

LEVERHULME
TRUST



String Axions & Associated Relics

Nicole Righi

Based on

[2110.02964] with Cicoli, Guidetti and Westphal

[2411.18496] with Leedom, Putti and Westphal

[2412.12012] with Sheridan, Carta, Gendler, Jain, Marsh,
McAllister, Rogers and Schachner

PLANCK 25, 27/05/25

AXIONS IN THE UNIVERSE

- Axions are a common product of string theory
- Their presence could affect the cosmological history
- We want to draw statistical features by studying the largest known ensemble of EFTs

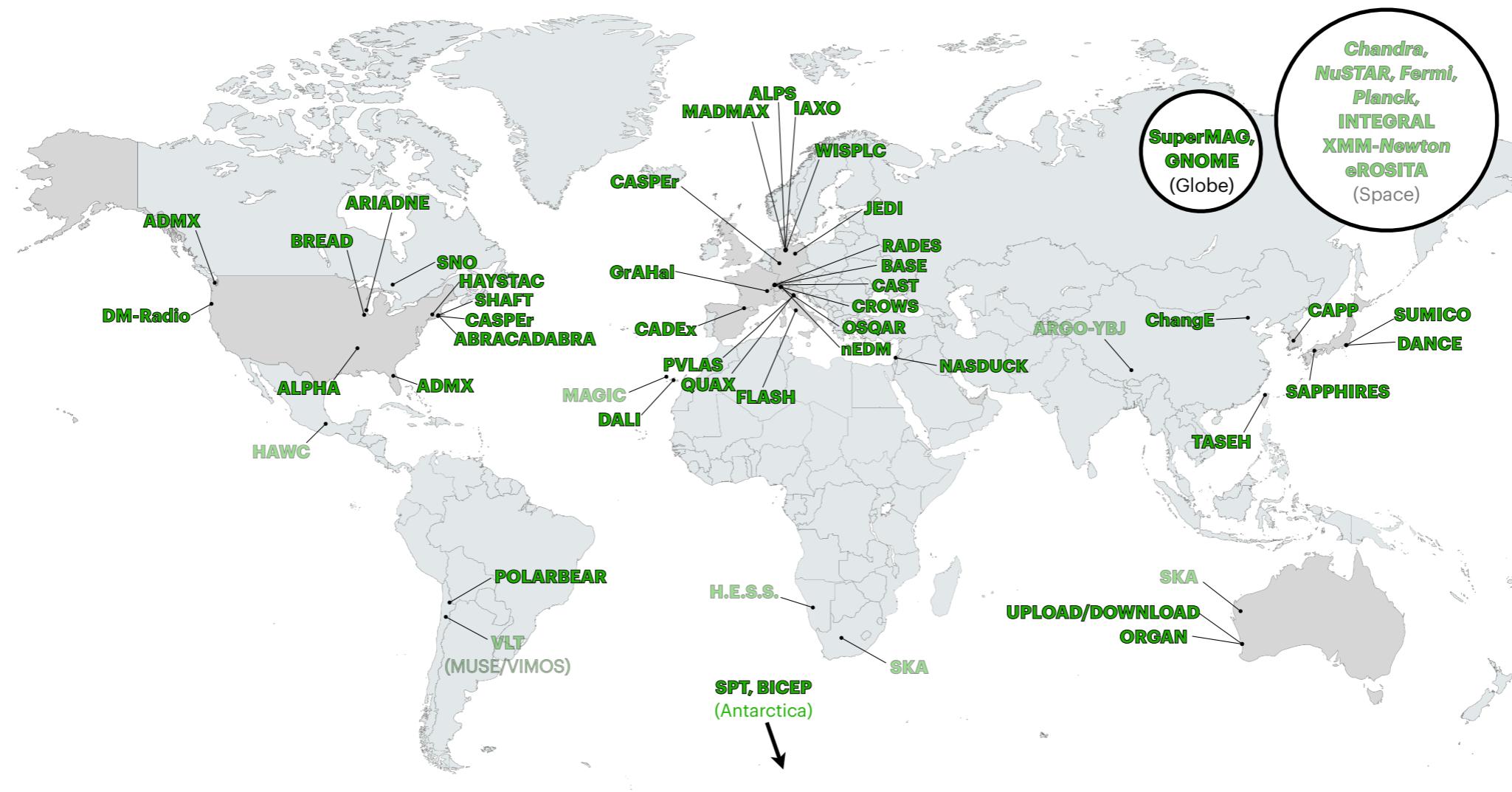
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The string axiverse can be realised in our universe and *detected*,
but at a **price**

THE SEARCH FOR AXIONS

1) Great experimental effort \Rightarrow great opportunity

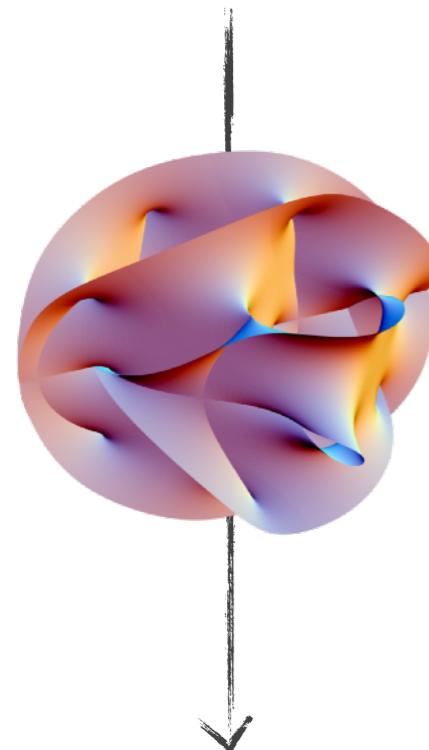


[O'Hare Website AxionLimits]

THE SEARCH FOR AXIONS

2) Axions arise naturally in string theory

10d superstring theory

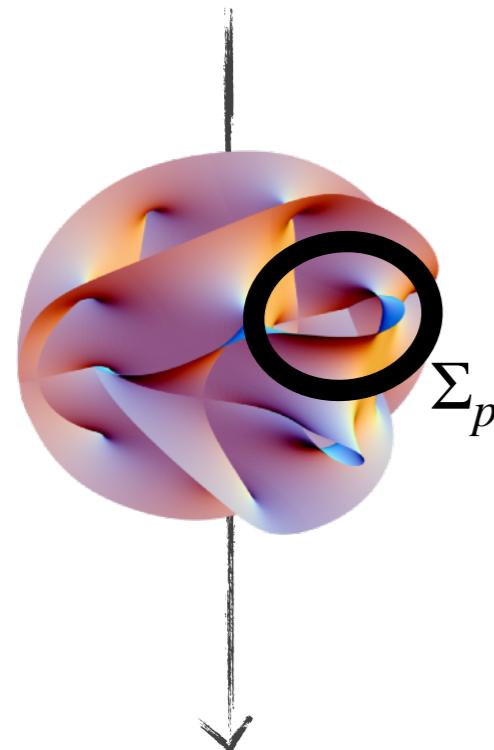


4d EFT

THE SEARCH FOR AXIONS

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10d superstring theory



$$S_{10D} \supset \int_{\mathcal{M}_{9,1}} dC_p \wedge \star dC_p$$

$$\int_{\Sigma_p} C_p \equiv \theta(x)$$

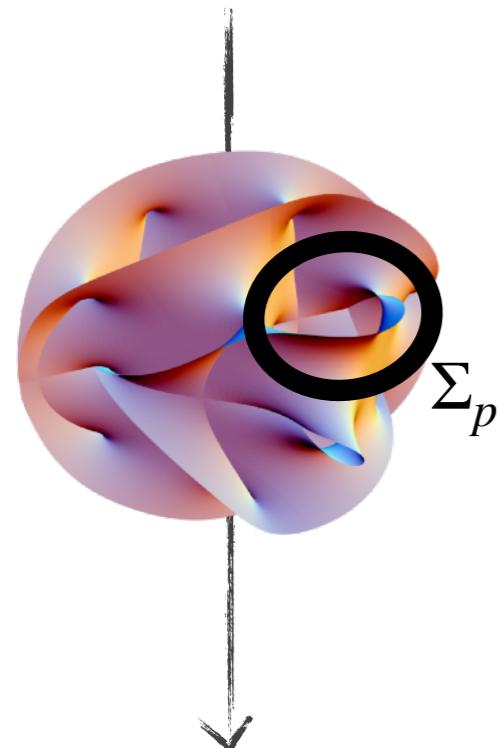
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$$S_{EFT} \supset - \int_{\mathcal{M}_{3,1}} d^4x \frac{f^2}{2} (\partial\theta(x))^2$$

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10d superstring theory



$$S_{10D} \supset \int_{\mathcal{M}_{9,1}} dC_p \wedge \star dC_p$$

$$C_p \rightarrow C_p + 2\pi \sum_i n_i \omega_p^i$$

4d EFT

$$S_{EFT} \supset - \int_{\mathcal{M}_{3,1}} d^4x \frac{f^2}{2} (\partial\theta(x))^2$$

$$\theta(x) \rightarrow \theta(x) + 2\pi n$$

$$\int_{\Sigma_p} C_p \equiv \theta(x)$$

$$\int_{\Sigma_p^i} \omega_p^j = 2\pi \delta_j^i$$

⇒ string axions are pre-inflationary

THE SEARCH FOR AXIONS

3) Axion physics is sensible to UV input

$$\mathcal{L}_{\text{EFT}} \supset -\frac{1}{2} K_{ij} \partial_\mu \theta^i \partial^\mu \theta^j + \frac{Q_{\text{QCD}}^i \theta_i}{32\pi^2} G \wedge G + \sum_{\alpha} \Lambda_\alpha^4 (1 - \cos(2\pi Q_\alpha^i \theta_i))$$

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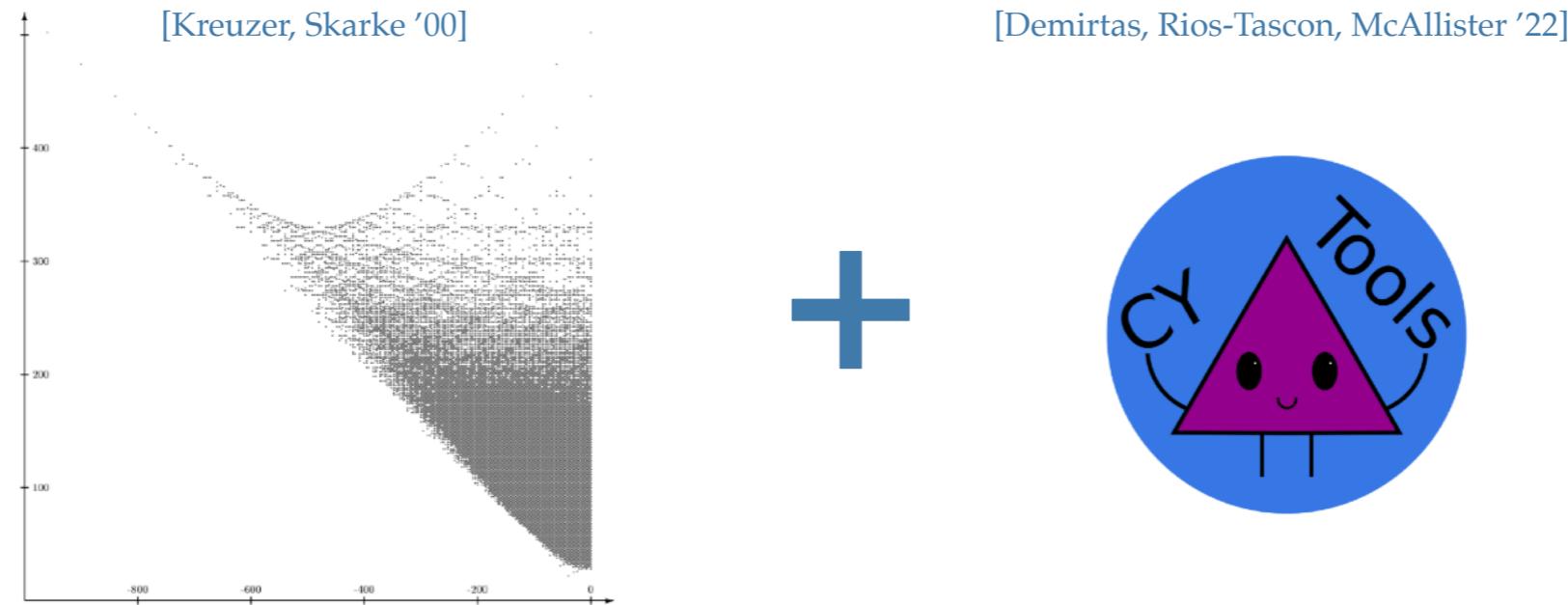
Q_α^i = instanton charges

$\Lambda_\alpha^4 \sim e^{-\text{vol}(\Sigma_4^\alpha)}$ = instanton scales

geometric quantities
can be computed in
(a subset of) the landscape

THE STRING AXION LANDSCAPE

The subset we focus on:



- which means:
- work with a *stringy* axion from C_4 potentials
 - scan over $\lesssim 10^{428}$ Calabi-Yau manifolds
 - work with concrete geometric data
 - use optimization methods

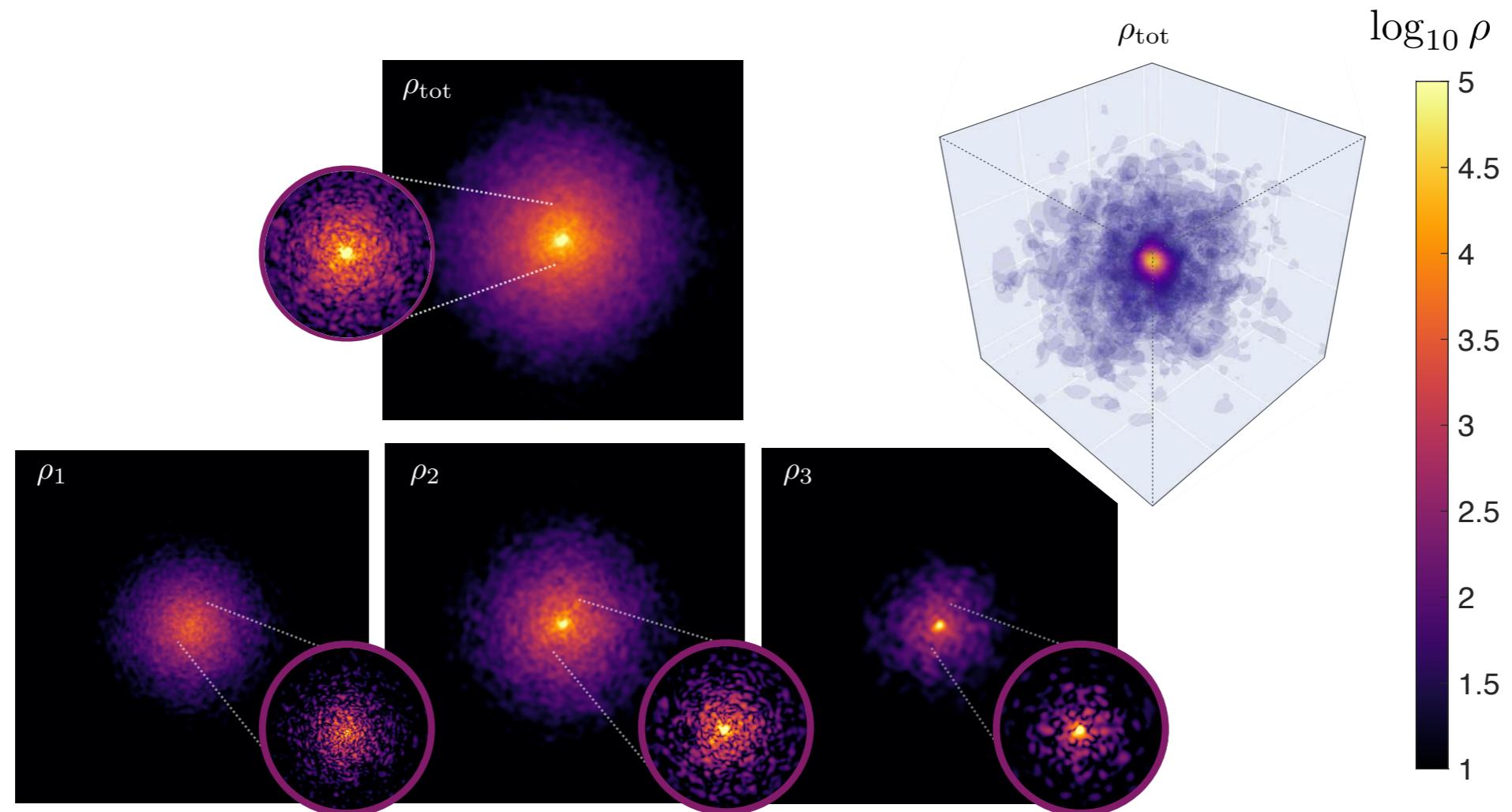
We leave behind: axions from other 10D elements, full SM implementation, positive Λ , etc...

— see **Margherita Putti's** parallel this afternoon —

STRING AXIONS AS DARK MATTER

Let us test the string axiverse:

Can we accomodate Fuzzy Dark Matter in string theory?



[Sheridan, Carta, Gendler, Jain, Marsh, McAllister, NR, Rogers, Schachner '24]

STRING AXIONS AS DARK MATTER

Generate EFTs such that

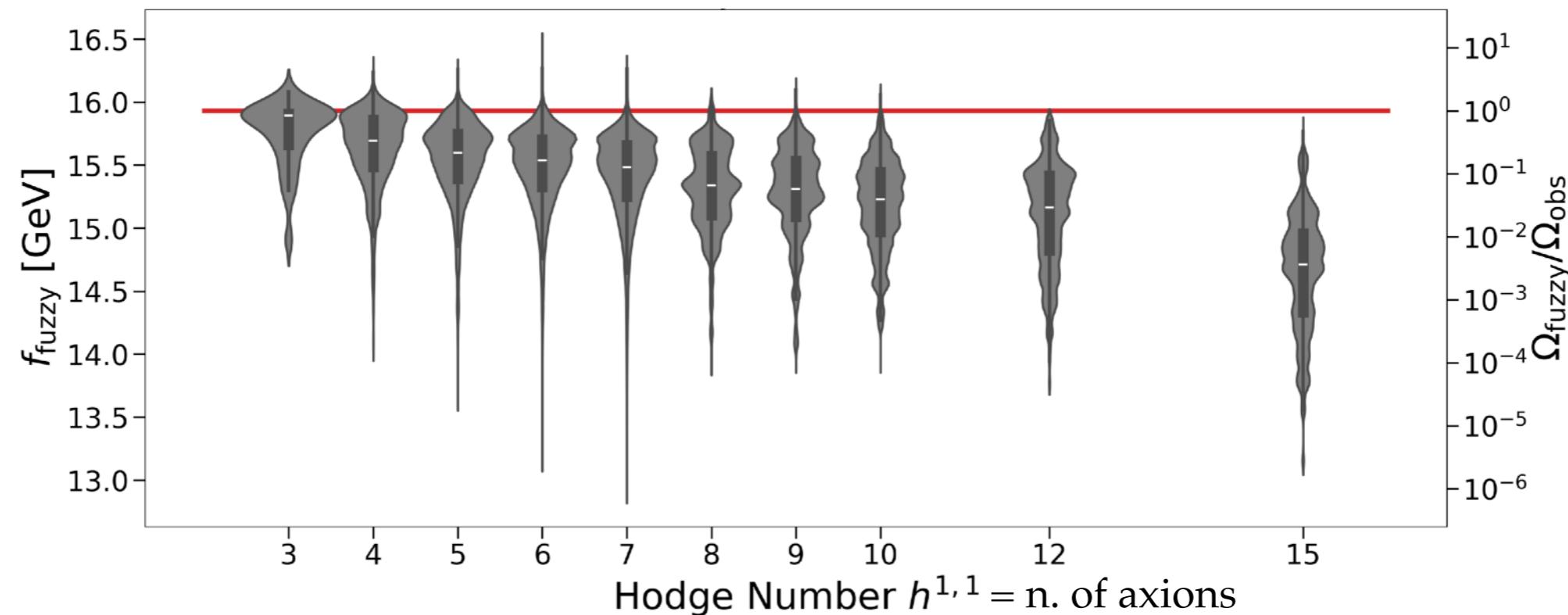
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STRING AXIONS AS DARK MATTER

Generate EFTs such that

- $f_{fuzzy} \gtrsim 10^{16} \text{ GeV} \Rightarrow$ focus on $2 \leq \text{axions} \leq 7$

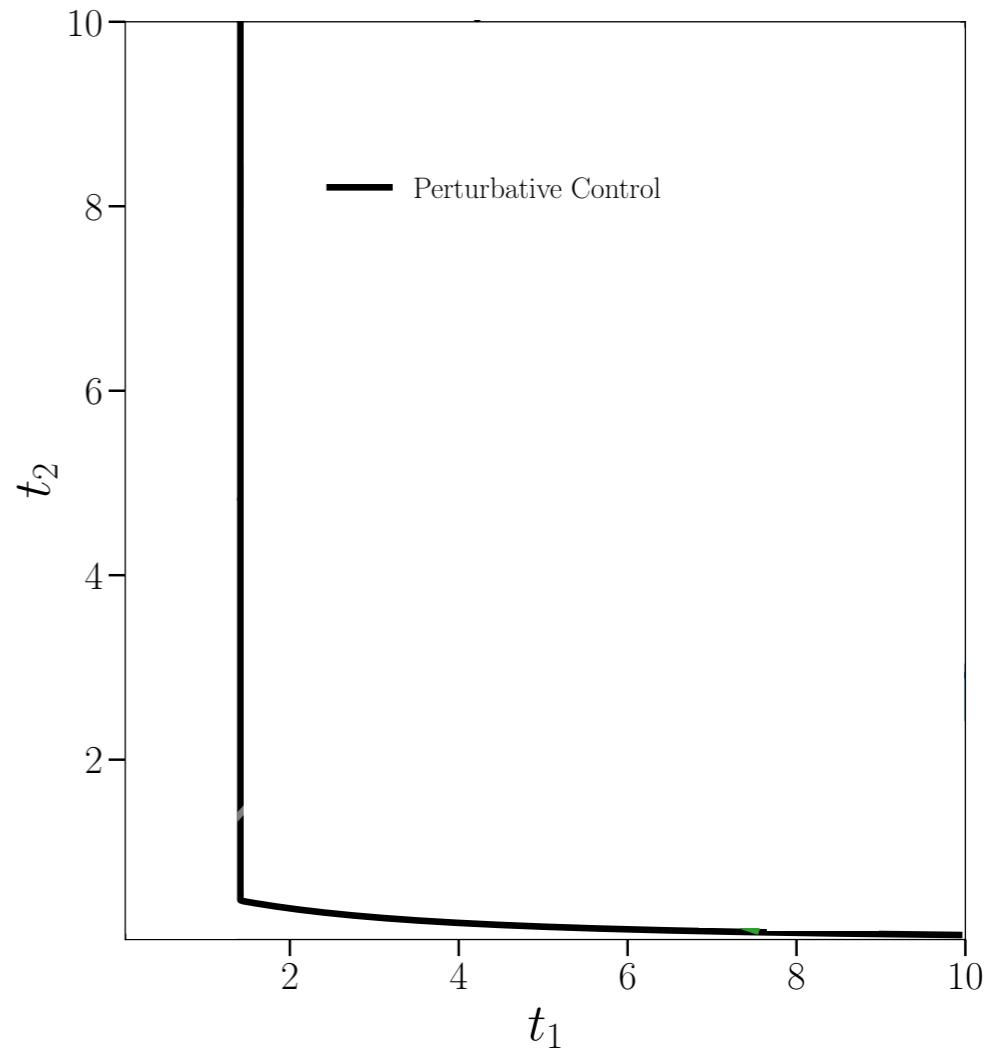
mean f decreases with the number of axions



STRING AXIONS AS DARK MATTER

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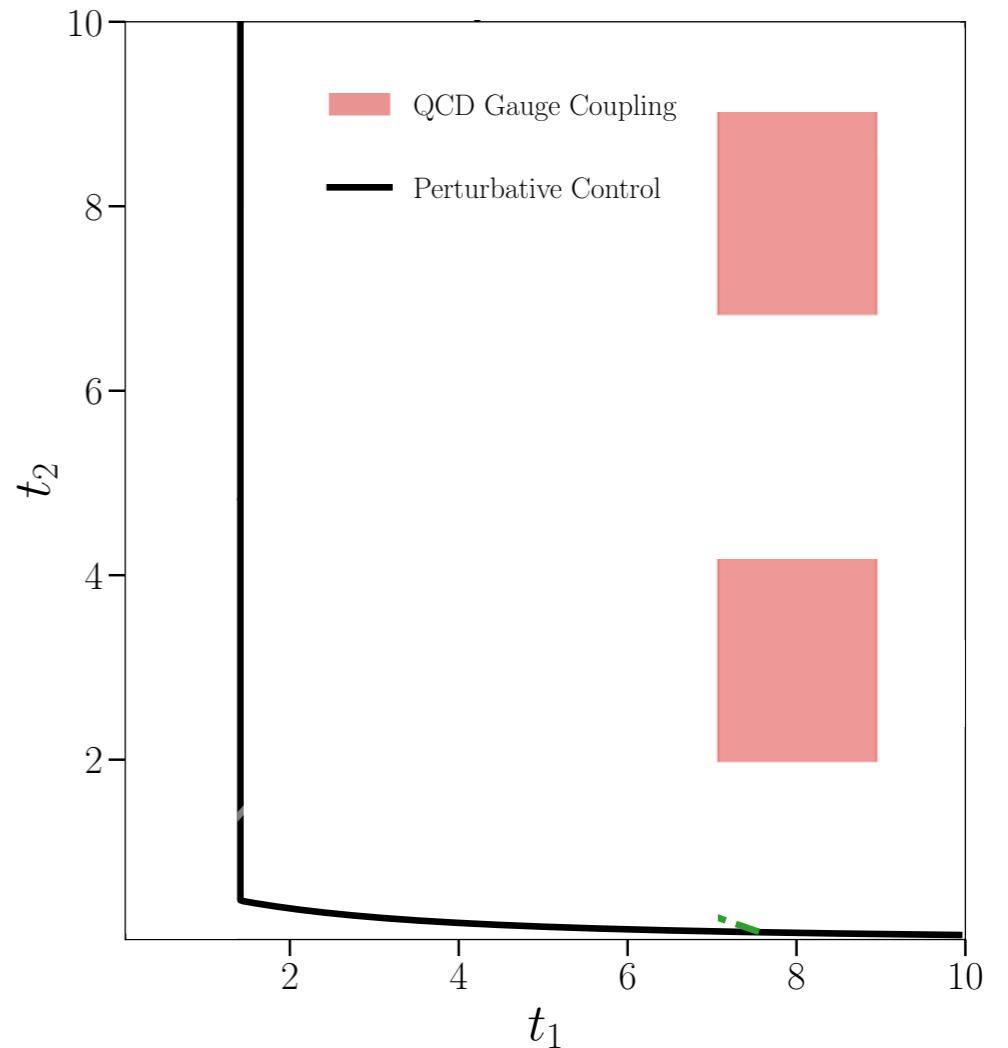
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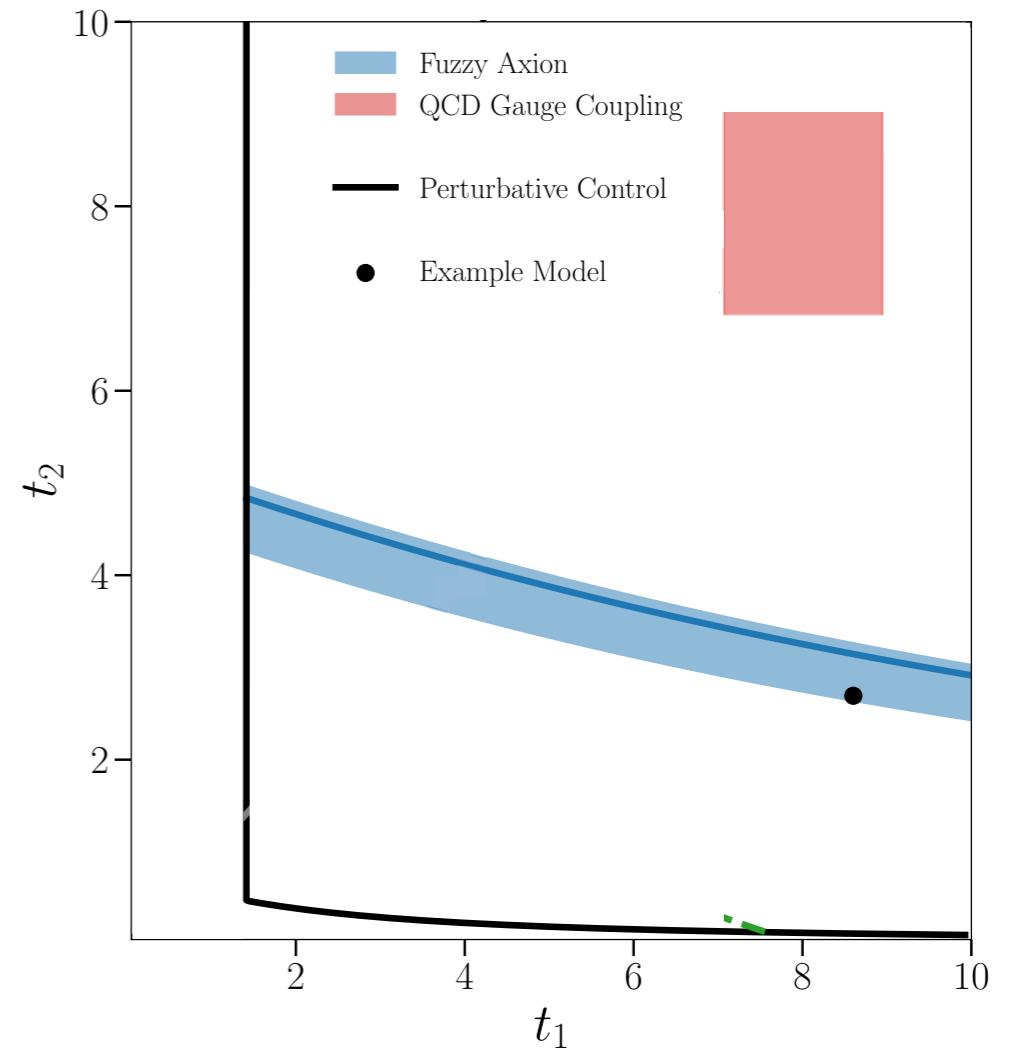
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$$m_{QCD} \sim 10^{-9} \text{ eV}$$

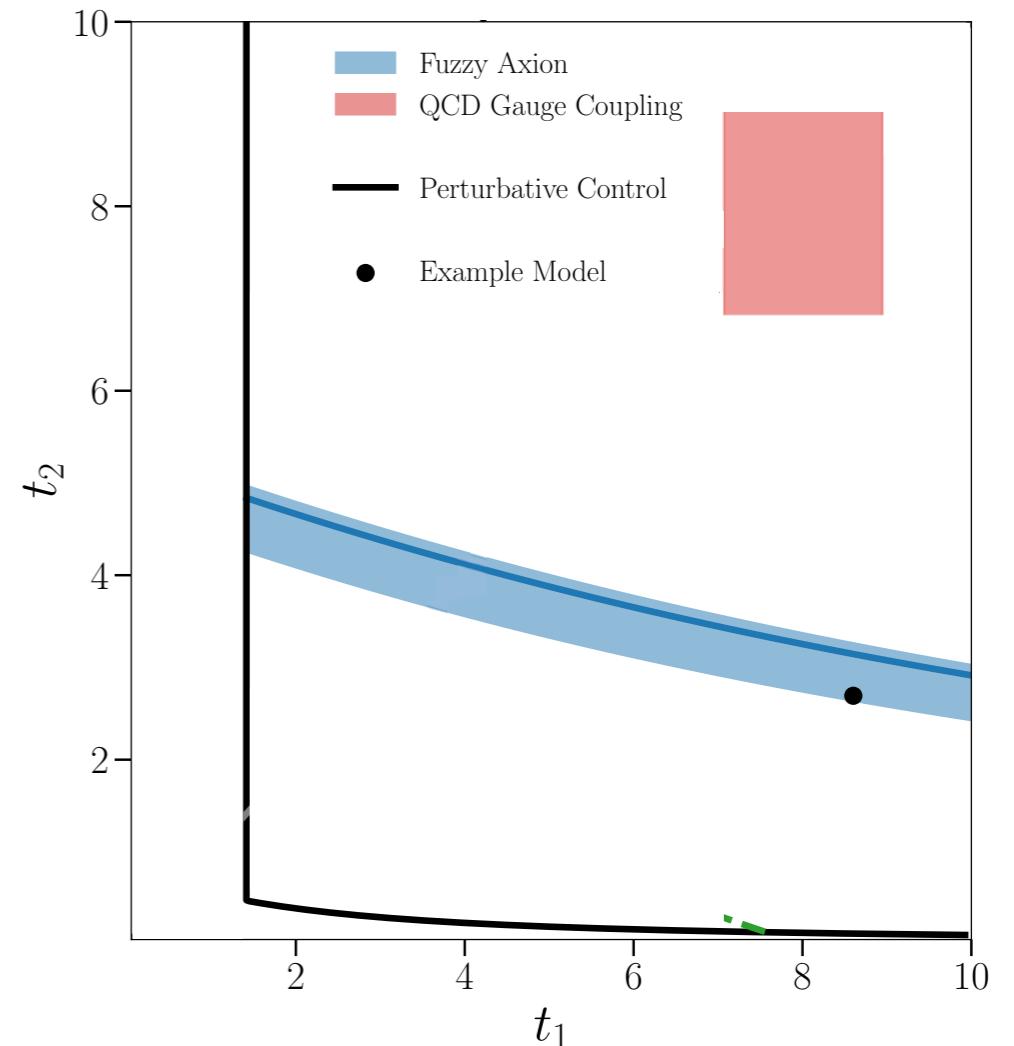
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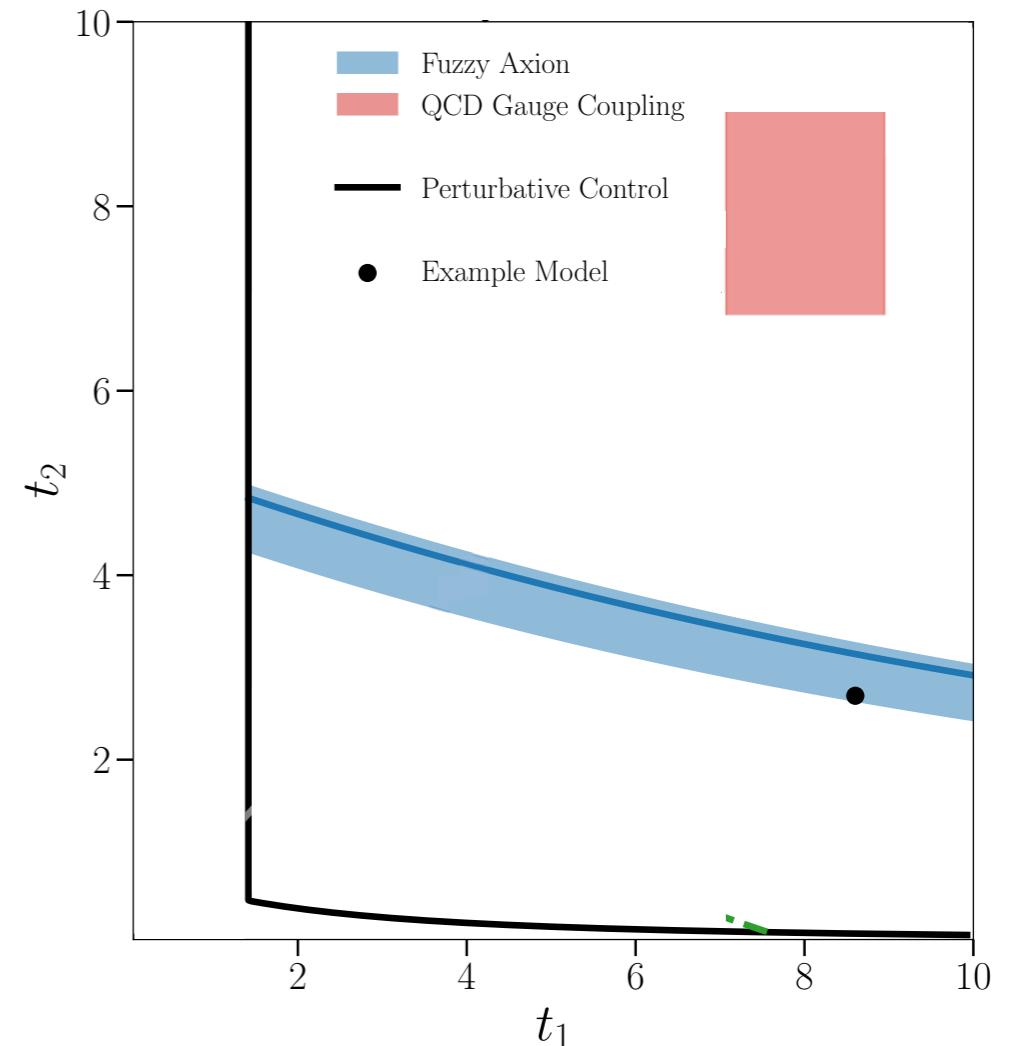
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in general, things are not that clean!

STRING AXIONS AND RELICS

Relic 1: AXIONS

$$\Omega_a h^2 \sim f_a^2 \theta_0^2 \sqrt{m_a}$$

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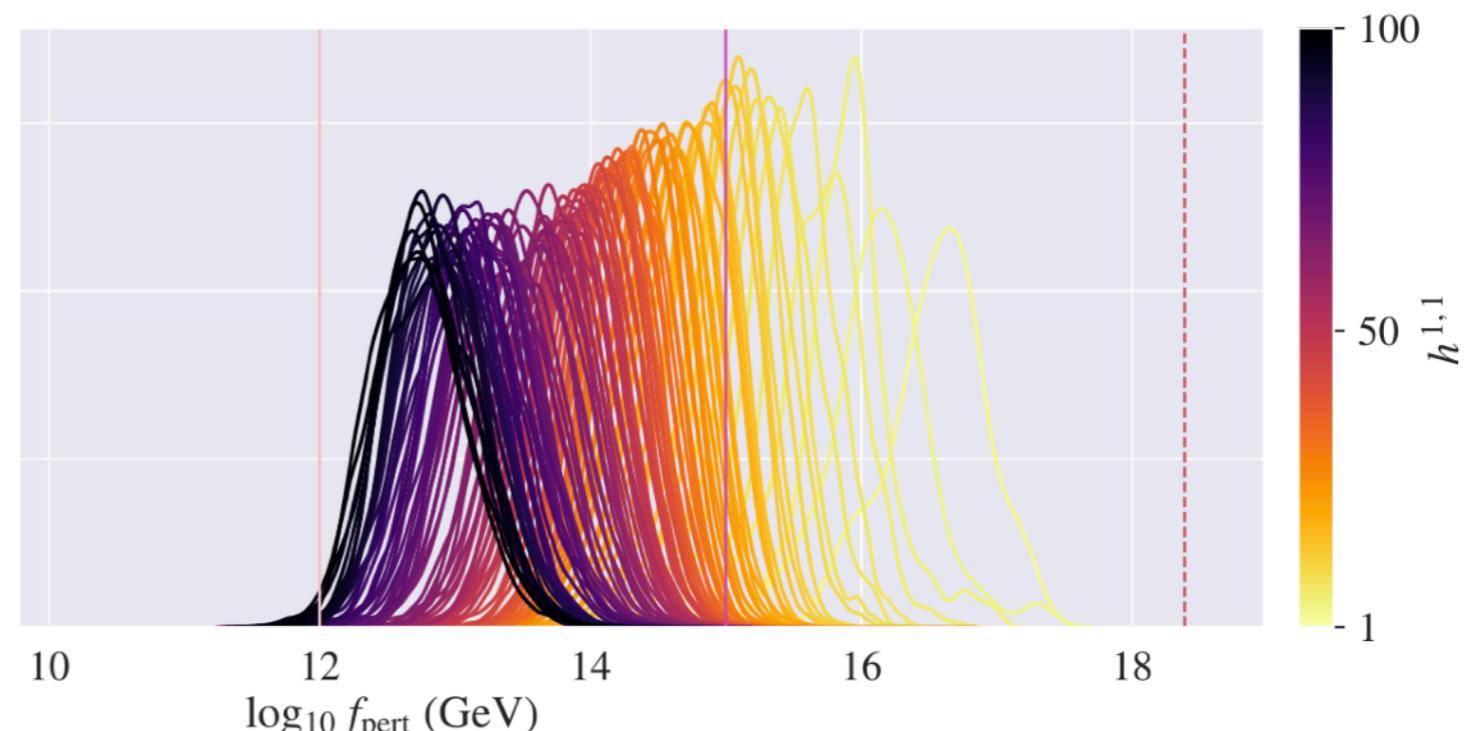
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$$\Omega_{a,\text{total}} h^2 = \Omega_{\text{QCD}} h^2 + \sum_i \Omega_i h^2 \Big|_m + \sum_j \Omega_j h^2 \Big|_r + \sum_k \Omega_k h^2 \Big|_{w_R} \leq \Omega_{\text{DM}} h^2 \approx 0.12$$

typical distributions:

- masses log flat
- decay constants clustered



[Mehta, Demirtas, Long, Marsh, McAllister, Stott '21]



WARNING
OVERCLOSURE



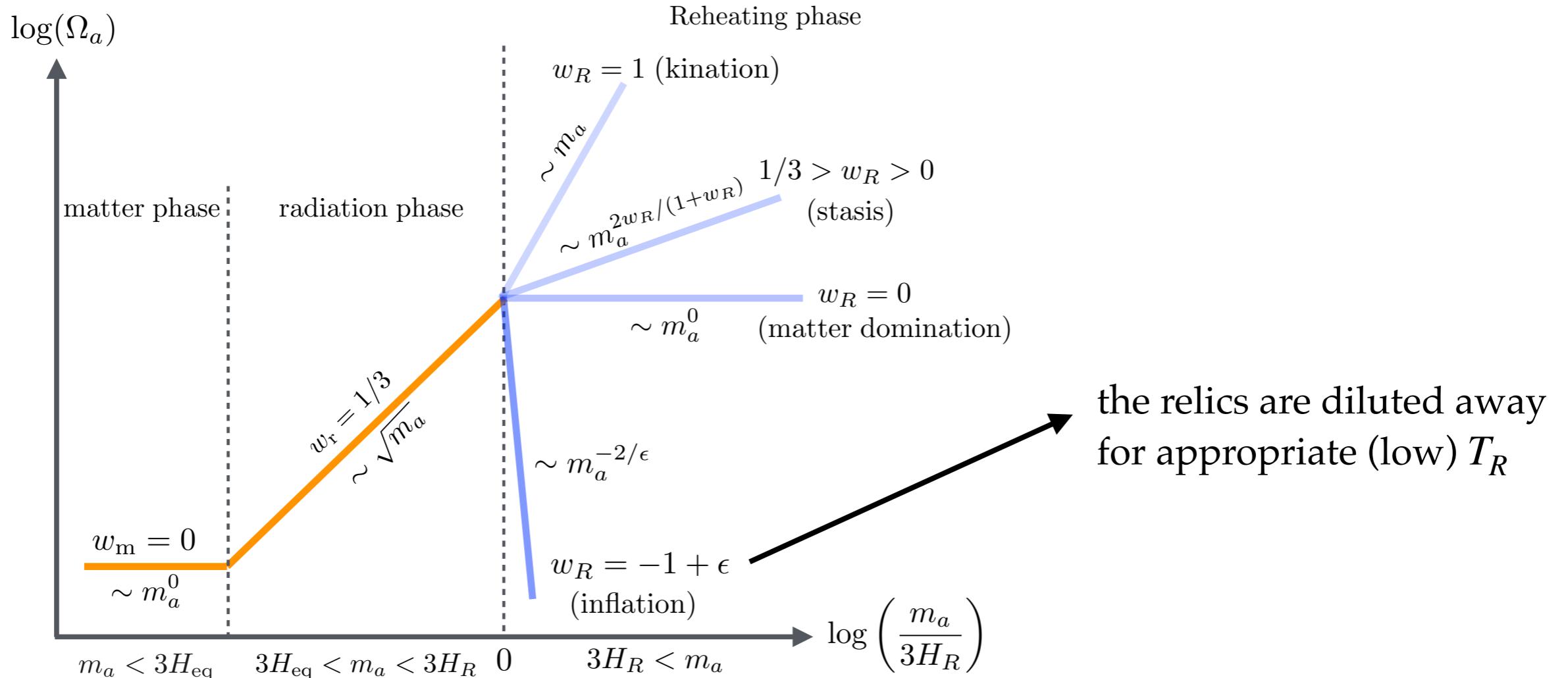
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- Dilution



STRING AXIONS AND RELICS

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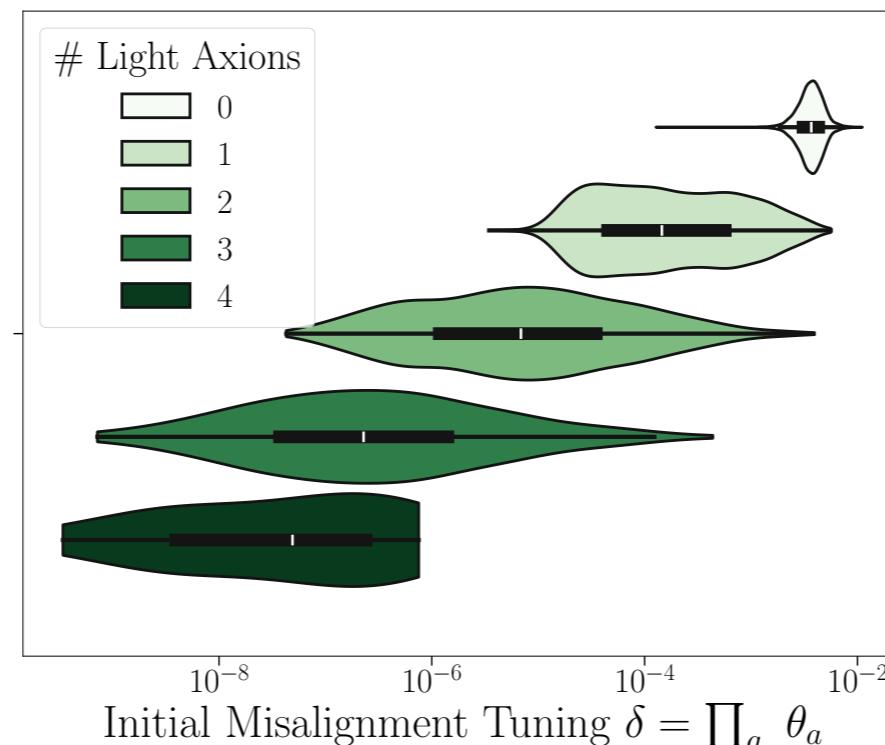
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- Initial misalignment



$$\Omega_{a,\text{total}} h^2 = \Omega_{\text{QCD}}(\theta_0) h^2 + \sum_i \Omega_i(\theta_0) h^2 \Big|_{\text{m}} + \sum_j \Omega_j(\theta_0) h^2 \Big|_{\text{r}} + \sum_k \Omega_k(\theta_0) h^2 \Big|_{w_R} \leq \Omega_{\text{DM}} h^2 \approx 0.12$$



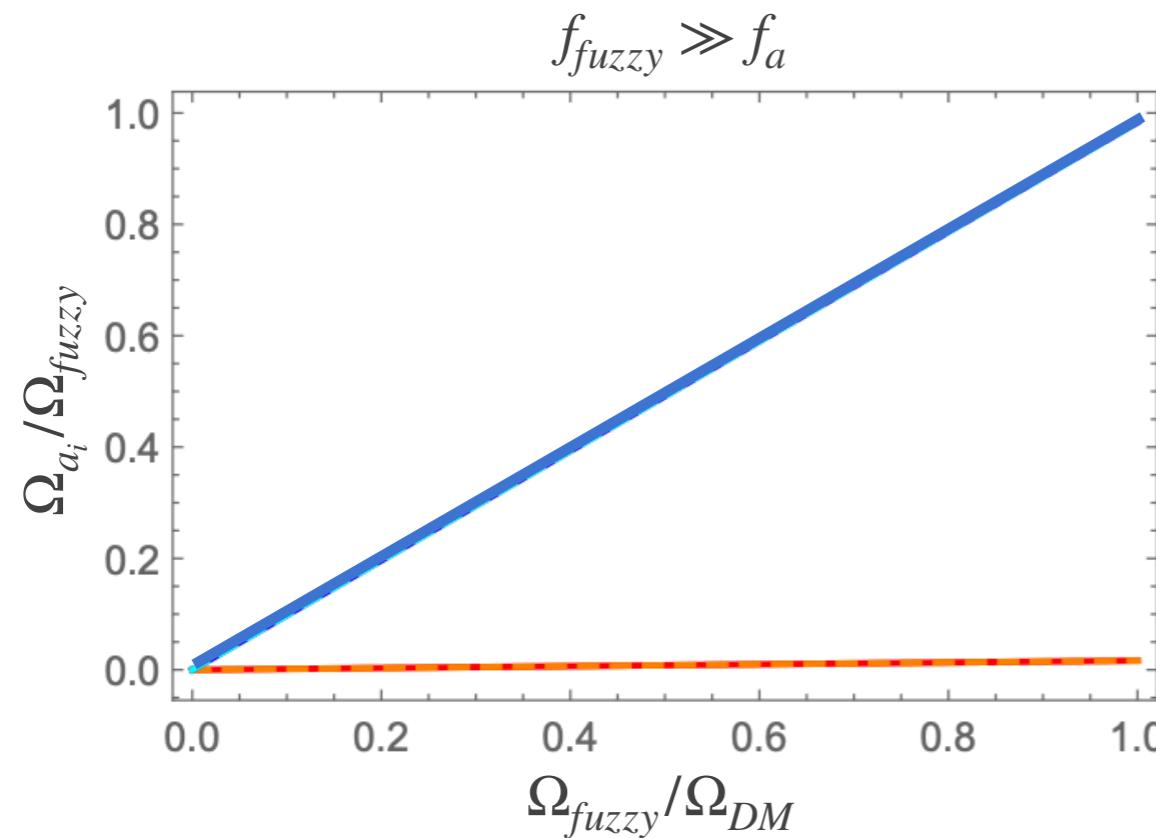
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- Small decay constants: $f_{\text{fuzzy}} \gg f_{\text{others}}$



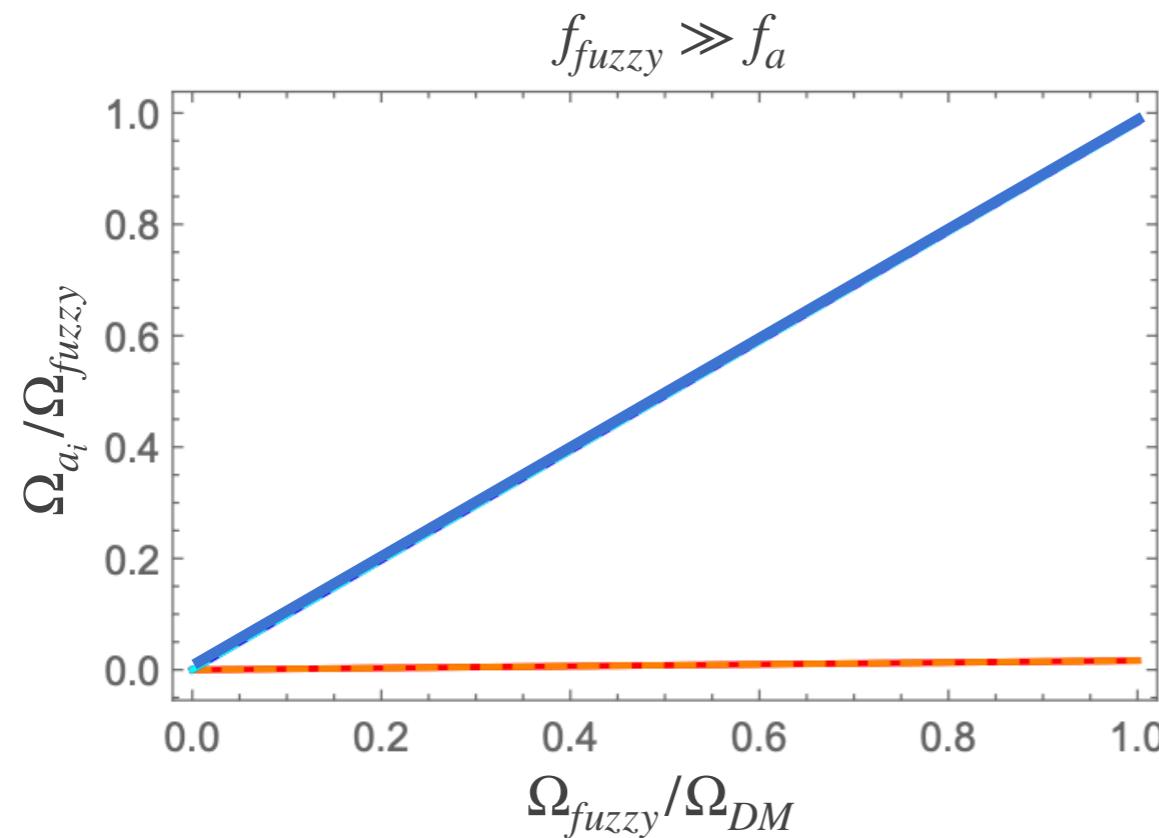
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not generic!

$$f_{\text{fuzzy}} \sim 10^7 f_{\text{QCD}}$$



$$\det(K) \Big|_{\text{fuzzy}} \sim 10^{-14} \det(K) \Big|_{\text{QCD}}$$

K metric on moduli space

STRING AXIONS AND RELICS

Relic 2: Moduli

4D $\mathcal{N} = 1$ chiral multiplet: $T_i = \text{vol}(\Sigma_4^i) + i\theta_i \Rightarrow$ at least as many moduli as axions!
must be stabilised at the right scale

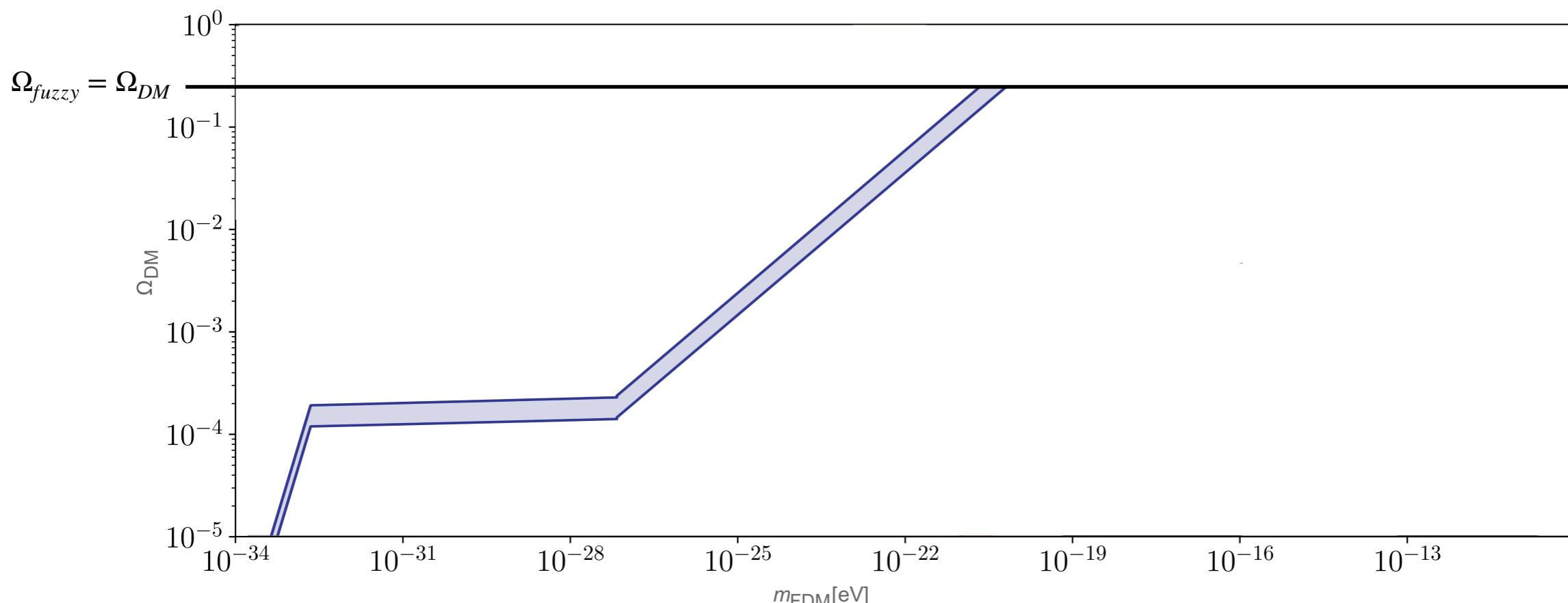
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1) Implement moduli stabilisation properly [Cicoli, Guidetti, NR, Westphal '21]

ensure $\langle \text{moduli} \rangle$, then compute axions EFT



STRING AXIONS AND RELICS

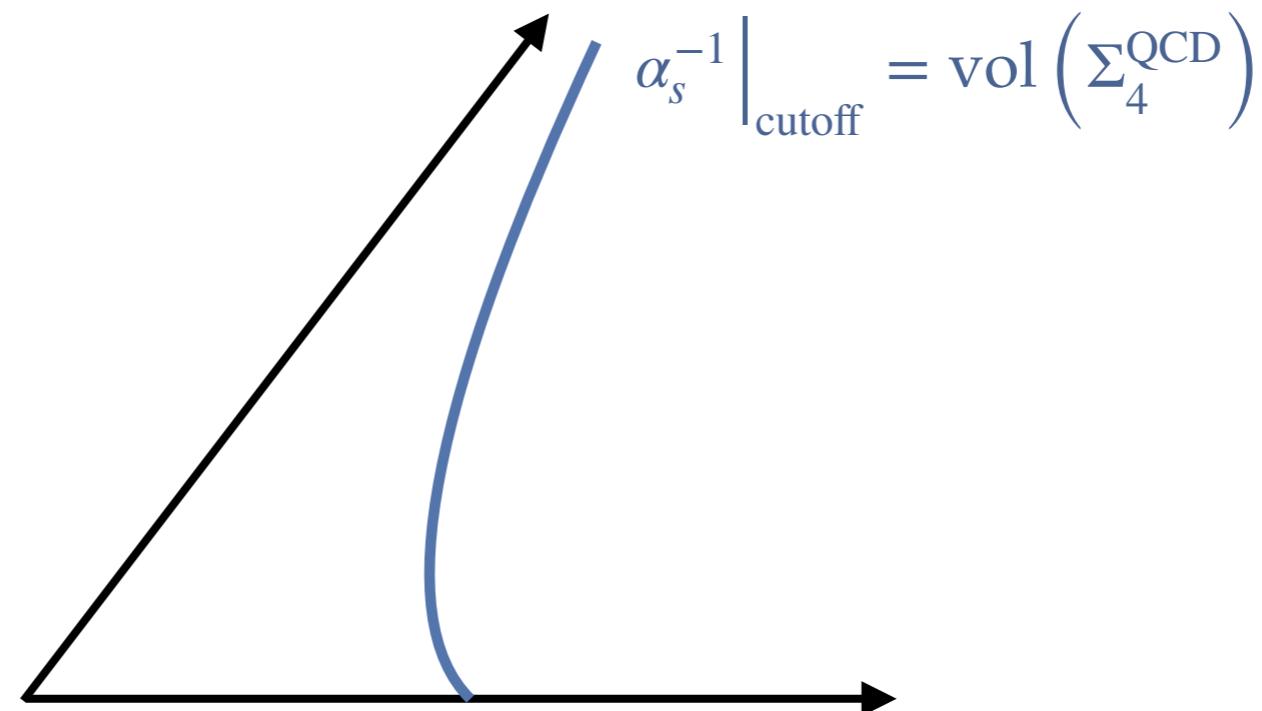
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2) Assume moduli are stabilised properly

[Sheridan, Carta, Gendler, Jain, Marsh, McAllister, NR, Rogers, Schachner '24]

$$M_{\text{moduli}} > \Lambda_{\text{EFT}}$$



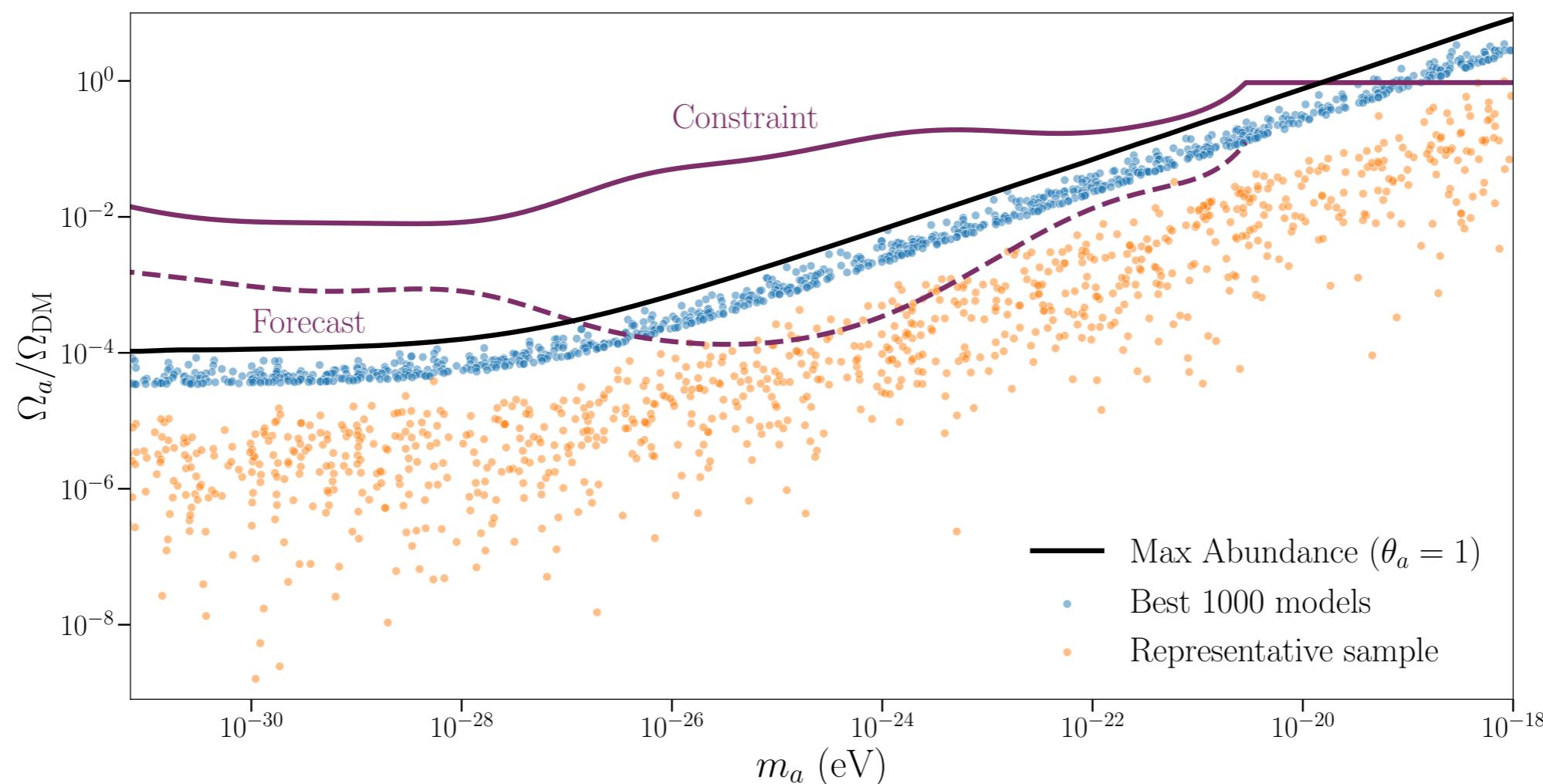
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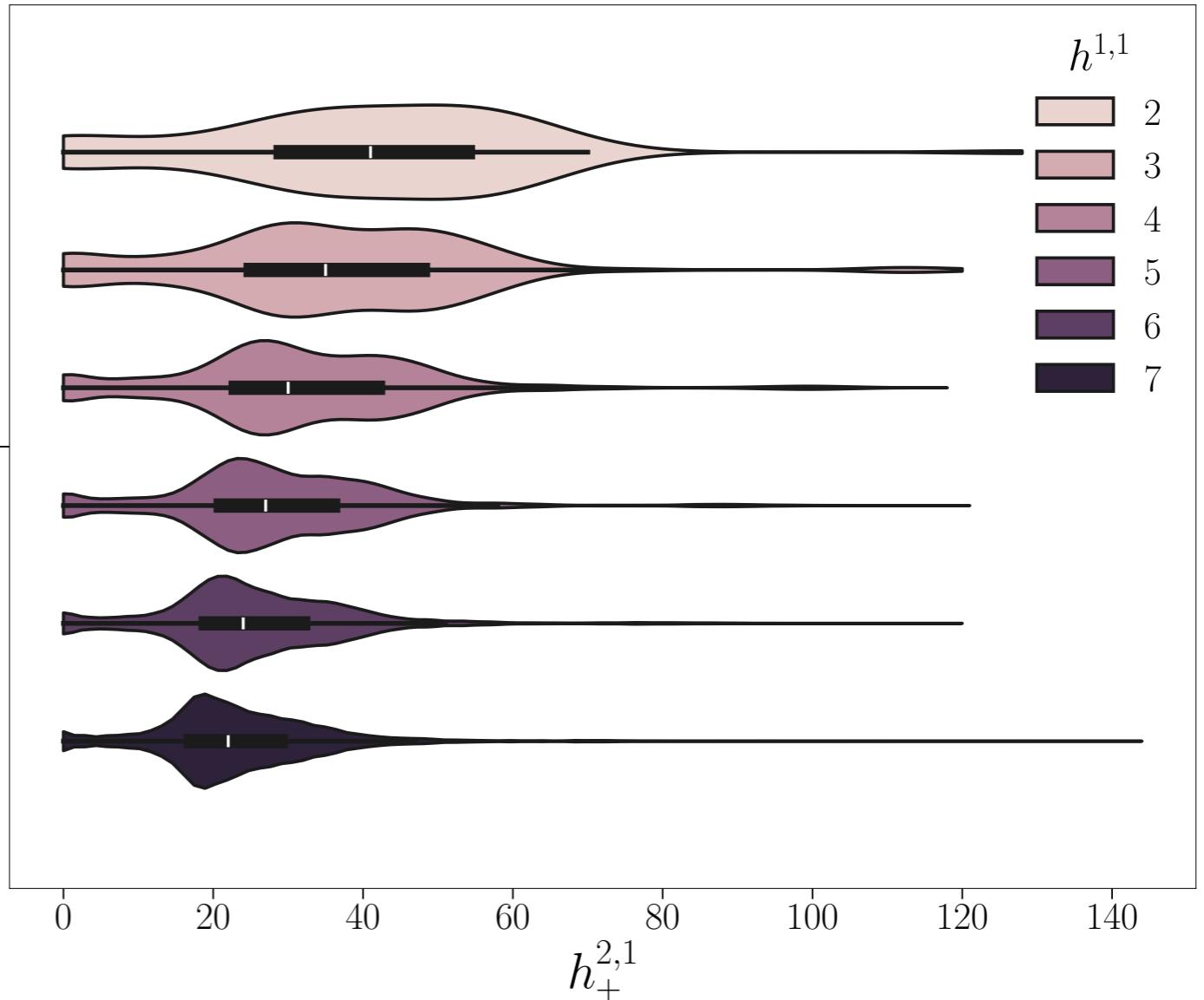
STRING AXIONS AND RELICS

Relic 3: Dark U(1) gauge fields

using [Moritz '23]

$h_+^{2,1} \neq 0$ in $\sim 95\%$ of orientifolds

$$C_4 = \theta_i \omega_4^i + \textcolor{blue}{V^a} \wedge \alpha_a$$



HEAVY STRING AXIONS FORM INFLATION

String axions are naturally light: $m_a^2 \sim e^{-\text{vol}(\Sigma_4)}$

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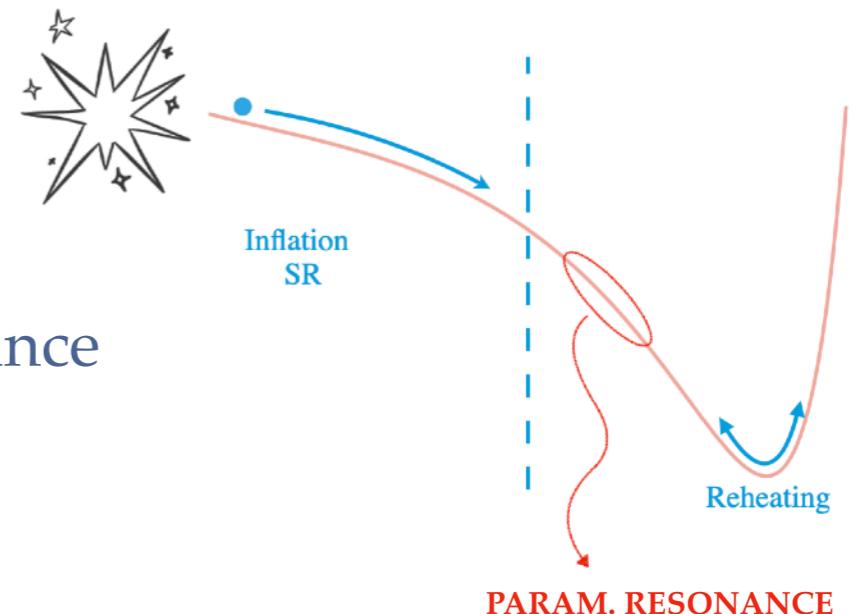
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A dynamical process can change this: parametric resonance

$$\text{inflaton: } \phi \simeq \langle \phi \rangle + \Delta\phi t^{-1} \cos(m_\phi t)$$

$$\text{axion: } \theta(t, \vec{x}) \simeq \langle \theta \rangle + \theta_k(t, \vec{x})$$



$$\ddot{\theta}_k + \left(3H - \frac{\partial K_{T\bar{T}}}{K_{T\bar{T}}} \right) \dot{\theta}_k + \left(\frac{k^2}{a^2} + \frac{\partial^2 V}{\partial \theta_k^2} \right) \theta_k = 0$$

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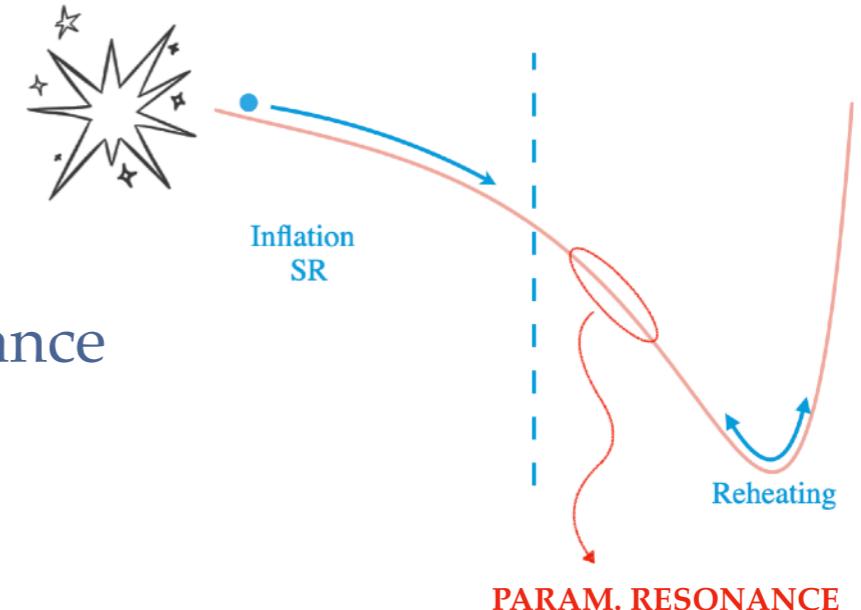
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[Leedom, Putti, NR, Westphal '24]

RELICS FROM HEAVY AXIONS

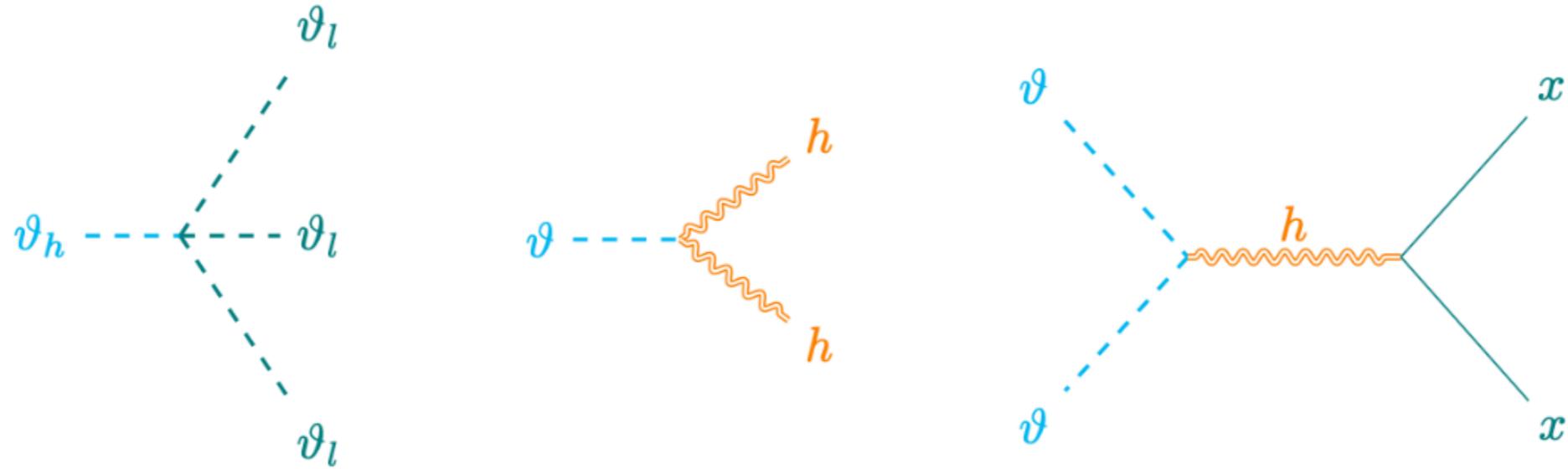
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$m_{\theta,\text{eff}}^2$

- $\mathcal{L}_{kin} > V \Rightarrow$ production of axions, $m_{\theta,\text{eff}} \lesssim 10^{-28} \text{ eV} \Rightarrow$ contribution to $\Delta N_{eff} \lesssim 10^{-6}$
- $\mathcal{L}_{kin} < V \Rightarrow$ production of axions, $m_{\theta,\text{eff}} \sim m_\phi \Rightarrow$ During radiation domination redshift slower than radiation, might lead to overclosure
↓
must decay efficiently

[Leedom, Putti, NR, Westphal '24]

RELICS FROM HEAVY AXIONS



If axion is heavy ($m_\theta \sim H_I$), it can decay into

1. Massless gauge bosons
2. Gravitons
3. SM — MSSM Higgs doublet
4. Lighter axions
5. Condensing gauge group

CONCLUSIONS

The string axiverse can be realised in our universe and *detected*, but at a price:

- Presence of a number of relics: moduli, dark photons, decay products...
- Introduction of non-standard cosmology: low T_R
- Tuning of the geometry

String theory p.o.v. is different from pure EFT, e.g. high quality and couplings

Axion detection could inform us about our place in the landscape.

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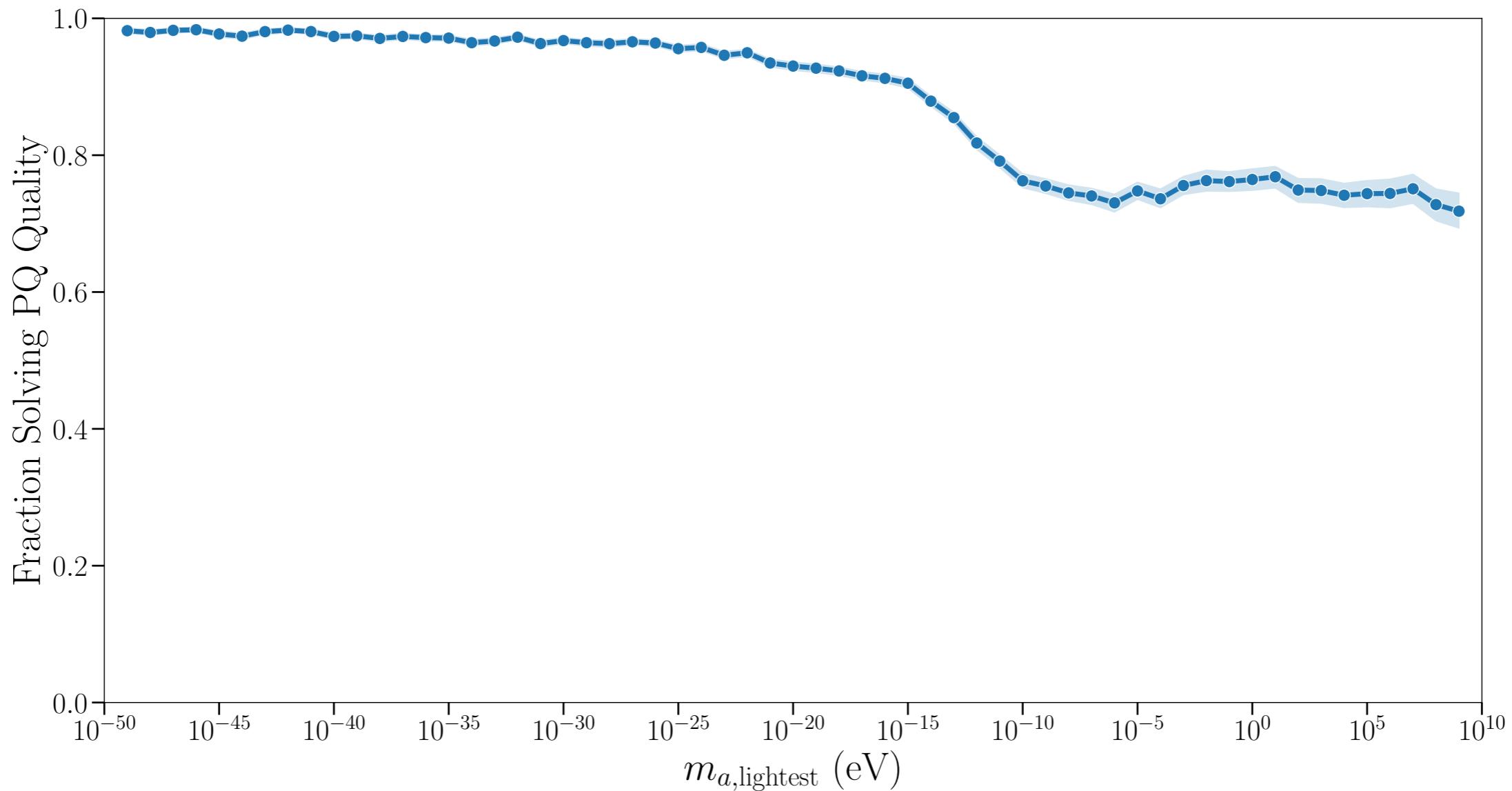
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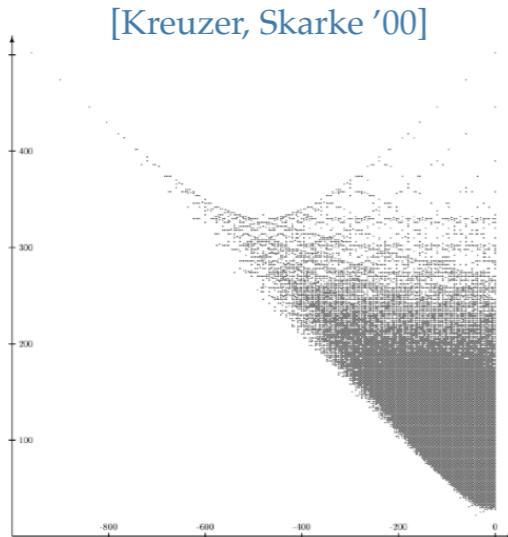
Thank you

BACKUP: PQ QUALITY

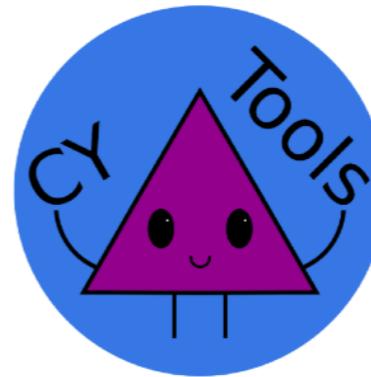
$$\Lambda_{\text{PQ}}^4 < \Lambda_{\text{lightest axion}}^4 \leq \Lambda_{\text{fuzzy}}^4 \quad \Rightarrow \quad \frac{\Lambda_{\text{PQ}}^4}{\Lambda_{\text{QCD}}^4} \lesssim 10^{-10} \Leftrightarrow \frac{m_{\text{lightest axion}}}{m_{\text{QCD}}} \lesssim 10^{-5}$$



BACKUP: HOW TO APPROACH THE LANDSCAPE



[Demirtas, Rios-Tascon, McAllister '22]



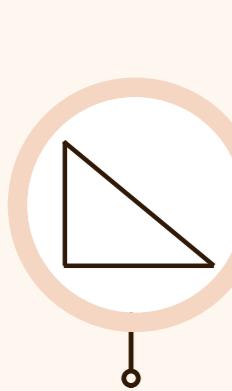
Choose a Fine, Regular, and Star triangulation of the polytope

Break the supersymmetry to N=1 by involuting the Calabi-Yau manifold and the string spectrum

Choose a point in the Kähler moduli space at which the Standard Model gauge couplings match IR expectations

Use the now fully-specified data of the Kähler potential and superpotential to compute axion masses and decay constants

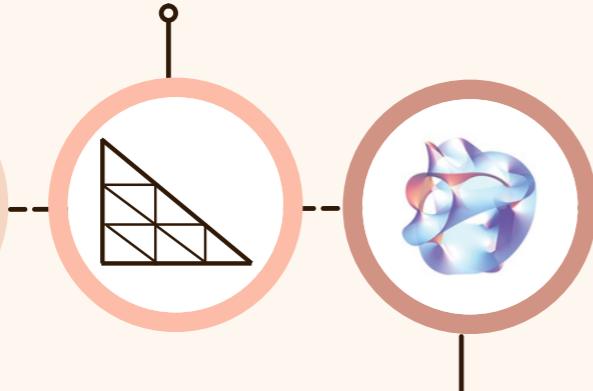
Triangulate the polytope



Choose a polytope

A 4d reflexive polytope from the Kreuzer-Skarke database

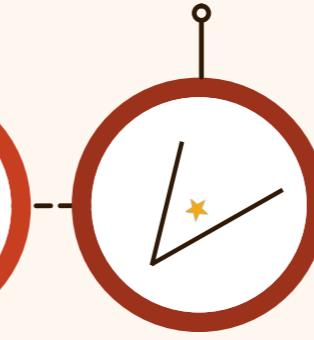
Choose an orientifold projection



Construct a Calabi-Yau threefold

Take the anti-canonical hypersurface in the toric variety defined by the triangulation

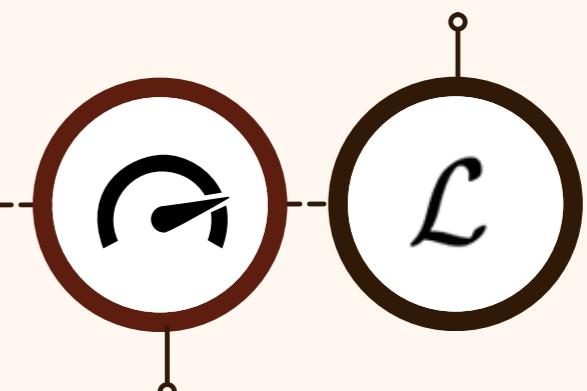
Fix the Calabi-Yau moduli



Choose a QCD divisor

Pick a four-cycle to host a toy version of QCD via a stack of D7-branes

Compute axion Lagrangian



Set superpotential

- Fix the scale of supersymmetry breaking
- Assume Euclidean D3-branes on every holomorphic divisor contribute