neutrinos with Majorana masses ν_L^i

$$m_\nu \approx A \mu A^T$$

- 3 heavy neutral leptons (HNLs) with hierarchical and (almost) Dirac masses n^i

$$M_n \approx \begin{pmatrix} 0 & M_R \\ M_R^T & \mu \end{pmatrix}$$

The anarchy in the active neutrino mass matrix is guaranteed since there is a (even partial) cancellation in the hierarchies as

$$A \equiv v Y_\nu M_R^{-1} \sim \frac{v}{\Lambda} \begin{pmatrix} \Delta_1 \Delta_2 & \Delta_1 \Delta_2 & \Delta_1 \Delta_2 \\ \Delta_1 & \Delta_1 & \Delta_1 \\ 1 & 1 & 1 \end{pmatrix} \quad \Delta_i \equiv \frac{\varepsilon_i}{\eta_i}$$

SM Interactions

The HNLs interact weakly with the SM

$$\mathcal{L} \supset \frac{g}{\sqrt{2}} \bar{e}_L W^- \textcolor{blue}{U} \nu_L + \frac{g}{\sqrt{2}} \bar{e}_L W^- \textcolor{violet}{V} n_L + \text{h.c.} + \mathcal{L}_Z$$

We exploit the following parameterization for the mixing matrices

$$\textcolor{blue}{U} = \mathcal{N} \left(1 - \frac{1}{2} \textcolor{green}{W} \textcolor{green}{W}^\dagger \right) \quad \textcolor{violet}{V} = \mathcal{N} \textcolor{green}{W} \quad \textcolor{green}{W} = \mathcal{U}^\dagger \hat{A} U_S^\dagger$$

Where \mathcal{N} is the PMNS matrix of the SM and \mathcal{U} , U_S are 3x3 unitary matrices while $\hat{A} = \frac{v}{\Lambda} \text{diag}(\Delta_1 \Delta_2, \Delta_1, 1)$

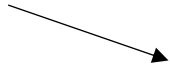
Parameters

There are 11 parameters relevant for the phenomenology:

Λ



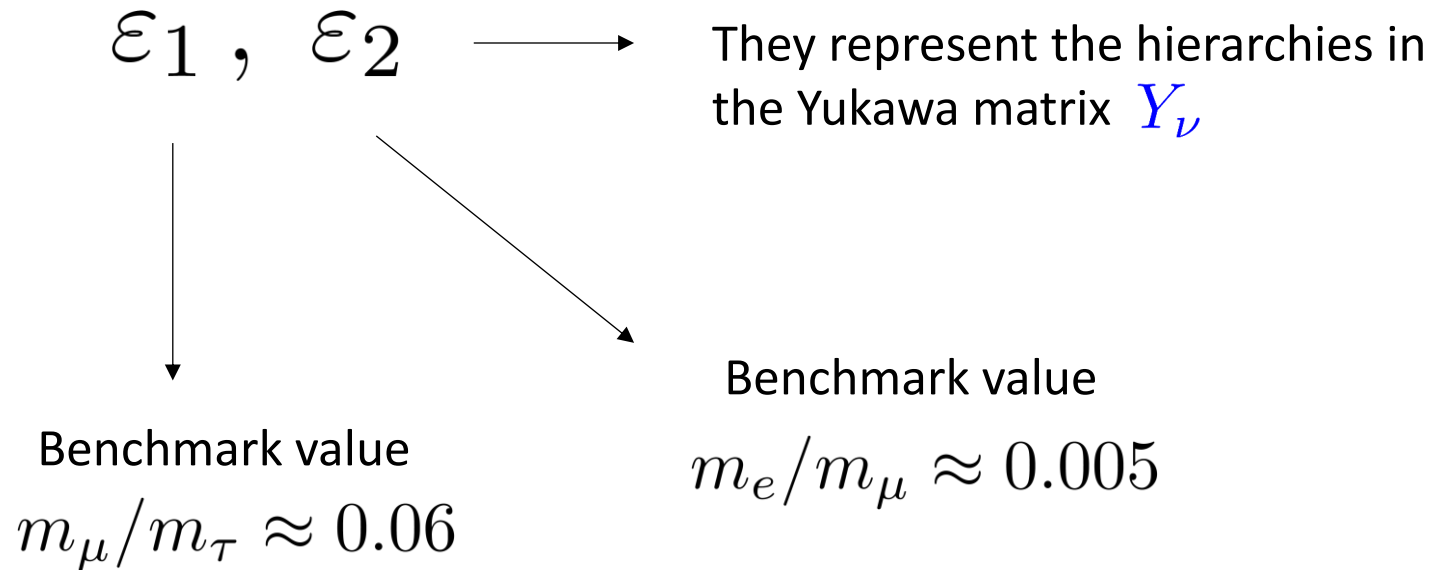
New-Physics (NP) scale



Hopefully around few TeV

Parameters

There are 11 parameters relevant for the phenomenology:



Parameters

There are 11 parameters relevant for the phenomenology:

$$\Delta_1, \Delta_2$$

They effectively represent the hierarchies
in the Heavy mass matrix M_R
(traded for η_1, η_2)

They enter in m_ν , so, if they departure too much from 1, the model
fails in reproducing the PMNS matrix as μ is assumed anarchic

Normal Ordering:

$$m_1 < m_2 < m_3$$

$$0.25 \lesssim \Delta_1 \lesssim 0.6 \quad 0.15 \lesssim \Delta_2 < 1$$

Inverted Ordering:


$$m_3 < m_1 \lesssim m_2$$

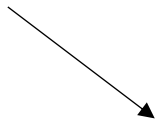
$$1 < \Delta_1 \lesssim 4$$

$$\Delta_2 \approx 1$$

Parameters

There are 11 parameters relevant for the phenomenology:

$\alpha_1, \alpha_2, \alpha_3$  Three angles that parameterize the 3x3 unitary matrix \mathcal{U}



If the leptonic Yukawa matrices are diagonalized on the left by matrices close to the identity, then

$$\alpha_i \approx \theta_i \quad (\theta_i \text{ are the PMNS mixing angles})$$

$$\mathcal{L} \supset \frac{g}{\sqrt{2}} \bar{e}_L W^- U \nu_L + \frac{g}{\sqrt{2}} \bar{e}_L W^- V n_L + \text{h.c.} + \mathcal{L}_Z$$

$$U = \mathcal{N} \left(1 - \frac{1}{2} W W^\dagger \right) \quad V = \mathcal{N} W \quad W = \mathcal{U}^\dagger \hat{A} U_S^\dagger \quad \alpha_i \text{ here}$$

Parameters

There are 11 parameters relevant for the phenomenology:

$$\beta_1, \beta_2, \beta_3$$

Three angles that parameterize the 3x3 unitary matrix U_S

In principle, they can range in $[0, 2\pi]$

They are related to the singlets of the Inverse Seesaw only, so there is no way to constrain them

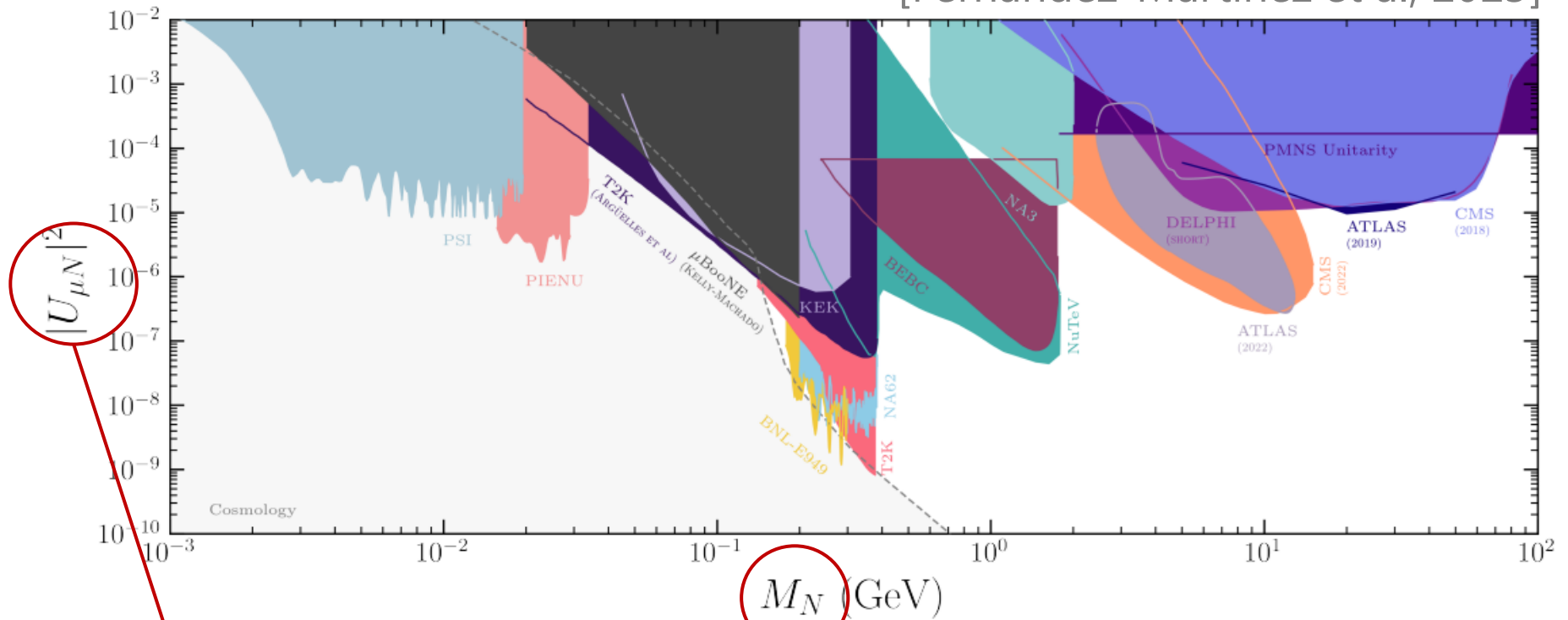
$$\mathcal{L} \supset \frac{g}{\sqrt{2}} \bar{e}_L W^- U \nu_L + \frac{g}{\sqrt{2}} \bar{e}_L W^- V n_L + \text{h.c.} + \mathcal{L}_Z$$

$$U = \mathcal{N} \left(1 - \frac{1}{2} W W^\dagger \right) \quad V = \mathcal{N} W \quad W = \mathcal{U}^\dagger \hat{A} U_S^\dagger$$

β_i here

Direct Searches

[Fernández-Martínez et al, 2023]



The HNLs have hierarchical masses
and interact with the charged leptons

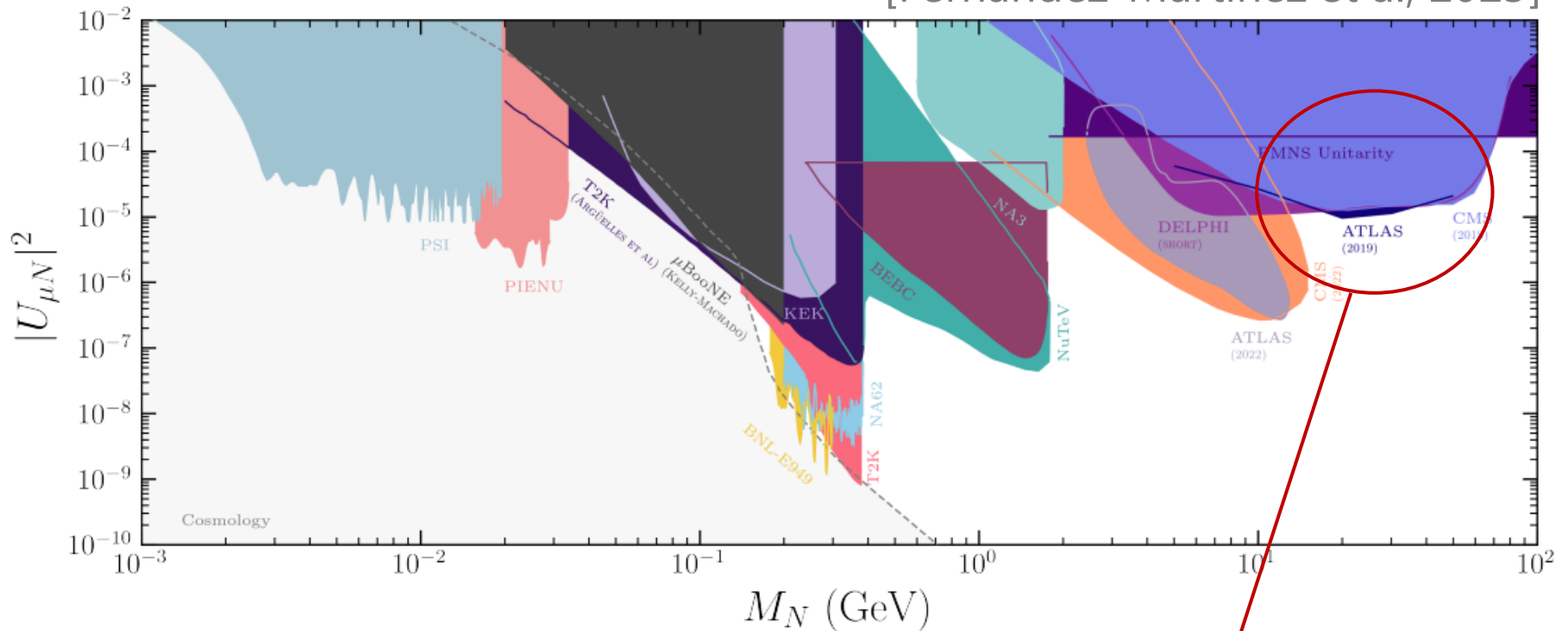
$$V_{eN} \sim v/\Lambda$$

$$M_3 = \Lambda \quad M_2 = \Lambda \frac{\varepsilon_1}{\Delta_1}$$

$$M_1 = \Lambda \frac{\varepsilon_1}{\Delta_1} \frac{\varepsilon_2}{\Delta_2}$$

Direct Searches

[Fernández-Martínez et al, 2023]



If the lightest HNL is lighter than Z and W bosons,
it can be produced on-shell at colliders

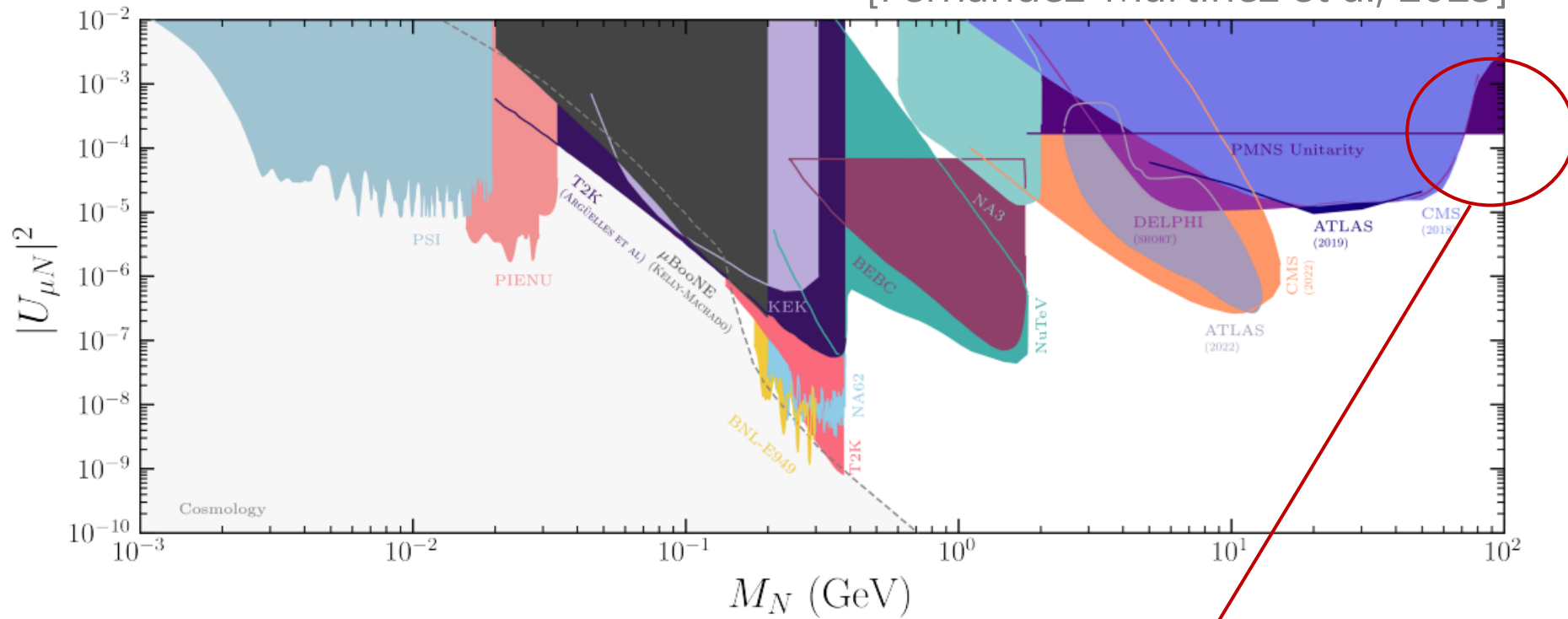
$$M_1 < M_{W,Z}$$

imposes

$$\Lambda \gtrsim 25 \text{ TeV}$$

Direct Searches

[Fernández-Martínez et al, 2023]



Otherwise, for $M_1 > M_{W,Z}$

$$\Lambda \gtrsim 20 \left(\frac{\Delta_1 \Delta_2}{0.07} \right) \left(\frac{m_\mu / m_\tau}{\varepsilon_1} \right) \left(\frac{m_e / m_\mu}{\varepsilon_2} \right) \text{ TeV}$$

PMNS non-Unitarity

As we add new neutrino states, the PMNS matrix is not unitary anymore

$$\eta \equiv |\mathbb{I} - UU^\dagger| \sim \left(\frac{v}{\Lambda}\right)^2 \begin{pmatrix} \Delta_1^2 \Delta_2^2 & \Delta_1^2 \Delta_2 & \Delta_1 \Delta_2 \\ \Delta_1^2 \Delta_2 & \Delta_1^2 & \Delta_1 \\ \Delta_1 \Delta_2 & \Delta_1 & 1 \end{pmatrix}$$

The current updated bounds
are [Antusch, Fischer, 2014]

$$\eta < \begin{pmatrix} 2.1 \cdot 10^{-3} & 1.0 \cdot 10^{-5} & 2.1 \cdot 10^{-3} \\ 1.0 \cdot 10^{-5} & 4.0 \cdot 10^{-4} & 8.0 \cdot 10^{-4} \\ 2.1 \cdot 10^{-3} & 8.0 \cdot 10^{-4} & 5.3 \cdot 10^{-3} \end{pmatrix}$$

Normal Ordering: η_{33} imposes $\Lambda \gtrsim 2.5 \text{ TeV}$

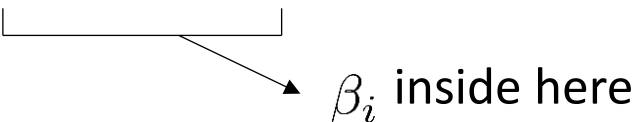
Inverted Ordering: η_{11} imposes $\Lambda \gtrsim 4\Delta_1 \text{ TeV}$

LFV Processes

Currently, $\mu \rightarrow e\gamma$ is the most constraining LFV process

$$\text{Br}(\mu \rightarrow e\gamma) = \frac{3\alpha}{2\pi} |\delta_\nu|^2$$

$$\begin{aligned}\delta_\nu &= \sum_k V_{ek} V_{\mu k}^* G_\gamma \left(\frac{M_k^2}{M_W^2} \right) \\ &\approx \frac{v^2}{\Lambda^2} \Delta_1^2 \Delta_2 \sum_k (U_S)_{ek} (U_S^*)_{\mu k} G_\gamma \left(\frac{M_k^2}{M_W^2} \right)\end{aligned}$$

 β_i inside here

LFV Processes

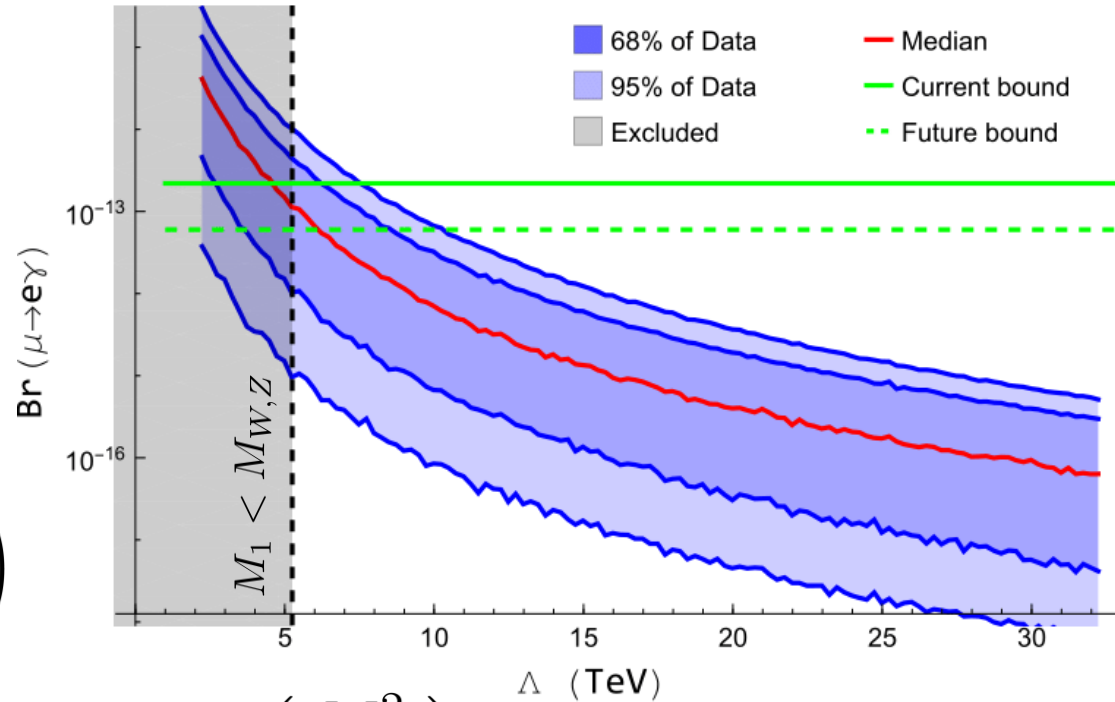
Currently, $\mu \rightarrow e\gamma$ is the most constraining LFV process

$$\text{Br}(\mu \rightarrow e\gamma) = \frac{3\alpha}{2\pi} |\delta_\nu|^2$$

$$\delta_\nu = \sum_k V_{ek} V_{\mu k}^* G_\gamma \left(\frac{M_k^2}{M_W^2} \right)$$

$$\approx \frac{v^2}{\Lambda^2} \underbrace{\Delta_1^2 \Delta_2}_{\substack{\downarrow \\ \text{Normal Ordering allows for } \Lambda \text{ to be around few TeV}}} \sum_k \underbrace{(U_S)_{ek} (U_S^*)_{\mu k}}_{\substack{\nearrow \\ \beta_i \text{ inside here}}} G_\gamma \left(\frac{M_k^2}{M_W^2} \right)$$

Normal Ordering allows for Λ to be around few TeV



Plot of $\text{Br}(\mu \rightarrow e\gamma)$ with

$$\Delta_1 = 0.35 \quad \Delta_2 = 0.2$$

$$\varepsilon_1 = 0.06 \quad \varepsilon_2 = 0.02$$

$$\alpha_i \in [\theta_i - 0.1, \theta_i + 0.1]$$

$$\beta_i \in [0, 2\pi]$$

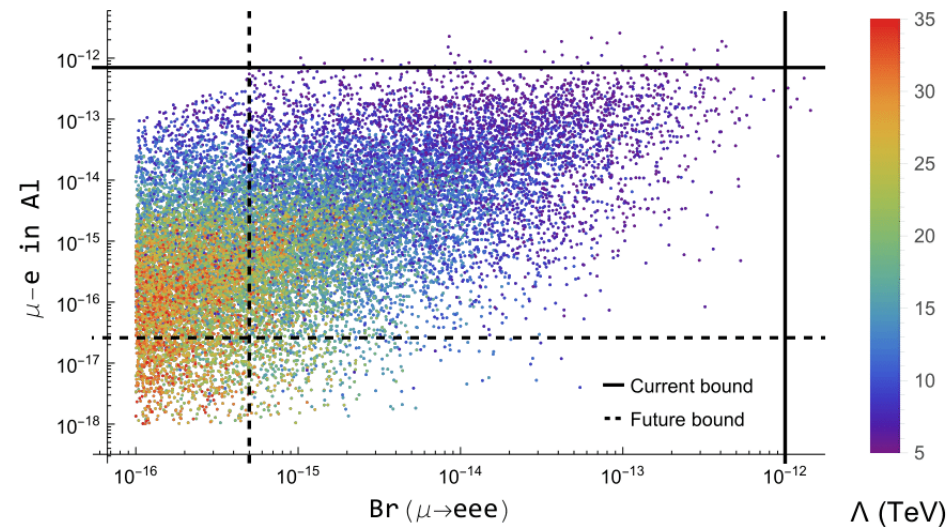
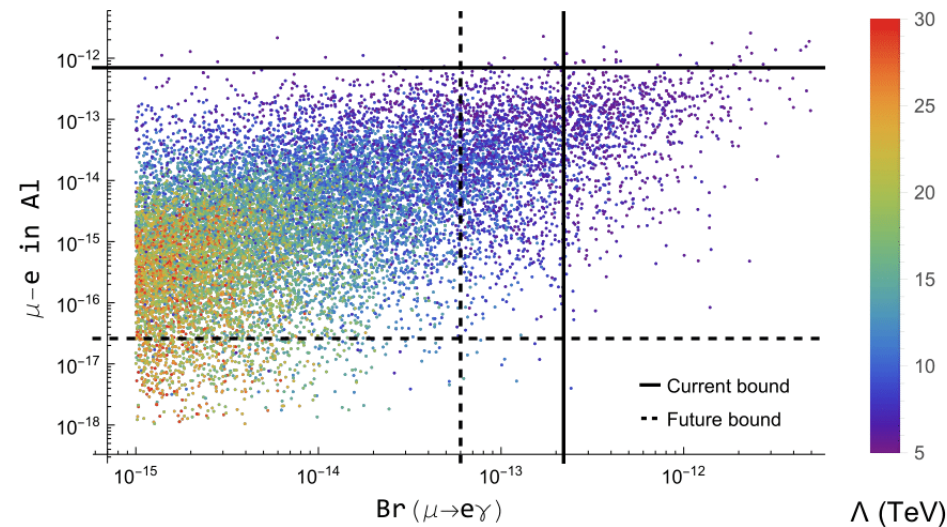
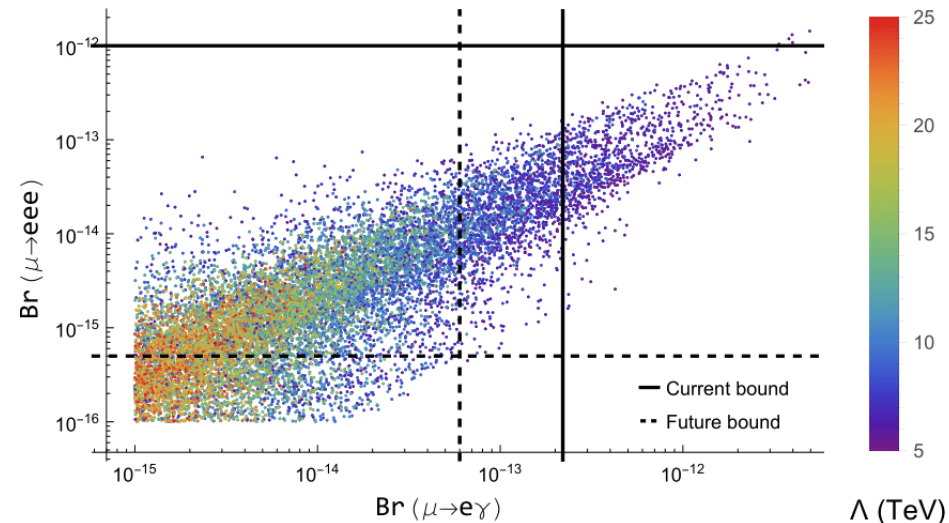
LFV Processes

Correlation plots between
the main LFV processes

$$\begin{array}{cc} \text{Br}(\mu \rightarrow e\gamma) & \text{Br}(\mu \rightarrow eee) \\ \text{Br}(\mu \text{ Al} \rightarrow e \text{ Al}) & \end{array}$$

$$\Delta_1 = 0.35 \quad \Delta_2 = 0.2 \quad \varepsilon_1 = 0.06 \quad \varepsilon_2 = 0.02$$

$$\alpha_i \in [\theta_i - 0.1, \theta_i + 0.1] \quad \beta_i \in [0, 2\pi]$$



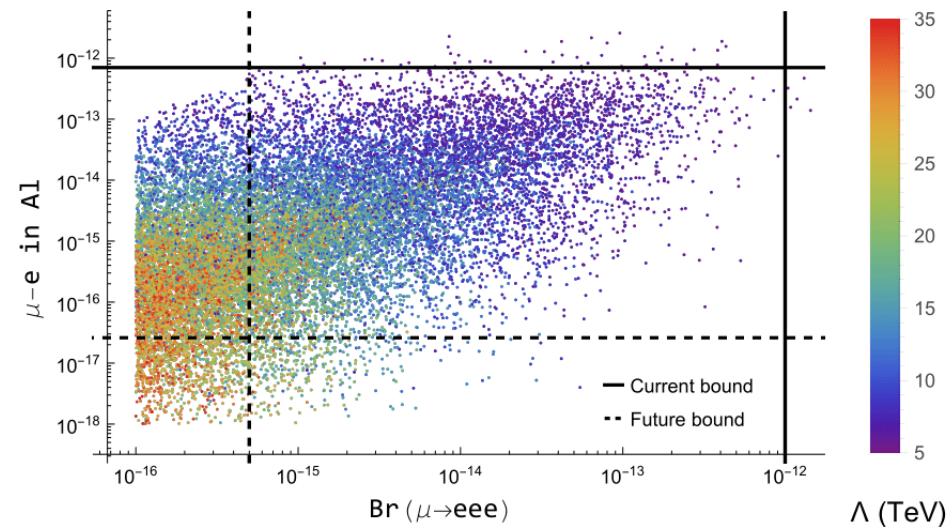
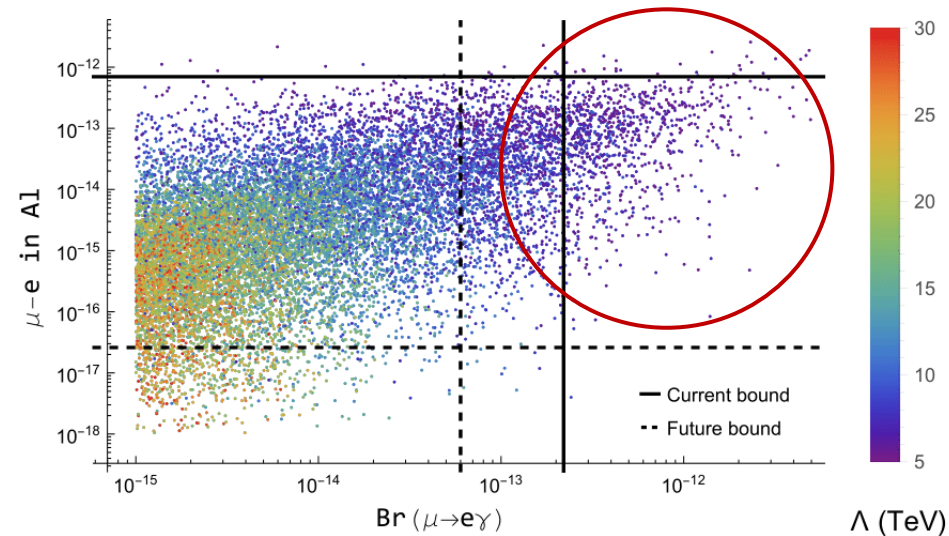
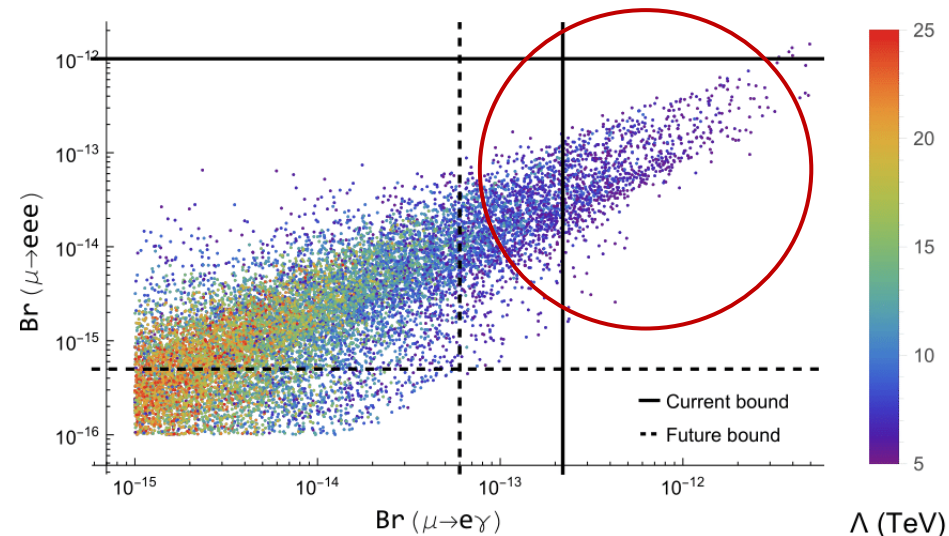
LFV Processes

Correlation plots between
the main LFV processes

$$\begin{array}{cc} \text{Br}(\mu \rightarrow e\gamma) & \text{Br}(\mu \rightarrow eee) \\ \text{Br}(\mu \text{ Al} \rightarrow e \text{ Al}) & \end{array}$$

$$\Delta_1 = 0.35 \quad \Delta_2 = 0.2 \quad \varepsilon_1 = 0.06 \quad \varepsilon_2 = 0.02$$

$$\alpha_i \in [\theta_i - 0.1, \theta_i + 0.1] \quad \beta_i \in [0, 2\pi]$$



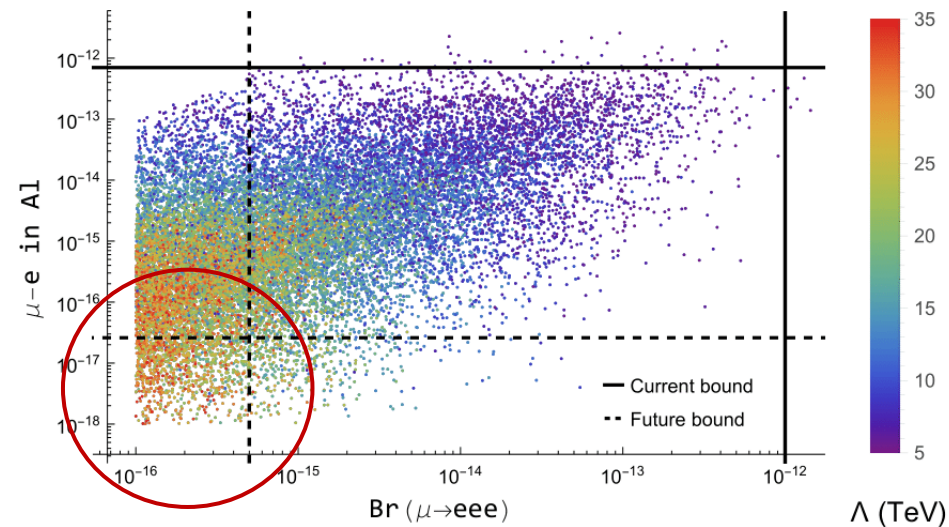
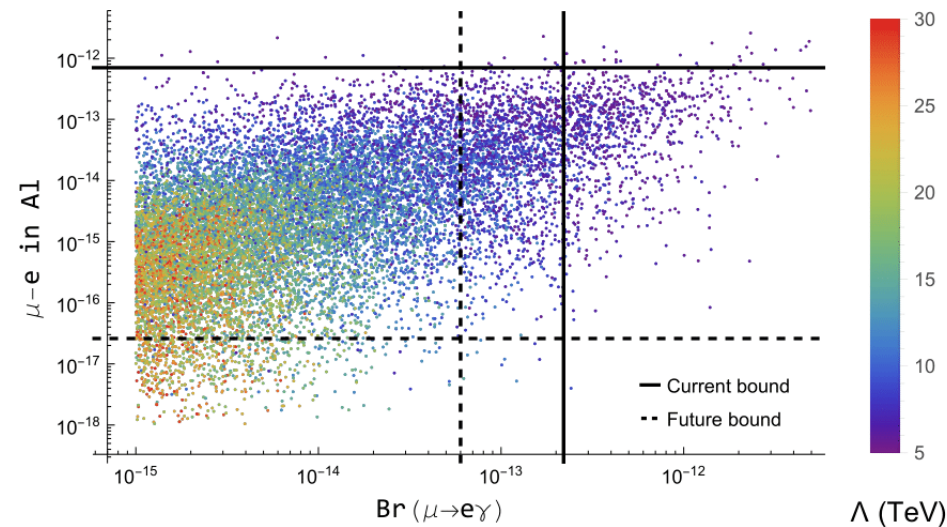
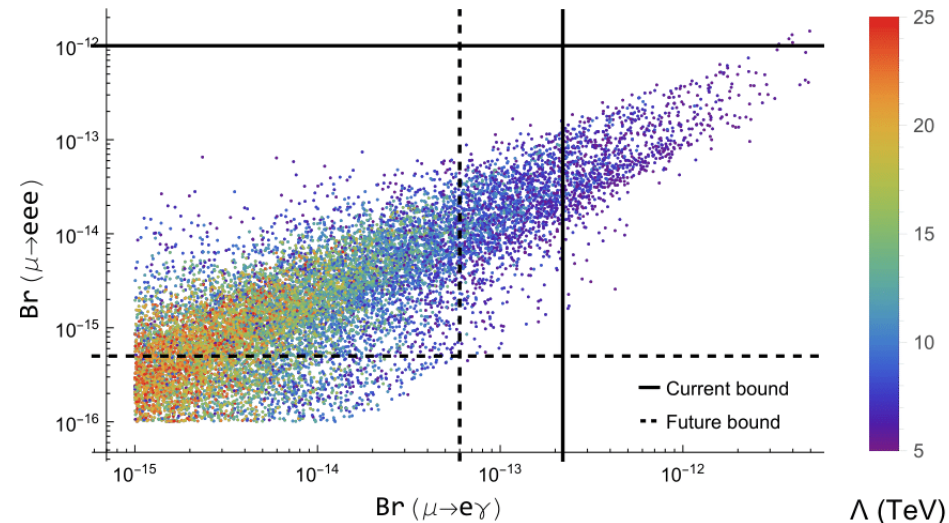
LFV Processes

Correlation plots between
the main LFV processes

$$\begin{array}{cc} \text{Br}(\mu \rightarrow e\gamma) & \text{Br}(\mu \rightarrow eee) \\ \text{Br}(\mu \text{ Al} \rightarrow e \text{ Al}) & \end{array}$$

$$\Delta_1 = 0.35 \quad \Delta_2 = 0.2 \quad \varepsilon_1 = 0.06 \quad \varepsilon_2 = 0.02$$

$$\alpha_i \in [\theta_i - 0.1, \theta_i + 0.1] \quad \beta_i \in [0, 2\pi]$$



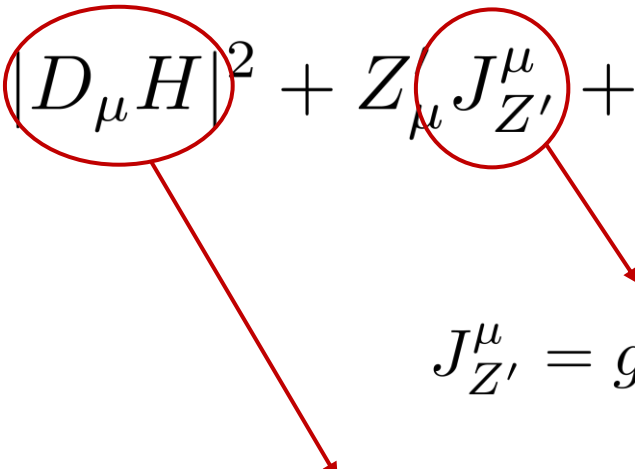
LFV from Gauge and Yukawa Sectors

Flavour-deconstructed models predict LFV processes even without including neutrinos

$$\mathcal{L} \supset |D_\mu H|^2 + Z'_\mu J^\mu_{Z'} + \frac{1}{2} M_{Z'} Z'_\mu Z'^\mu + \mathcal{L}_Y$$

LFV from Gauge and Yukawa Sectors

Flavour-deconstructed models predict LFV processes even without including neutrinos

$$\mathcal{L} \supset |D_\mu H|^2 + Z_\mu J_{Z'}^\mu + \frac{1}{2} M_{Z'} Z'_\mu Z'^\mu + \mathcal{L}_Y$$


$$J_{Z'}^\mu = g_{\text{NP}} \sum_\psi \bar{\psi} \gamma^\mu \psi Q_{Z'}(\psi)$$

$$D_\mu H \supset \partial_\mu H - \frac{ig}{c_W} (T_3 - s_W^2 Q) Z_\mu H - ig_{\text{NP}} Q_{Z'}(H) Z'_\mu H$$

Z' \longrightarrow It is a neutral heavy gauge boson that couples non-universally with all the fermions in the theory

LFV from Gauge and Yukawa Sectors

Flavour-deconstructed models predict LFV processes even without including neutrinos

$$\mathcal{L} \supset |D_\mu H|^2 + Z'_\mu J^\mu_{Z'} + \frac{1}{2} M_{Z'} Z'_\mu Z'^\mu + \mathcal{L}_Y$$

$$\mathcal{L}_Y \sim y_{33} \bar{\ell}_3 H e_3 + \sum_{j=1,2} \sum_{\alpha=\text{heavy}} Y_{j\alpha} \bar{\ell}_j H E_\alpha$$
$$+ \left[\sum_{\alpha=\text{heavy}} Y'_{\alpha i} \bar{E}_\alpha \phi_{32} e_2 + \sum_{\alpha=\text{heavy}} M_\alpha \bar{E}_\alpha E_\alpha + 1^{\text{st}} \text{ generation} \right]$$

$E_\alpha \longrightarrow$ Heavy NP fermions

$$\Lambda_{32} \sim M_\alpha$$

LFV from Gauge and Yukawa Sectors

Flavour-deconstructed models predict LFV processes even without including neutrinos

$$\mathcal{L} \supset |D_\mu H|^2 + Z'_\mu J^\mu_{Z'} + \frac{1}{2} M_{Z'} Z'_\mu Z'^\mu + \mathcal{L}_Y$$

$$\mathcal{L}_Y \sim y_{33} \bar{\ell}_3 H e_3 + \sum_{j=1,2} \sum_{\alpha=\text{heavy}} Y_{j\alpha} \bar{\ell}_j H E_\alpha$$

$$+ \left[\sum_{\alpha=\text{heavy}} Y'_{\alpha i} \bar{E}_\alpha \phi_{32} e_2 + \sum_{\alpha=\text{heavy}} M_\alpha \bar{E}_\alpha E_\alpha + 1^{\text{st}} \text{ generation} \right]$$

It generates a mass-mixing matrix between light and heavy fermions

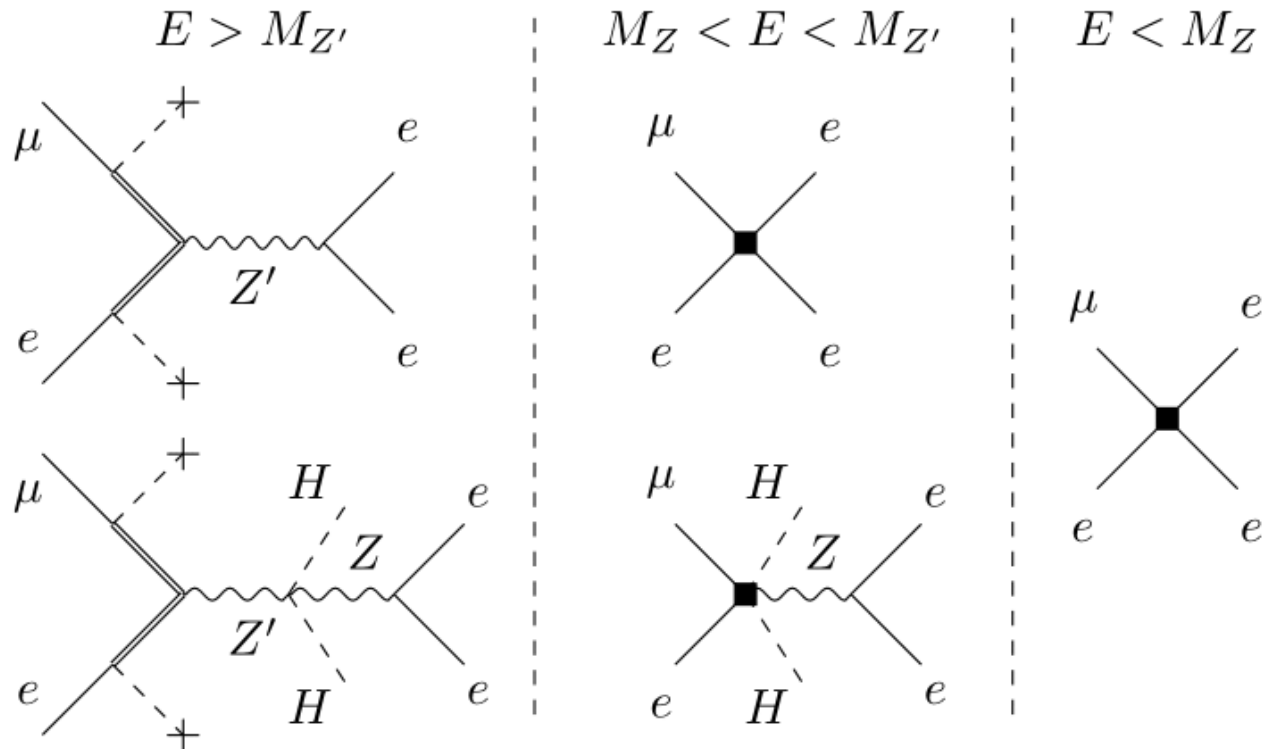
$$U_{\text{mix}} = \begin{pmatrix} \mathbb{I} - \frac{1}{2} \mathcal{E}^\dagger \mathcal{E} & \mathcal{E}^\dagger \\ -\mathcal{E} & \mathbb{I} - \frac{1}{2} \mathcal{E} \mathcal{E}^\dagger \end{pmatrix}$$

$$\mathcal{E} \sim \langle \phi_{32} \rangle / \Lambda_{32}$$

LFV from Gauge and Yukawa Sectors

Flavour-deconstructed models predict LFV processes even without including neutrinos

$$\mathcal{L} \supset |D_\mu H|^2 + Z'_\mu J^\mu_{Z'} + \frac{1}{2} M_{Z'} Z'_\mu Z'^\mu + \mathcal{L}_Y$$



LFV from Gauge and Yukawa Sectors

Flavour-deconstructed models predict LFV processes even without including neutrinos

$$\mathcal{L} \supset |D_\mu H|^2 + Z'_\mu J^\mu_{Z'} + \frac{1}{2} M_{Z'} Z'_\mu Z'^\mu + \mathcal{L}_Y$$

$$\frac{\text{Br}(\mu \rightarrow eee)|_{Z'}}{\text{Br}(\mu \rightarrow eee)|_\nu} \approx (10^{-2} \div 10) \times \left(\frac{\alpha_{\text{NP}}}{\alpha}\right)^2 \left(\frac{\varepsilon_e \varepsilon_\mu}{0.05^2}\right)^2 \left(\frac{\Lambda}{M_{Z'}}\right)^4$$

$$\frac{\text{Br}(\mu \text{ Al} \rightarrow e \text{ Al})|_{Z'}}{\text{Br}(\mu \text{ Al} \rightarrow e \text{ Al})|_\nu} \approx \underbrace{(10^{-1} \div 10)}_{\text{This range is only due to } \beta_i} \times \left(\frac{\alpha_{\text{NP}}}{\alpha}\right)^2 \left(\frac{\varepsilon_e \varepsilon_\mu}{0.05^2}\right)^2 \left(\frac{\Lambda}{M_{Z'}}\right)^4$$

This range is only due to β_i

Mixing between third
and light generations

Neutrino sector could dominate if $\Lambda \lesssim M_{Z'}$

Explicit Model

This model-independent study can be easily matched to any given flavour-deconstructed model of interest

As example, we refer to Model B discussed in [Greljo, Isidori, 2024]

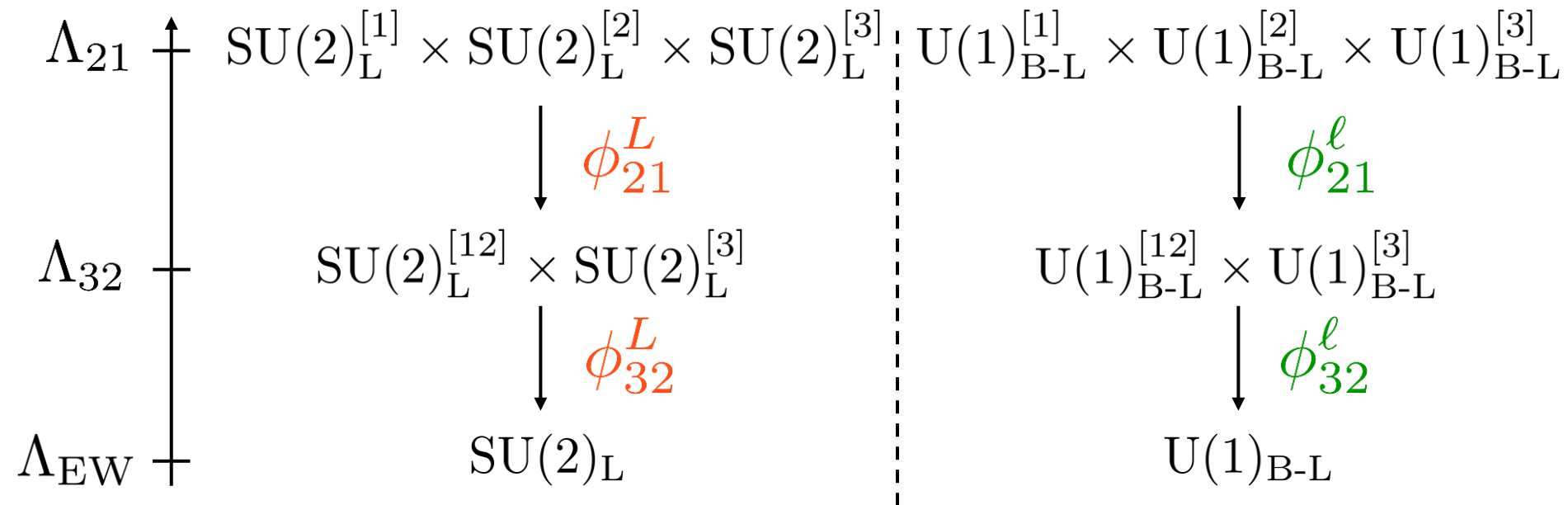
Explicit Model

This model-independent study can be easily matched to any given flavour-deconstructed model of interest

Gauge group: $SU(3)_C \times SU(2)_L^3 \times U(1)_R \times U(1)_{B-L}^3$

↙ Flavour-deconstructed ↘

To break the symmetry down to the SM gauge group we need some scalar fields



Explicit Model

This model-independent study can be easily matched to any given flavour-deconstructed model of interest

Gauge group: $SU(3)_C \times SU(2)_L^3 \times U(1)_R \times U(1)_{B-L}^3$

The Lagrangian contains all the possible EFT operators allowed by the full symmetry

$$\mathcal{L}_Y = y_{33} \bar{\ell}_3 \tilde{H} \nu_3 + \frac{c_{32}}{\Lambda_{32}} \bar{\ell}_3 \tilde{H} \phi_{32}^\ell \nu_2 + \frac{c_{23}}{\Lambda_{32}^2} \bar{\ell}_2 \tilde{H} \phi_{32}^L \phi_{32}^\ell \nu_3 + 1\text{-st generation} \quad \left. \vphantom{\mathcal{L}_Y} \right\} \rightarrow Y_\nu$$

$$\mathcal{L}_R = \tilde{c}_{i3} \bar{s}_i \chi \nu_3 + \frac{\tilde{c}_{i2}}{\Lambda_{32}} \bar{s}_i \chi \phi_{32}^\ell \nu_2 + 1\text{st generation} \quad \left. \vphantom{\mathcal{L}_R} \right\} \rightarrow M_R$$

\swarrow
 $\langle \chi \rangle \sim \Lambda$

Explicit Model

This model-independent study can be easily matched to any given flavour-deconstructed model of interest

$$\text{Gauge group: } \text{SU}(3)_C \times \text{SU}(2)_L^3 \times \text{U}(1)_R \times \text{U}(1)_{B-L}^3$$

The Lagrangian leads to the following hierarchical matrices

$$Y_\nu \sim \begin{pmatrix} \varepsilon_1 \varepsilon_2 & \varepsilon_1 \varepsilon_2 \eta_2 & \varepsilon_1 \varepsilon_2 \eta_1 \eta_2 \\ \varepsilon_1 \eta_2 & \varepsilon_1 & \varepsilon_1 \eta_1 \\ \eta_1 \eta_2 & \eta_1 & 1 \end{pmatrix} \quad M_R \sim \Lambda \begin{pmatrix} \eta_1 \eta_2 & \eta_1 & 1 \\ \eta_1 \eta_2 & \eta_1 & 1 \\ \eta_1 \eta_2 & \eta_1 & 1 \end{pmatrix}$$

$$\varepsilon_1 = \langle \phi_{32}^L \rangle / \Lambda_{32}$$

$$\varepsilon_2 = \langle \phi_{21}^L \rangle / \Lambda_{21}$$

$$\eta_1 = \langle \phi_{32}^\ell \rangle / \Lambda_{32}$$

$$\eta_2 = \langle \phi_{21}^\ell \rangle / \Lambda_{21}$$

Explicit Model

This model-independent study can be easily matched to any given flavour-deconstructed model of interest

Gauge group: $SU(3)_C \times SU(2)_L^3 \times U(1)_R \times U(1)_{B-L}^3$

The Lagrangian leads to the following hierarchical matrices

$$Y_\nu \sim \begin{pmatrix} \varepsilon_1 \varepsilon_2 & \varepsilon_1 \varepsilon_2 \eta_2 & \varepsilon_1 \varepsilon_2 \eta_1 \eta_2 \\ \varepsilon_1 \eta_2 & \varepsilon_1 & \varepsilon_1 \eta_1 \\ \eta_1 \eta_2 & \eta_1 & 1 \end{pmatrix} \quad M_R \sim \Lambda \begin{pmatrix} \eta_1 \eta_2 & \eta_1 & 1 \\ \eta_1 \eta_2 & \eta_1 & 1 \\ \eta_1 \eta_2 & \eta_1 & 1 \end{pmatrix}$$

$$\varepsilon_1 = \langle \phi_{32}^L \rangle / \Lambda_{32}$$

$$\varepsilon_2 = \langle \phi_{21}^L \rangle / \Lambda_{21}$$

$$\eta_1 = \langle \phi_{32}^\ell \rangle / \Lambda_{32}$$

$$\eta_2 = \langle \phi_{21}^\ell \rangle / \Lambda_{21}$$

We have the freedom to
require Normal Ordering

$$\Delta_1 \lesssim 1 \quad \Delta_2 \lesssim 1$$

$$\implies \Lambda \gtrsim \text{few TeV}$$

Conclusions

In this work we have considered the leading phenomenological implications of neutrino anarchy in flavour deconstruction [Greljo, Isidori, 2024]

- We have shown that Normal Ordering allows for the NP scale Λ to be lower with respect to Inverted Ordering
- The contribution to LFV processes coming from the neutrino sector can be dominant over the Gauge and Yukawa sectors
- In some cases the NP scale Λ can be as low as few TeV and can be probed by near future experiments, such as Mu3e and COMET