

String Phenomenology Conference 2024
Centro Culturale Altinate - San Gaetano - Padova (Italy)

REALISTIC BRANE- ANTIBRANE INFLATION



Mario Ramos-Hamud
University of Cambridge



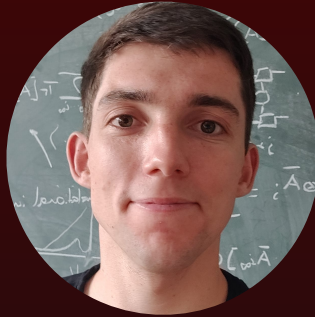
Thursday, 27th June 2024



COLLABORATION



M. Cicoli



C. Hughes



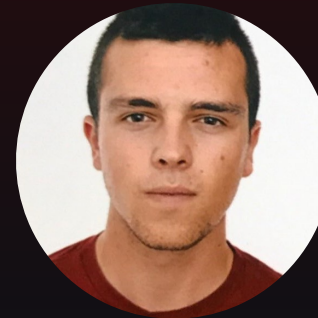
A. Rakin



F. Marino



F. Quevedo

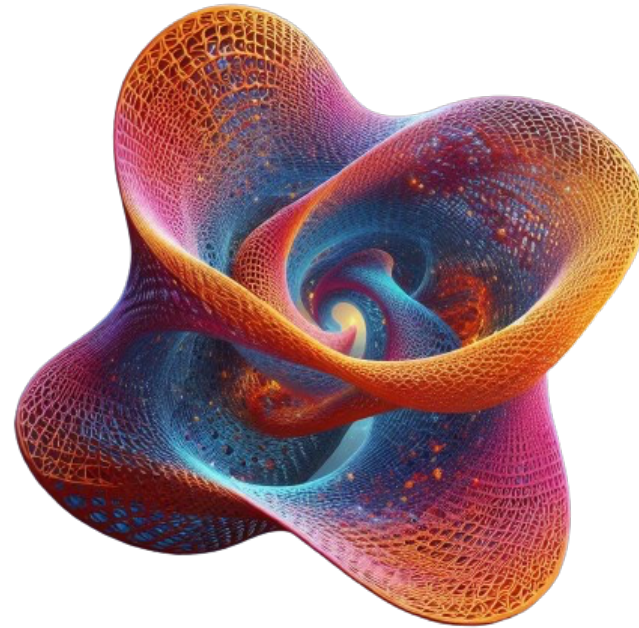


G. Villa



OUTLINE

- Motivation
- Perturbative corrections
- Perturbative modulus stabilisation
- Brane anti-brane inflation
- Conclusions



MOTIVATION



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Inflation stands as the standard realisation of early universe cosmology. Concave potentials favoured experimentally:

$$V(\phi) = A - \frac{B}{\phi^n} + \dots \quad \text{or} \quad V(\phi) = C - De^{-a\phi} + \dots$$



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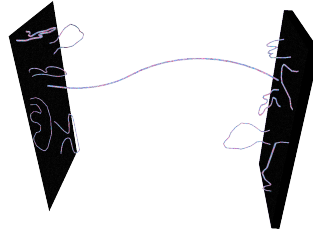
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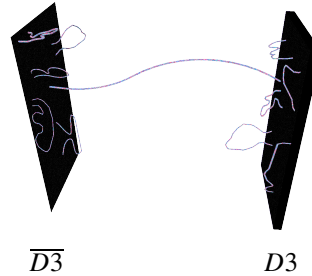
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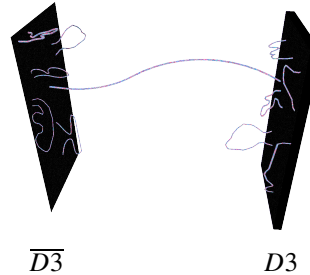
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1. Inflation potential must consider the inflaton and the volume modulus \mathcal{V} .
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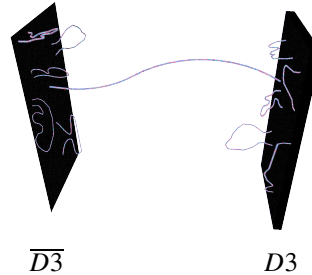
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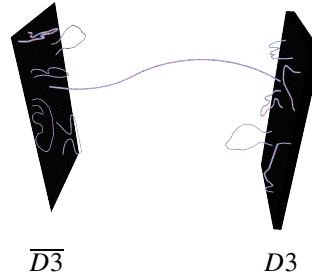
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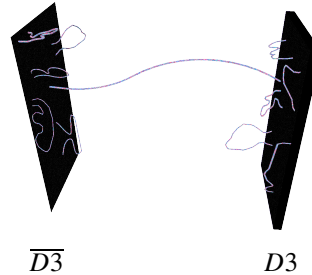
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Leading terms



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The leading order **Kähler potential**:

$$K = -\ln(s) - 3 \ln \left(\tau - \alpha \ln[\tau] + \frac{\xi s^2 - 3D \ln(\tau)}{3s^{1/2}\tau^{1/2}} \right),$$

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The leading order **scalar potential**:

$$\frac{V_s}{3|W_0|^2} = \frac{\alpha}{\tau^4} + \frac{s^2\xi + \mathcal{O}(1/s^2) - 3D \ln \tau}{4s^{1/2}\tau^{9/2}} + \mathcal{O}\left(\frac{1}{\tau^5}\right),$$

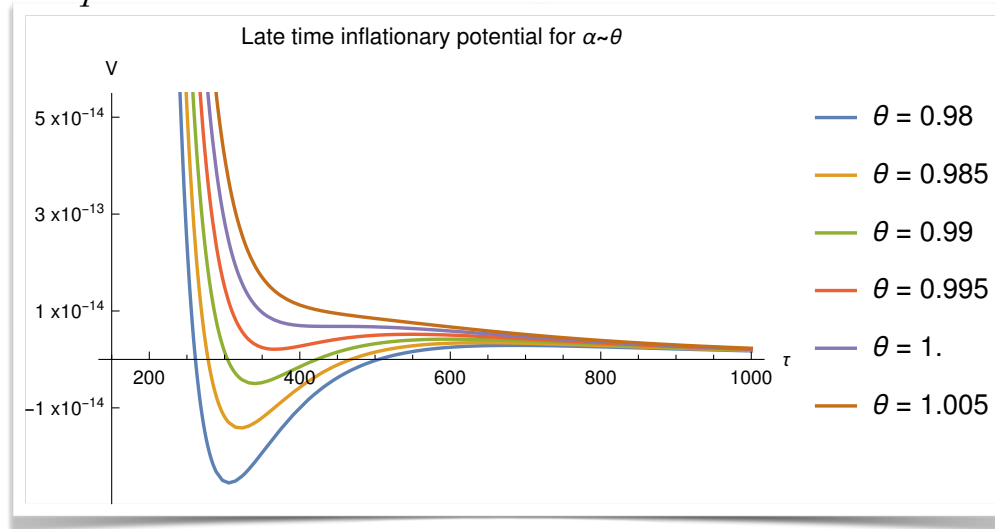
Minimum: $\tau_* = \exp\left(\frac{s^2\xi}{3D} + \frac{2}{9} - 2\mathcal{W}_0\left[\frac{\theta}{e}\right]\right)$ with $\theta := \frac{16}{27}D^{-1}s^{1/2}\alpha e^{\frac{s^2\xi}{6D} + \frac{10}{9}}$ and

$$\alpha \sim \frac{D}{\sqrt{s\tau_*}}.$$

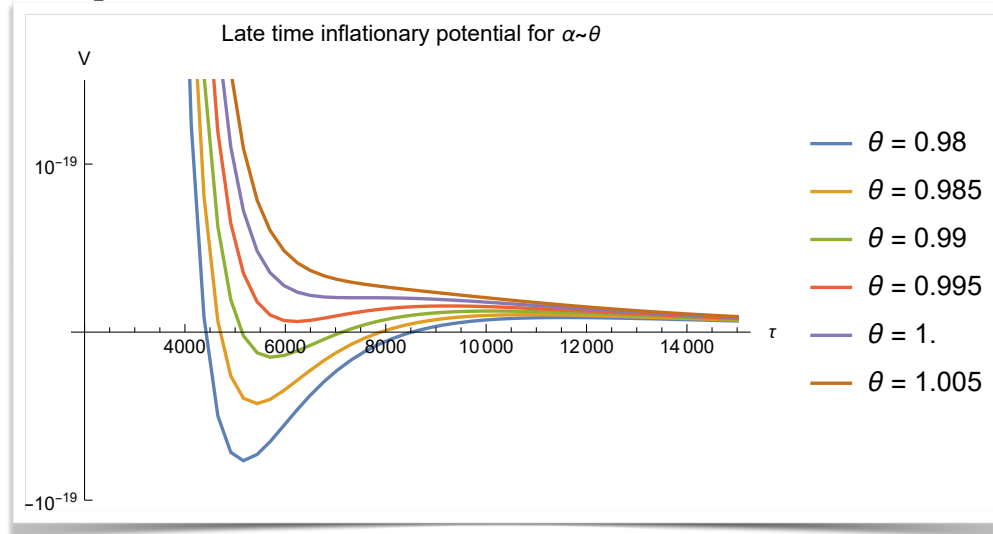


PERTURBATIVE STABILISATION

Only-leading-term perturbative corrections:



Including all known perturbative corrections:

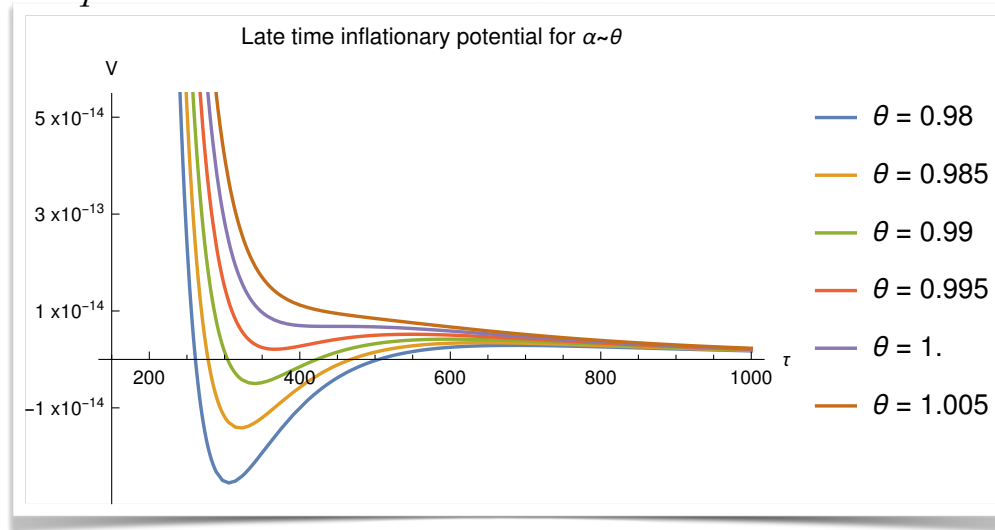


* In the plots $W_0 = 1$ and $s = 10$. We get $\tau \sim 350$ and $V_{\min} \ll 10^{-14}$.

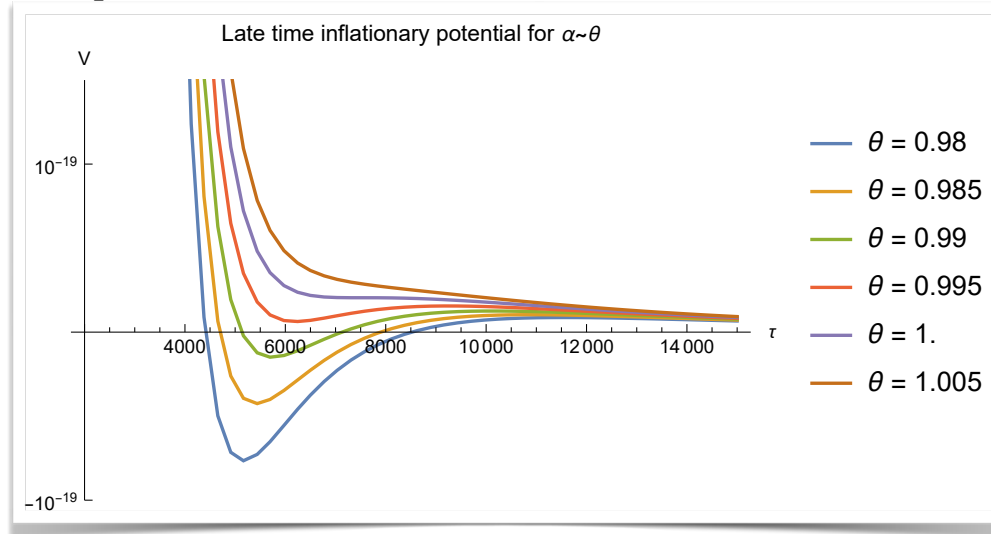


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In both cases, increasing values of θ moves AdS \rightarrow dS \rightarrow runaway.

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Type IIB string theory compactified on a CY threefold in the presence of fluxes.



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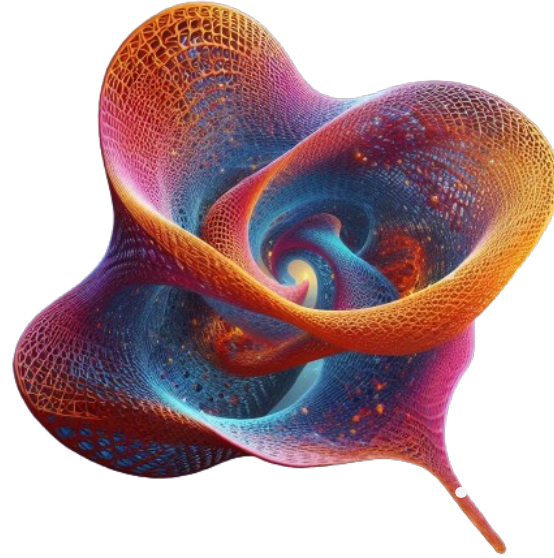
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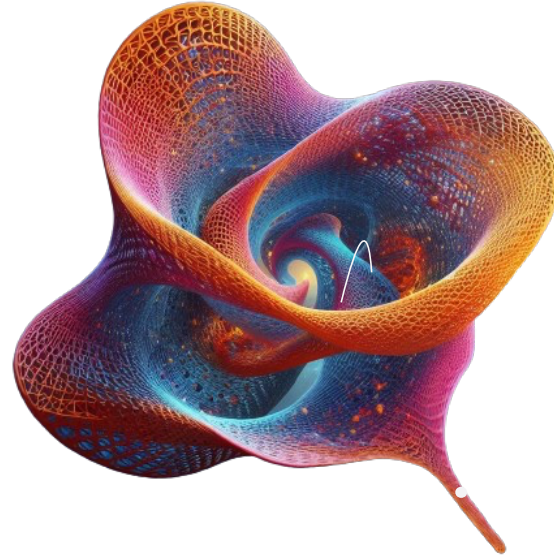
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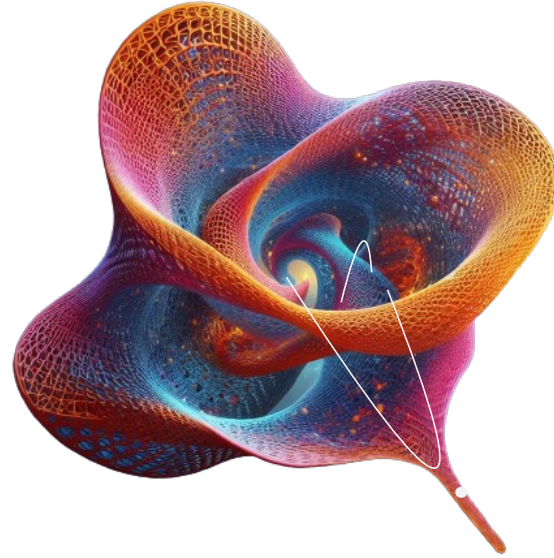
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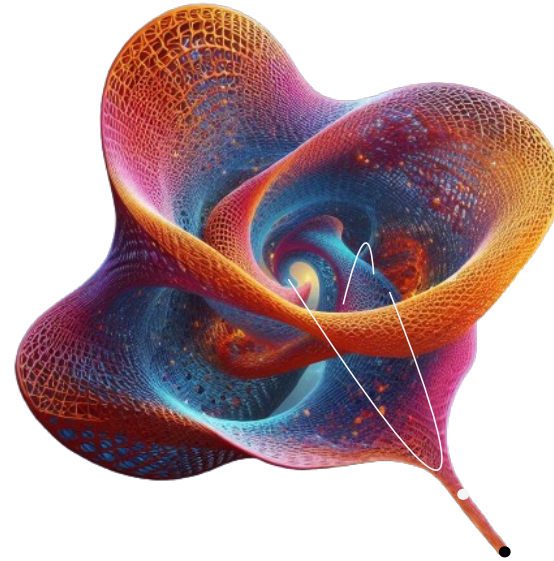
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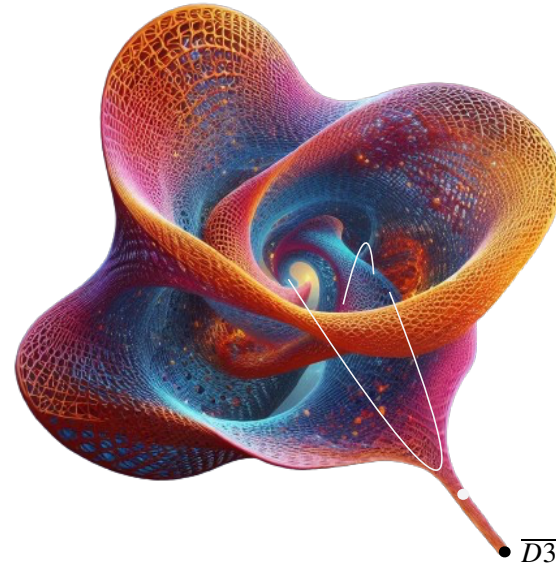
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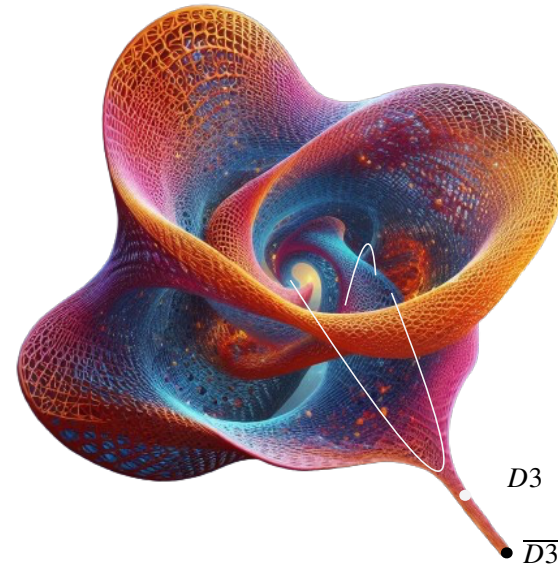
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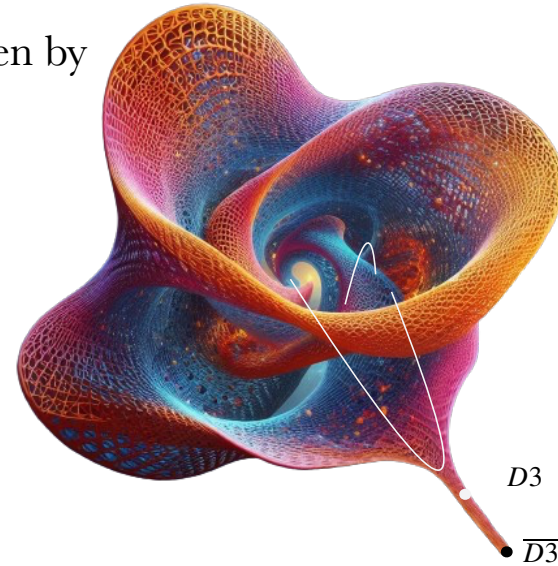


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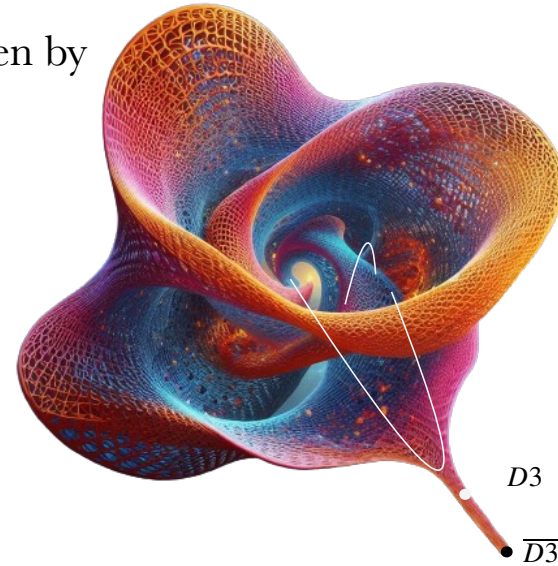
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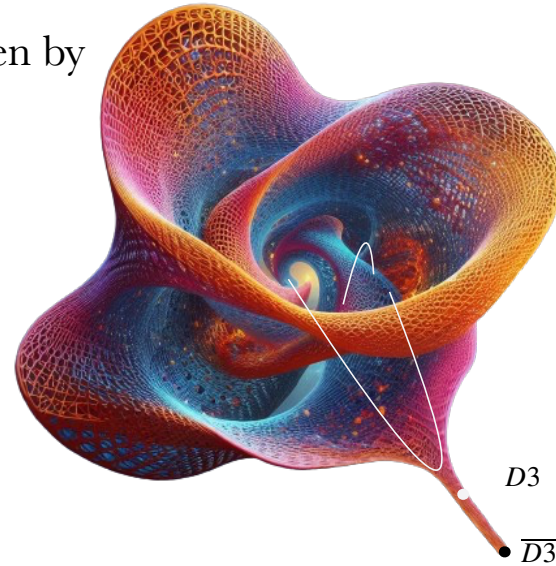
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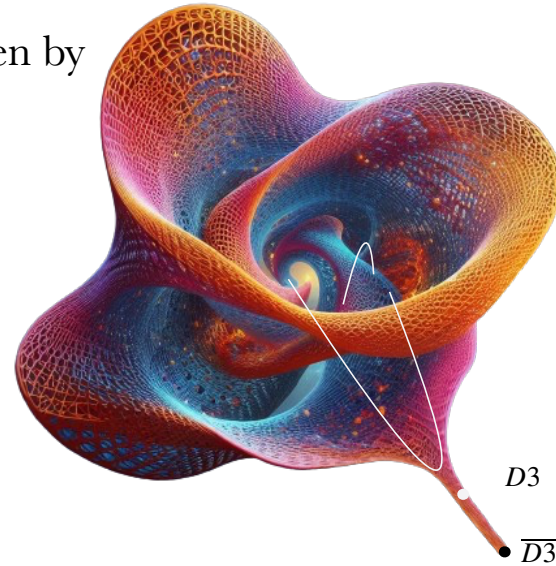
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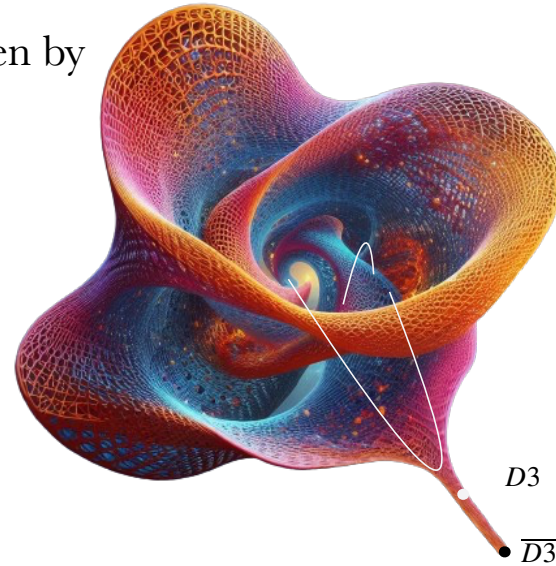
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Nilpotent superfield framework:

The setup can be studied using non-linear SUSY with a **goldstino** superfield X breaking SUSY:

$$K = -3 \ln (f(\tau) + (X + \bar{X}) g(\tau) + X\bar{X} h(\tau)),$$

and

$$W = W_0 + XW_X.$$

So we divided our study in two scenarios:

- Case with $g(\tau) \neq 0$.
- Case with $g(\tau) = 0$.



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The Kähler potential with the computed corrections is

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1. At leading order with $\alpha = 0$: $\frac{V}{W_0^2} = \frac{1}{3s\tau^2} \left(\delta - \frac{3a}{s\tau} \right)^2 \rightarrow$ Minkowski: $\tau = \frac{3a}{s\delta}$.

2. We uplift to dS by considering the value of V_{NLO} at this minimum and restore α .



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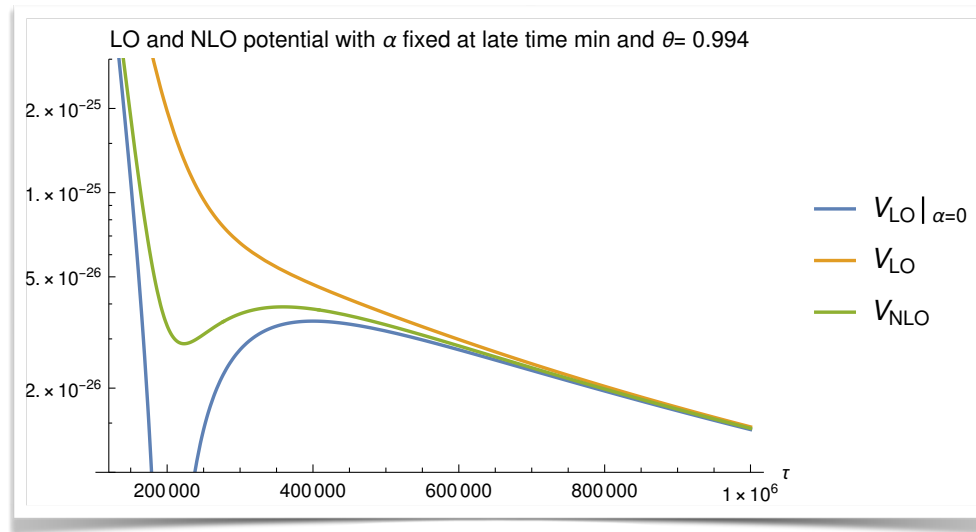
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1. At leading order with $\alpha = 0$: $\frac{V}{W_0^2} = \frac{1}{3s\tau^2} \left(\delta - \frac{3a}{s\tau} \right)^2 \rightarrow$ Minkowski: $\tau = \frac{3a}{s\delta}$.

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LINEAR TERM INCLUDED

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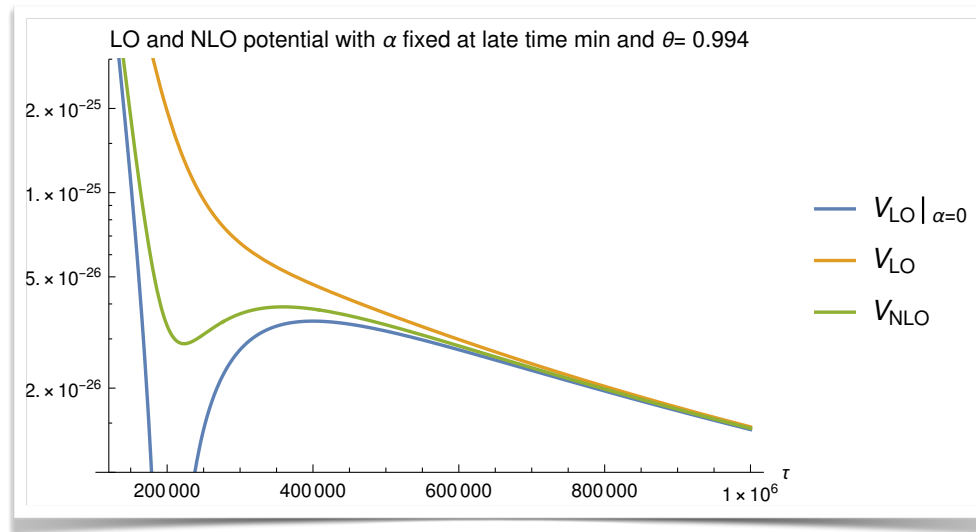


Figure.- Parameter space: $s = 15$, $a = 1$, $W_0 = 1$, $\delta = 10^{-6}$, $\xi = 0.1$, $A = 1$. NNLO terms are suppressed.



WITHOUT LINEAR TERM

^



WITHOUT LINEAR TERM

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WITHOUT LINEAR TERM

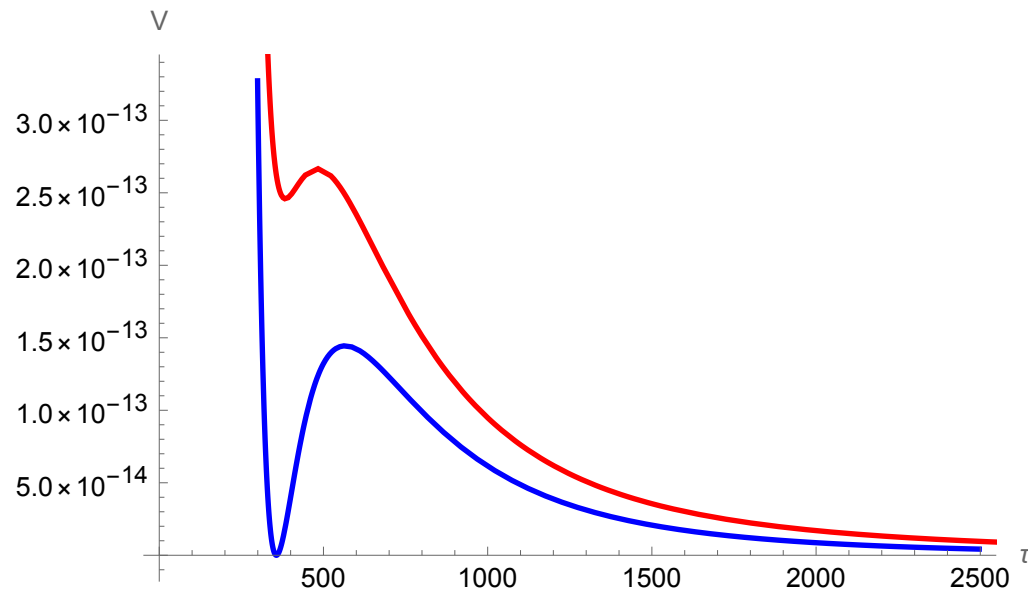
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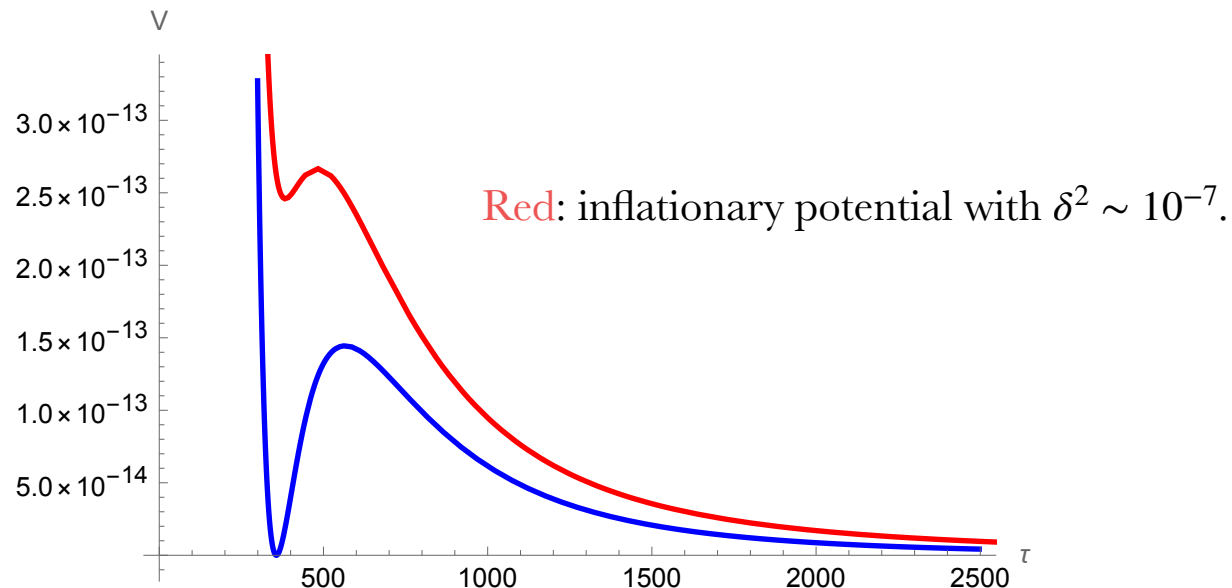
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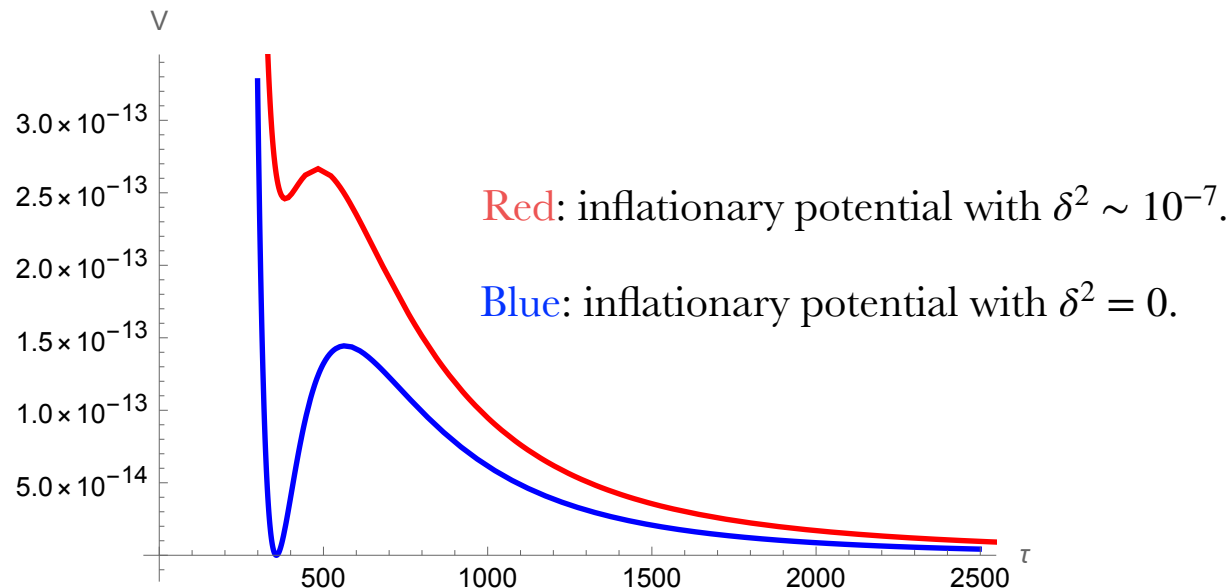
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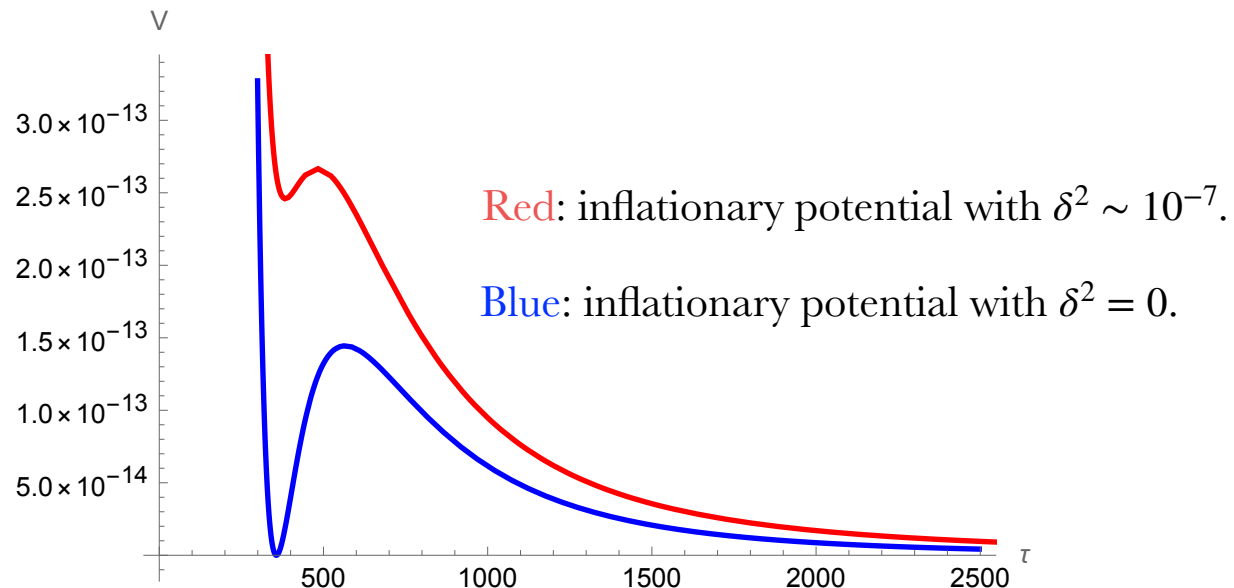
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The minimum is at $V_{\min}^{\text{inf}} \sim 10^{-13}$ and late minimum is approximately Minkowski.

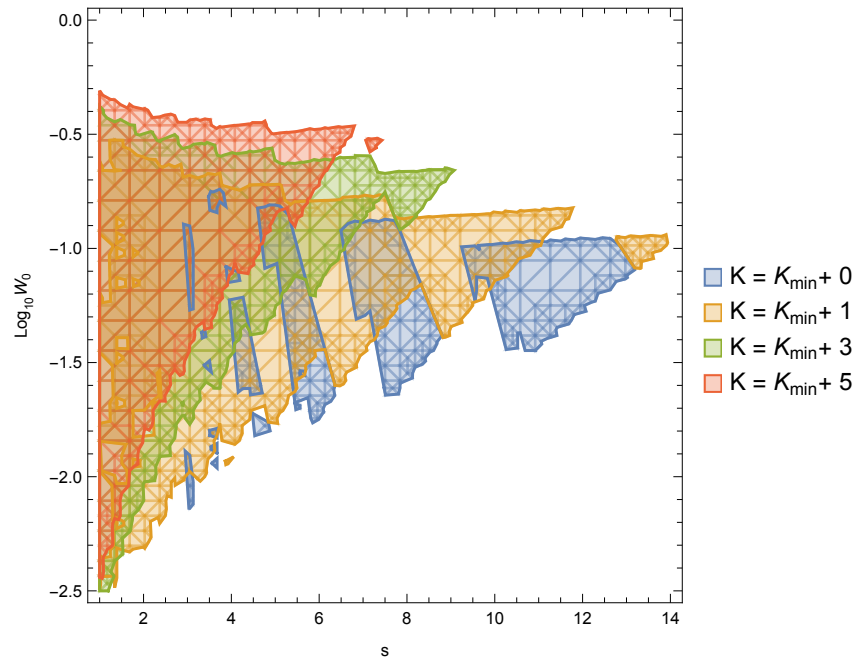


CONSISTENCY CONSTRAINTS FOR INFLATION

- Inter-brane separation larger than string length: $\varphi^4 > \frac{6MKg_s^3}{(2\pi)^4\mathcal{V}^{4/3}}e^{-4\rho}$.
- Proper separation smaller than the KK length scale: $\varphi^4 < \frac{6MKg_s^3}{(2\pi)^4\mathcal{V}^2}$.
- Gravitino mass condition: $W_0 \frac{\sqrt{g_s}}{\mathcal{V}^{1/3}} \ll 1$.
- Curvature corrections at the tip of the throat: $g_s M \geq 1$.
- Conifold modulus stability: $g_s M^2 \geq 46$.
- Non-singular bulk condition: $\frac{\mathcal{V}^{2/3}}{KM} \gg 1$.

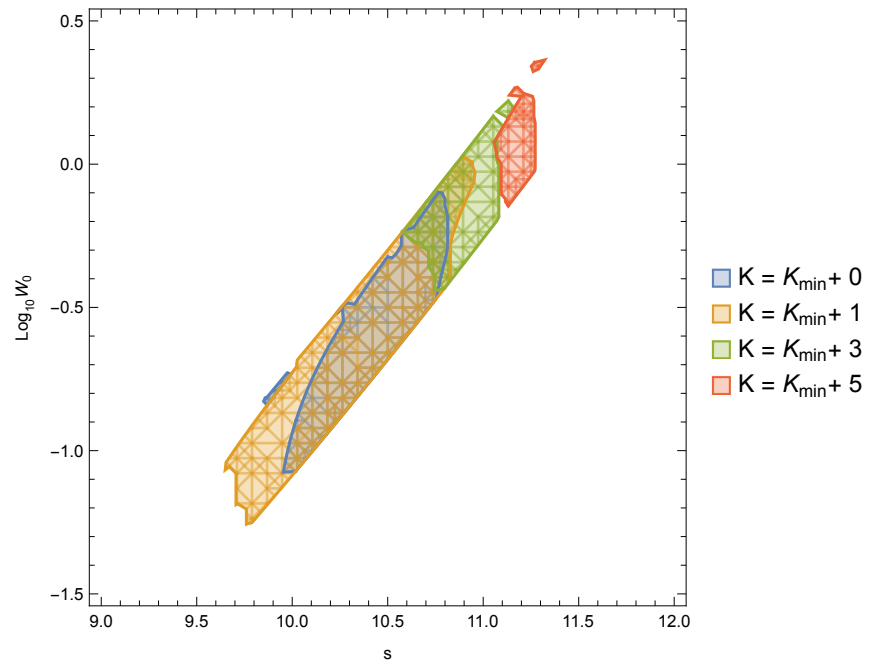


RESULTS



Parameter space
with linear
contribution

Parameter space
without linear
contribution



SUMMARY AND CONCLUSIONS



*String Phenomenology
Conference 2024*



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For extra details and further questions please visit the homonymous poster session by Ahmed.



"The invisible and the non-existent look very much alike."
-S. Weinberg.

GRATZIE!

Mario Ramos Hamud
Email: mr895@cam.ac.uk
DAMTP | University of Cambridge



String Phenomenology
Conference 2024



BACKUP SLIDES

η -PROBLEM

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η -PROBLEM

Consider the Kähler potential

$$K \simeq -3 \ln[\tau - \phi\bar{\phi} + \dots].$$

when τ is fixed by **non-perturbative effects**, $\phi\bar{\phi}$ induces a correction to the inflaton potential given by

$$V_{\text{correction}} \sim \frac{V_{\text{original}}}{\tau^3} \phi\bar{\phi},$$

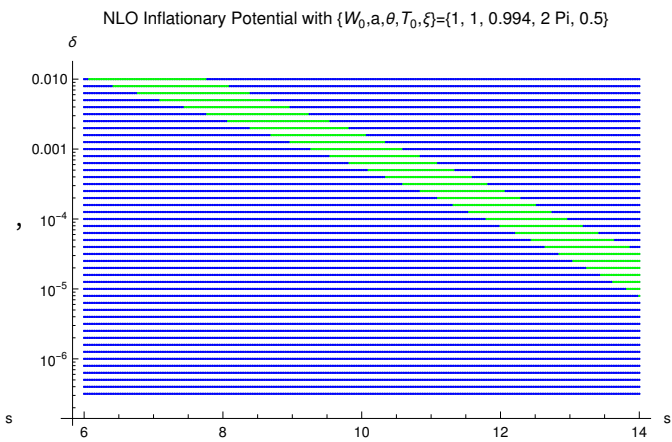
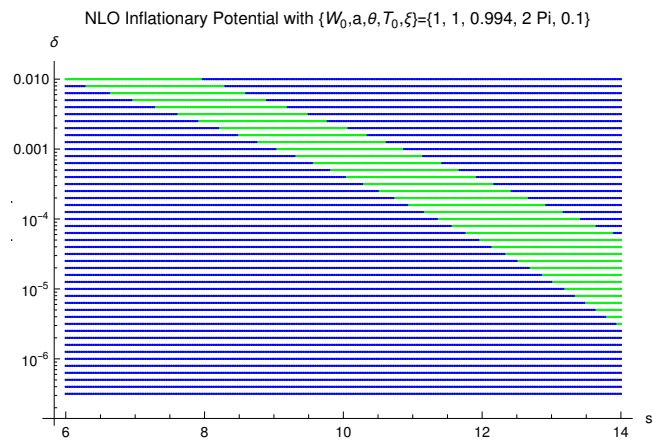
with V_{original} fixing the Hubble scale during inflation: $H_I^2 \sim \frac{V_{\text{original}}}{\tau^3}$.

- The mass contribution of the inflaton is $m_\phi^2 \sim \frac{V_{\text{original}}}{\tau^3} \sim H_I^2$
- Slow roll parameter: $\eta \sim \frac{V'''}{V} \sim \frac{m_\phi^2}{H_I^2} \sim 1 \Rightarrow$ **No longer slow-roll inflation!**

η -problem can be avoided by doing a **perturbative stabilisation of the volume modulus.**



LINEAR TERM PART I



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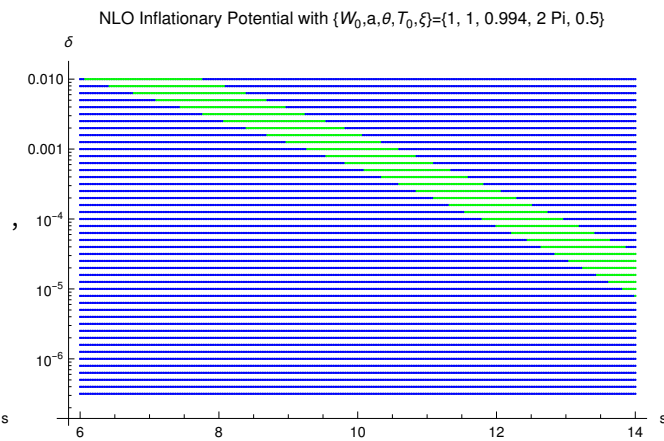
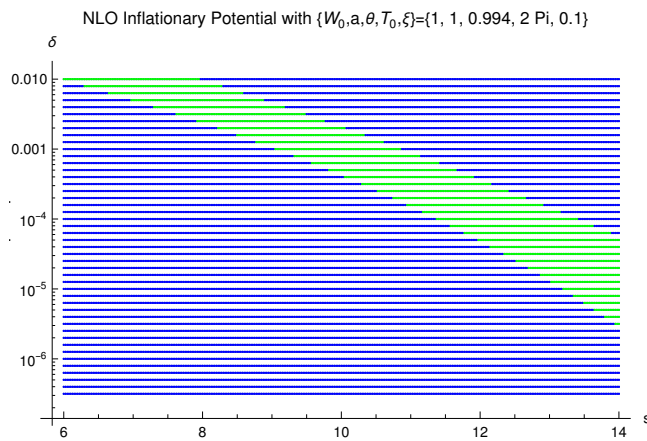
$$K = -\ln(s) - 3 \ln \left[\tau - \alpha \ln(\tau) + \frac{s^2 \xi - 3D \ln(\tau)}{3s^{1/2} \tau^{1/2}} + (X + \bar{X}) \frac{a \ln(\tau)}{s} - \frac{1}{2} X \bar{X} \right],$$

meanwhile the scalar potential becomes

$$\frac{V}{W_0^2} = \mathcal{A} \frac{\delta^2}{\tau^2} + \mathcal{B} \frac{\delta}{\tau^3} + \mathcal{C} \frac{1}{\tau^4}, \quad \delta = \frac{|W_X|}{|W_0|},$$

where

- $\mathcal{A} = \frac{1}{3s} + \frac{a^2 (1 - 2 \ln(\tau) + 3 \ln(\tau)^2) + 2\alpha s^2 \ln(\tau) - 2As}{3s^3 \tau} + \dots,$
- $\mathcal{B} = -\frac{2a}{s^2} - \frac{2a [a^2 (1 - 2 \ln(\tau) + 3 \ln(\tau)^2) - s \ln(\tau)(3A - \alpha s) - 2s(A - \alpha s)]}{s^4 \tau} + \dots,$
- $\mathcal{C} = \frac{3(a^2 + \alpha s^2)}{s^3} + \frac{3(\xi s^2 + 8D + 3\sigma - 3D \ln(\tau))}{4s^{3/2} \tau^{1/2}} +$
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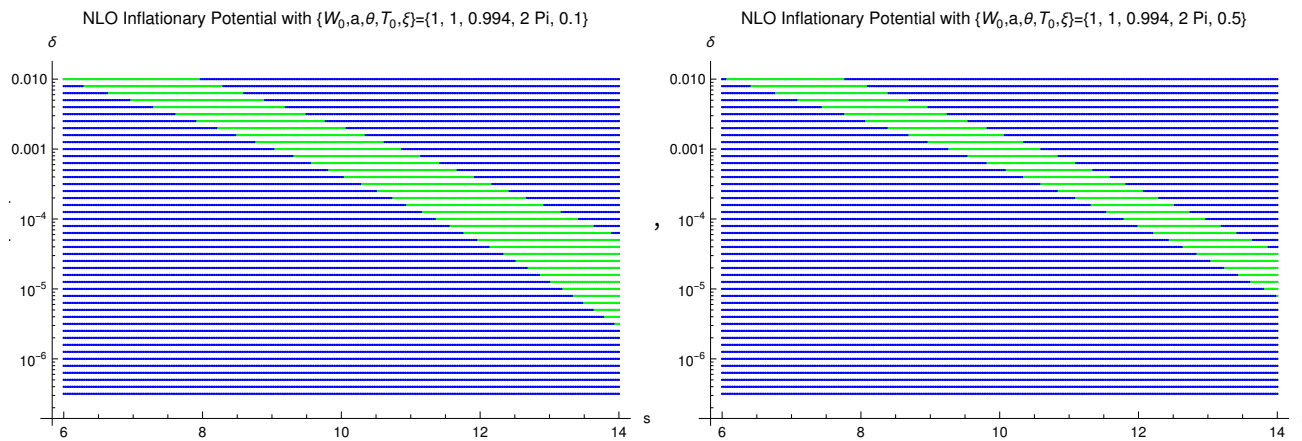
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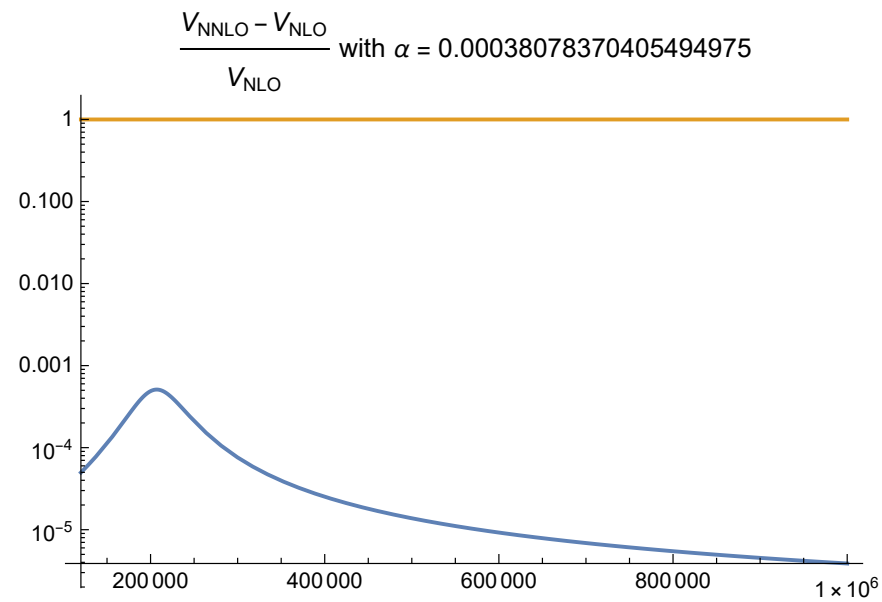
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Green: dS solution. Blue: runaway.



LINEAR TERM PART II



LINEAR TERM PART II

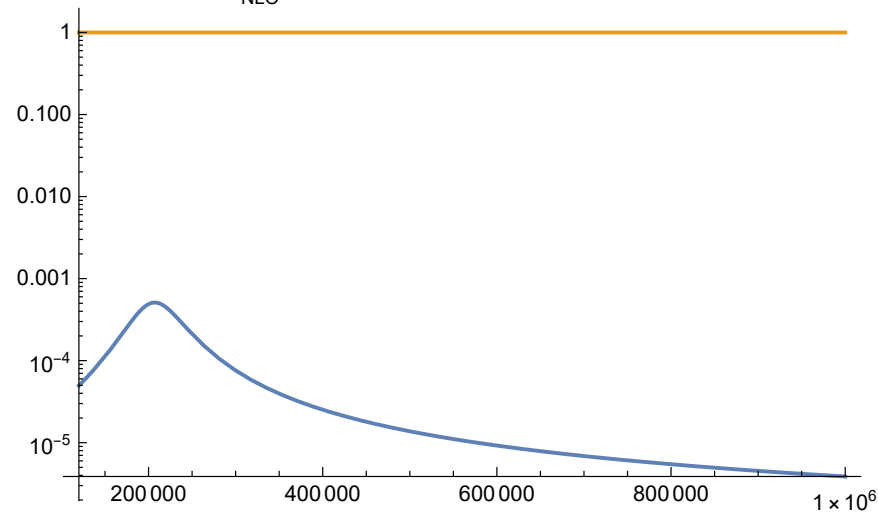
Leading contribution comes from C at $\mathcal{O}\left(\frac{1}{\sqrt{\tau}}\right)$. The most important at large τ .

$$\frac{V_{LO}}{|W_0|^2} = \frac{\delta^2}{3s\tau^2} - \frac{2a\delta}{s^2\tau^2} + \frac{3(a^2 + \alpha s^2)}{s^3\tau^4} = \frac{|W_0|^2}{3s\tau^2} \left(\delta - \frac{3a}{s\tau} \right)^2 + \frac{3|W_0|^2\alpha}{s\tau^4},$$

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$$\frac{V_{NNLO}}{|W_0|^2} \sim \frac{\delta^a}{\tau^b} \text{ with } a+b = 5.$$

$$\frac{V_{NNLO} - V_{NLO}}{V_{NLO}} \text{ with } \alpha = 0.00038078370405494975$$



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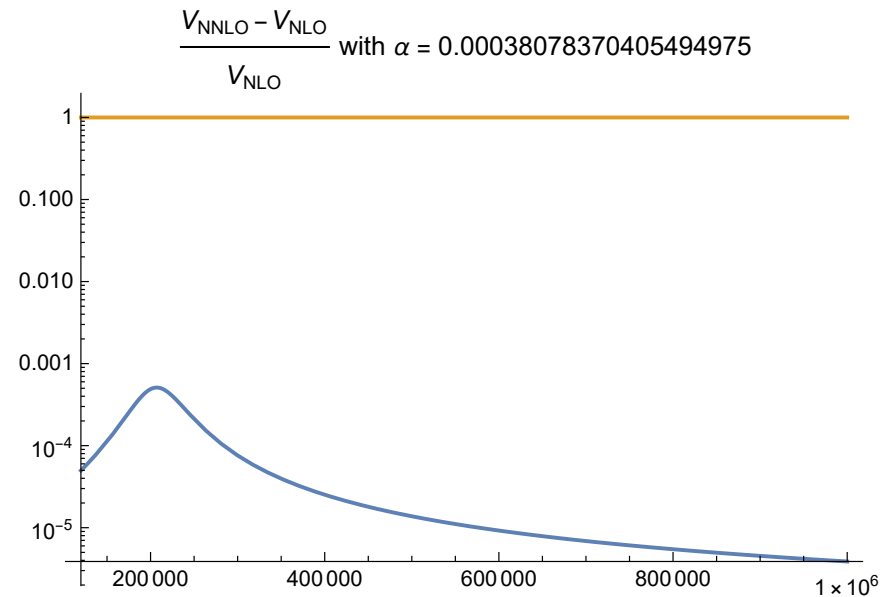


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Some remarks about the competing terms:

$$V_{LO} \sim \frac{\mathcal{O}(1)}{\tau^2 s} - \frac{\mathcal{O}(1)}{\tau^3 s^2} + \frac{\mathcal{O}(1)}{\tau^4 s^3} \sim s$$

and

$$V_{NLO} \sim \frac{\mathcal{O}(1)e^{-s}}{\tau^4 s^{3/2}} + \frac{\mathcal{O}(1)}{\tau^{9/2} s^{3/2}} + \frac{\mathcal{O}(1)s^{1/2}}{\tau^{9/2}} + \frac{\mathcal{O}(1)\ln(\tau)}{\tau^{9/2} s^{3/2}} \sim s^{5/2}e^{-s} + s^3 + s^5 + s^3 \ln s.$$

For increasing s we have some implications:

- The inverse dependence $\tau \sim s^{-1}$ implies that position of the minimum will move to smaller τ . Hierarchies between V_{LO} and V_{NLO} reduced by expansion in $\frac{1}{\tau}$.
- Coefficients in the NLO terms will increase more rapidly than the coefficients of the LO terms.
- NLO become dominant and therefore, for arbitrarily large s , the NLO corrections to the potential will become too strong leading to a runaway potential.
- To compensate for larger values of $s \rightarrow$ greater hierarchy between the LO and NLO terms \rightarrow smaller $\delta \rightarrow$ larger τ at the minimum.
- Arbitrarily large $s \Rightarrow$ arbitrarily large $\tau \rightarrow$ cosmological moduli problem.



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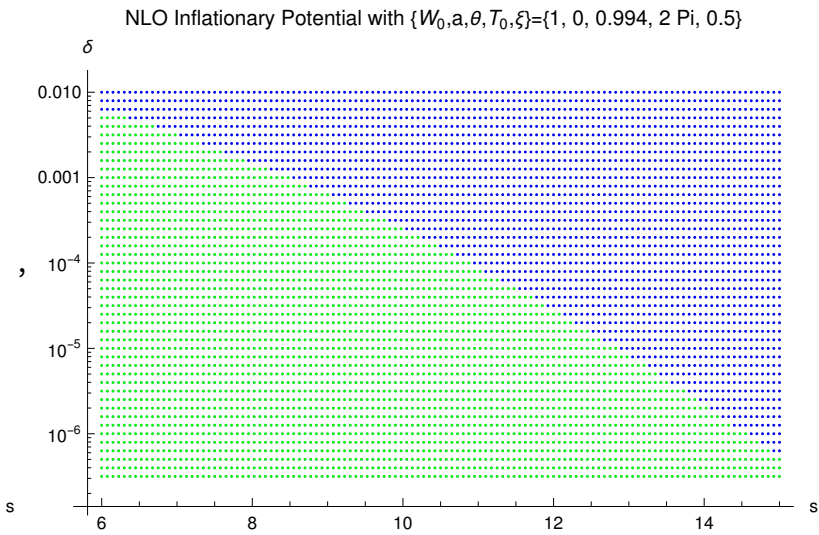
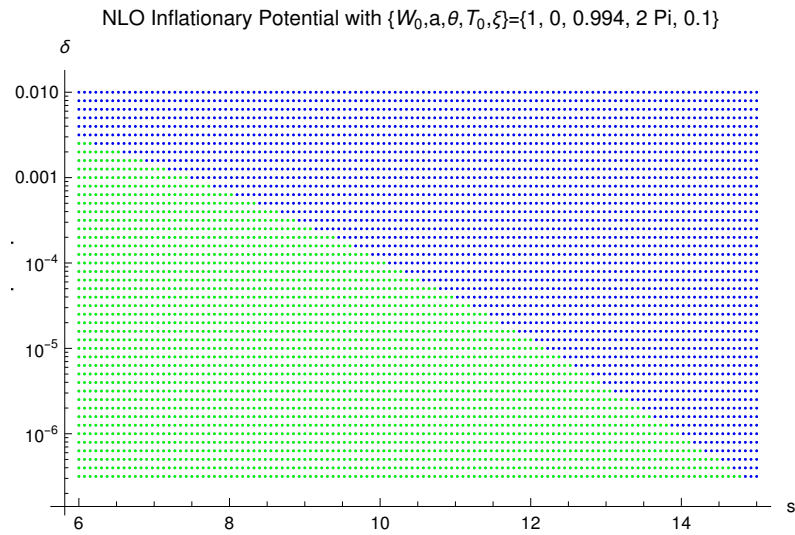
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[K. J. Bae, H. Baer, V. Barger, and R. W. Deal, 2022]



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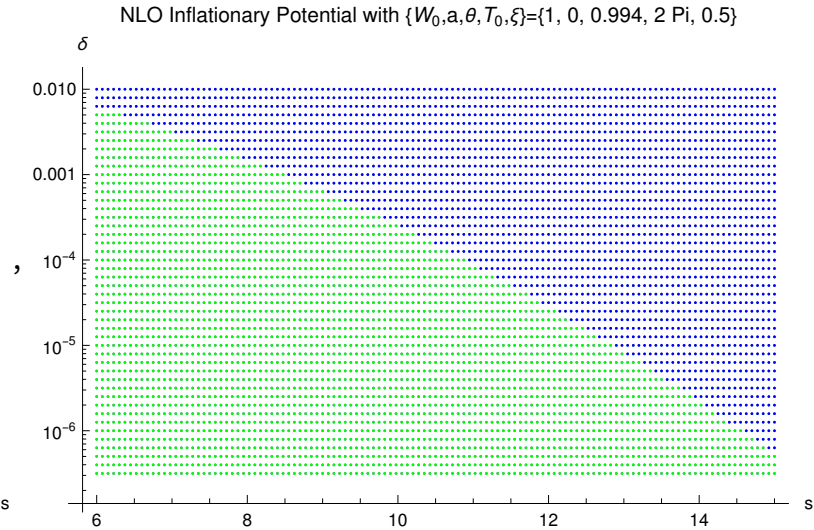
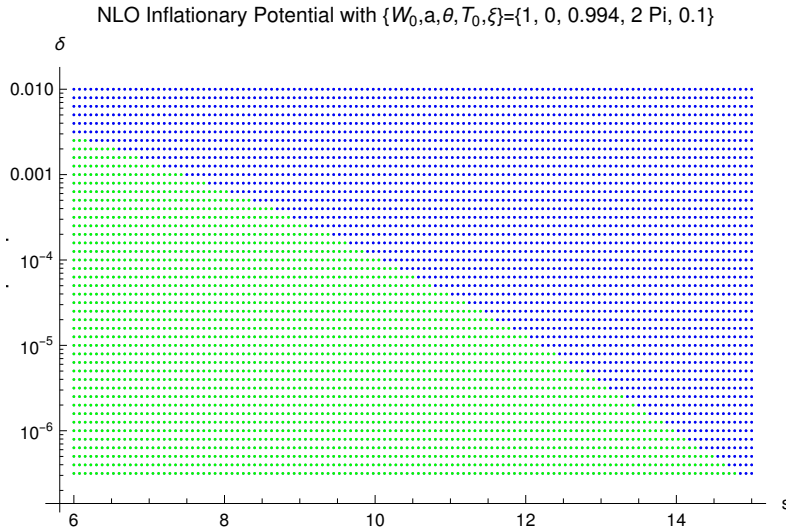
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where coefficients as in case with linear term but $a = 0$:

- $\mathcal{A} = \frac{1}{3s} - \frac{2As}{3s^3 \tau} + \dots,$

- $\mathcal{C} = \frac{3(\alpha s^2)}{s^3} + \frac{3(\xi s^2 + 8D + 3\sigma - 3D \ln(\tau))}{4s^{3/2} \tau^{1/2}} + \frac{3s^2(3A^2 - 2\alpha As + 3\alpha^2 s^2)}{s^5 \tau} + \dots$



WITHOUT LINEAR TERM

The Kähler potential is

$$K = -\ln(s) - 3 \ln \left[\tau - \alpha \ln(\tau) + \frac{s^2 \xi - 3D \ln(\tau)}{3s^{1/2} \tau^{1/2}} - \frac{1}{2} X \bar{X} \right],$$

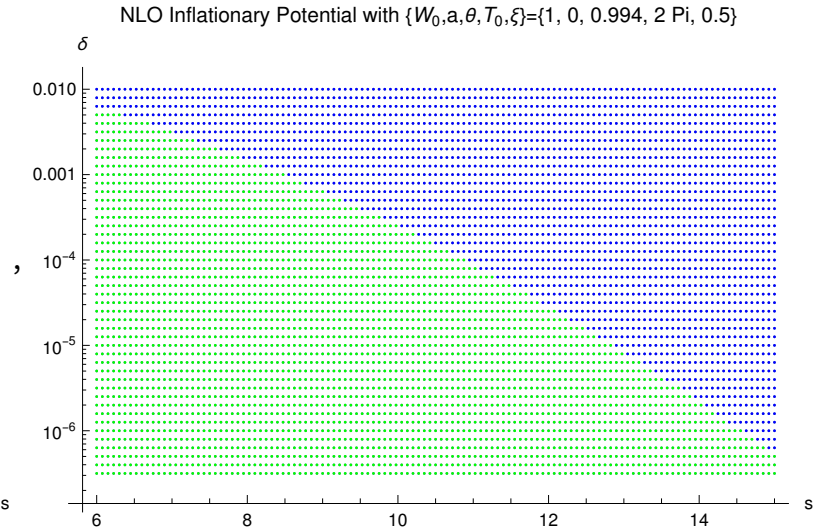
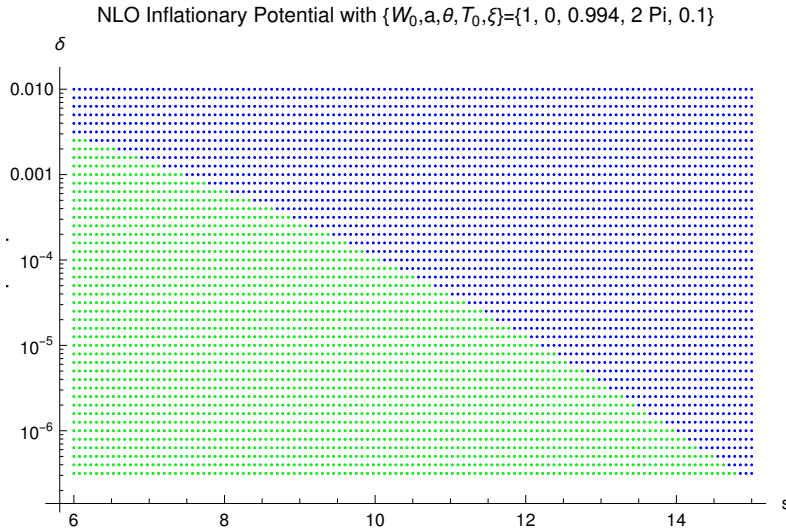
meanwhile the scalar potential becomes

$$\frac{V}{W_0^2} = \mathcal{A} \frac{\delta^2}{\tau^2} + \mathcal{C} \frac{1}{\tau^4}, \quad \delta = \frac{|W_X|}{|W_0|},$$

where coefficients as in case with linear term but $a = 0$:

- $\mathcal{A} = \frac{1}{3s} - \frac{2As}{3s^3 \tau} + \dots,$

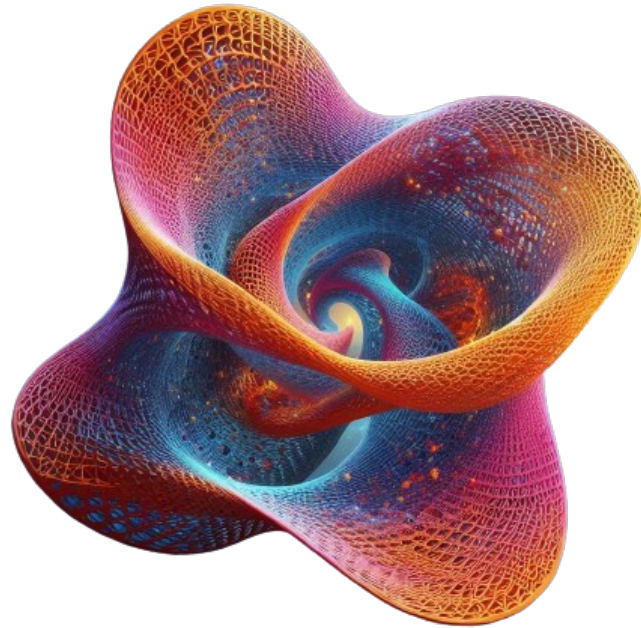
- $\mathcal{C} = \frac{3(\alpha s^2)}{s^3} + \frac{3(\xi s^2 + 8D + 3\sigma - 3D \ln(\tau))}{4s^{3/2} \tau^{1/2}} + \frac{3s^2(3A^2 - 2\alpha As + 3\alpha^2 s^2)}{s^5 \tau} + \dots$



Green: dS solution. Blue: runaway.



GEOMETRICAL TOOLKIT



GEOMETRICAL TOOLKIT

Parameters for inflation, α and ξ , are constrained:

- ξ (and therefore D) is determined by the Euler characteristic χ .
- Kreuzer-Skarke CY database favours: $|\chi| < 200 \Rightarrow 0 < |\xi| < 5$.
- α is a one-loop beta function coefficient and is expected to be suppressed.

