

Loop Blow-Up Inflation

A novel way to inflate with the Kähler moduli

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Based on:

S. Bansal, LB, M. Cicoli, A. Hebecker, R. Kuespert: 2403.04831

See Hebecker's talk

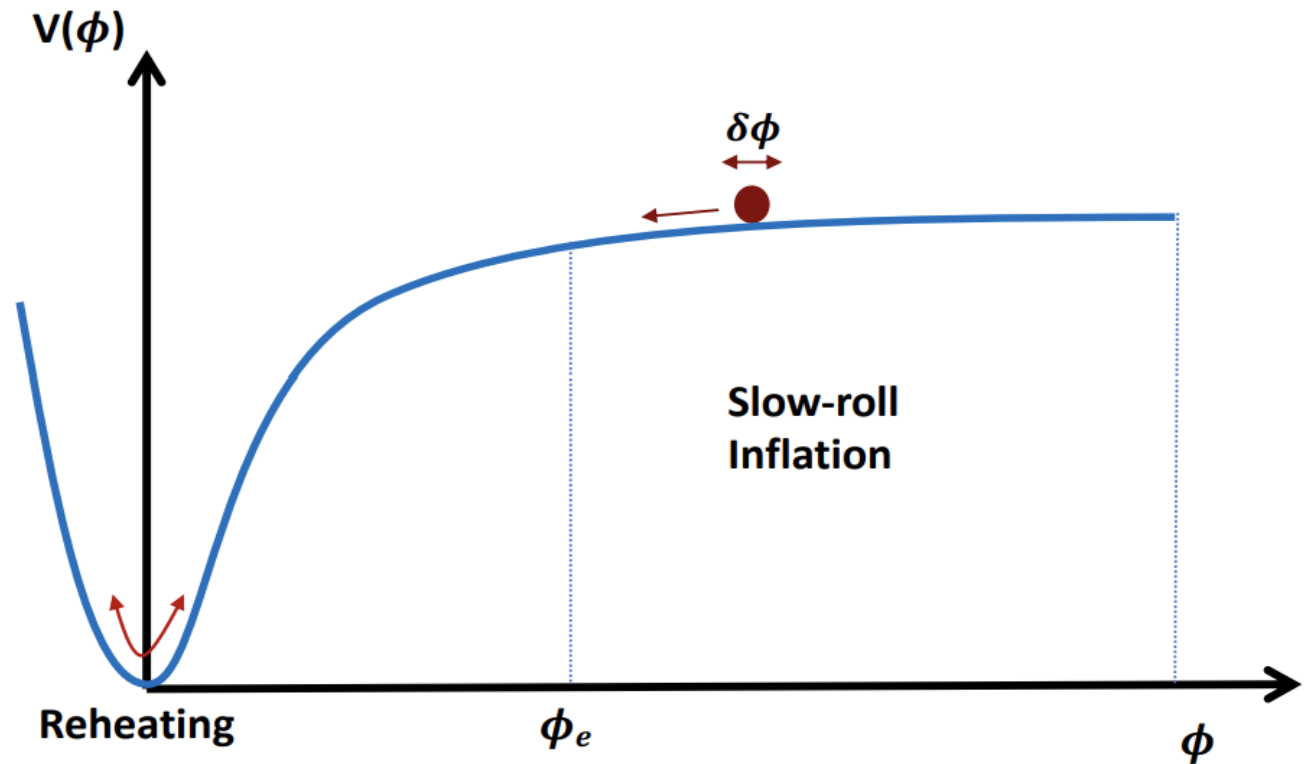
Slow-Roll Inflation

- **Standard Slow-Roll:** Scalar field with almost-flat direction in the potential

- Possible form of the potential:

$$V(\phi) = V_0[1 - f(\phi)]$$

with $f(\phi) \rightarrow 0$ as $\phi \rightarrow +\infty$.



Credits: String Cosmology: from the Early Universe to Today
[Cicoli, Conlon, Maharana, Parameswaran, Quevedo, Zavala: 2023]

Kähler Moduli Inflation

- Type IIB String Compactifications \implies Moduli with leading-order flat potential
- **Kähler moduli:** Tree level no-scale + 1-loop extended no-scale [Cicoli, Conlon, Quevedo: 2008]
- **Volume \mathcal{V} :** lifted by leading-order corrections:
 - **BBHL:** $V_{\alpha'^3}(\mathcal{V})$ [Becker, Becker, Haack, Louis: 2002]
 - **Uplifting:** $V_{\text{up}}(\mathcal{V})$ (anti-D3, T-branes, ...)
- **Other Kähler moduli:** LO flat directions \implies good inflaton candidates τ_φ !
- **Need:** Subleading quantum corrections (loops, non-perturbative effects)

Classification of Inflationary Models

- Classification of inflationary models with Kähler moduli based on:
 - a) **Topology (bulk/local)**: determines the canonical normalization $\tau_\varphi(\varphi)$
 - b) **Lifting Effects (perturbative/non-perturbative)**: determine the shape of the potential
- All models give a potential of the form:

$$V(\varphi) = V_0[1 - f(\varphi)]$$

with $f(\varphi)$ depending on topology + lifting effects and such that $f(\varphi) \ll 1$ for $\varphi \gg 1$.

Lifting Effect Topology	Non-Perturbative: $V(\tau) \sim e^{-a\tau} \quad (a > 0)$	Perturbative: $V(\tau) \sim \frac{1}{\tau^\beta} \quad (\beta > 0)$
Bulk (fibre) $\tau(\varphi) = e^{k\varphi}$	Non-Perturbative Fibre Inflation: $f(\varphi) \propto e^{-ae^{k\varphi}}$ [Cicoli, Pedro, Tasinato: 2011] [Lüst, Zhang: 2013]	Loop Fibre Inflation $f(\varphi) \propto e^{-\beta k\varphi}$ [Cicoli, Burgess, Quevedo: 2008] [Broy, Ciupke, Pedro Westphal: 2015] [Cicoli, Ciupke, de Alwis, Muia: 2016]
Local (Blow-up) $\tau(\varphi) = \gamma \mathcal{V}^{2/3} \varphi^{4/3}$	Non-Perturbative Blow-Up Inflation $f(\varphi) \propto e^{-a\gamma \mathcal{V}^{2/3} \varphi^{4/3}}$ [Cicolon, Quevedo: 2006] [Bond, Kofman, Prokushkin, Vaudrevange: 2006]	Loop Blow-Up Inflation $f(\varphi) \propto \frac{1}{\mathcal{V}^{2\beta/3} \varphi^{4\beta/3}}$ [Bansal, LB, Cicoli, Hebecker, Kuespert: 2024] New!

Non-Perturbative Blow-Up Inflation

- Calabi-Yau volume:

$$\mathcal{V} = \tau_b^{3/2} - \tau_s^{3/2} - \tau_\phi^{3/2} \simeq \tau_b^{3/2} \quad \text{with} \quad T_i = \tau_i + i\vartheta_i$$

- LVS stabilisation: $\mathcal{O}(\alpha'^3)$ correction to Kähler potential and non-perturbative correction to W:

$$K = -2 \ln \left(\mathcal{V} - \frac{\xi}{2g_s^{3/2}} \right) \quad W = W_0 + A_s e^{-a_s T_s} + A_\phi e^{-a_\phi T_\phi}$$

- Scalar Potential: $V = V_{LVS} + V_\phi$

$$V_{LVS}(\mathcal{V}, \tau_s) = \tilde{V} \left(B_s \frac{\sqrt{\tau_s} e^{-2a_s \tau_s}}{\mathcal{V}} - C_s \frac{\tau_s e^{-a_s \tau_s}}{\mathcal{V}^2} + \frac{3\xi}{4g_s^{3/2} \mathcal{V}^3} + \frac{D}{\mathcal{V}^2} \right)$$

$$V_\phi(\mathcal{V}, \tau_\phi) = \tilde{V} \left(B_\phi \frac{\sqrt{\tau_\phi} e^{-2a_\phi \tau_\phi}}{\mathcal{V}} - C_\phi \frac{\tau_\phi e^{-a_\phi \tau_\phi}}{\mathcal{V}^2} \right)$$

$$\text{with } a_\phi^{3/2} \gg a_s^{3/2}$$

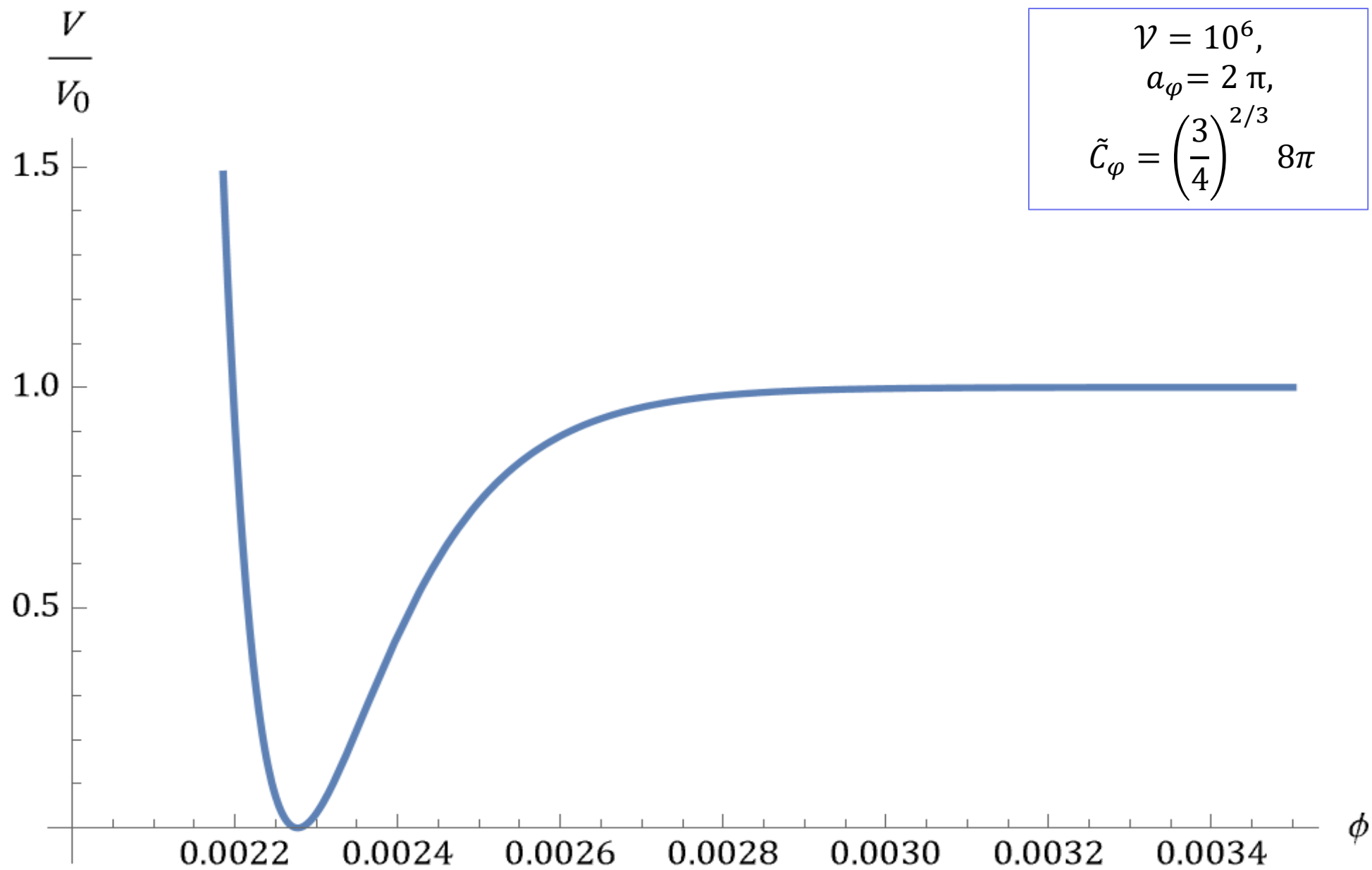
$$\longrightarrow \langle \tau_{s,\phi} \rangle \sim \xi^{2/3} g_s^{-1} \quad \text{and} \quad \langle \mathcal{V} \rangle \sim e^{a_s \tau_s} \sim e^{a_\phi \tau_\phi}$$

- Inflationary potential [Conlon, Quevedo: 2006]:

$$V(\tau_\phi) \simeq V_0 [1 - C_\phi \mathcal{V} \tau_\phi e^{-a_\phi \tau_\phi}] \xrightarrow{\tau = \left(\frac{3\mathcal{V}}{4}\right)^{2/3} \phi^{4/3}} V(\phi) = V_0 [1 - \tilde{C}_\phi \mathcal{V}^{5/3} \phi^{4/3} e^{-a_\phi \mathcal{V}^{2/3} \phi^{4/3}}]$$

$$\text{with } V_0 = \tilde{V} \frac{\beta}{\mathcal{V}^3}$$

Exponentially Flat Plateau!



Loop Corrections

- No exact computation of loop corrections on CY background
- 1-loop corrections computed on toroidal orientifolds [Berg, Haack, Körs: 2005]
- Conjectured generalization to CY orientifold [Berg, Haack, Pajer: 2007]
- Two kinds of corrections to K :

1. Kaluza-Klein (KK): $\delta K^{(KK)} = g_s \sum_i \frac{c_i^{(KK)} t_i}{\mathcal{V}}$ \longrightarrow Extended no-scale in V
[Cicoli, Conlon, Quevedo: 2008]

2. Winding (W): $\delta K^{(W)} = \sum_i \frac{c_i^{(W)}}{\mathcal{V} t_i}$

- For a Blow-Up mode τ :

$$\delta K(\tau) \simeq \frac{c_{loop}}{\mathcal{V} \sqrt{\tau}} \longrightarrow \delta V(\tau) \simeq \frac{c_{loop}}{\mathcal{V}^3 \sqrt{\tau}}$$

See Hebecker's talk for details

- EFT understanding from 1-loop corrections to 2-point functions and V

[Von Gersdorff, Hebecker: 2005] [Cicoli, Conlon, Quevedo: 2008] [Gao, Hebecker, Schreyer, Venken:2022]

Loop Blow-Up Inflation

- Potential for τ_ϕ including loop corrections:

$$V = \tilde{V} \left[\frac{\beta}{\nu^3} + B_\phi \frac{\sqrt{\tau_\phi} e^{-2a_\phi \tau_\phi}}{\nu} - C_\phi \frac{\tau_\phi e^{-a_\phi \tau_\phi}}{\nu^2} - \frac{c_{loop}}{\nu^3 \sqrt{\tau_\phi}} \right]$$

- Non-perturbative Blow-Up inflation if:

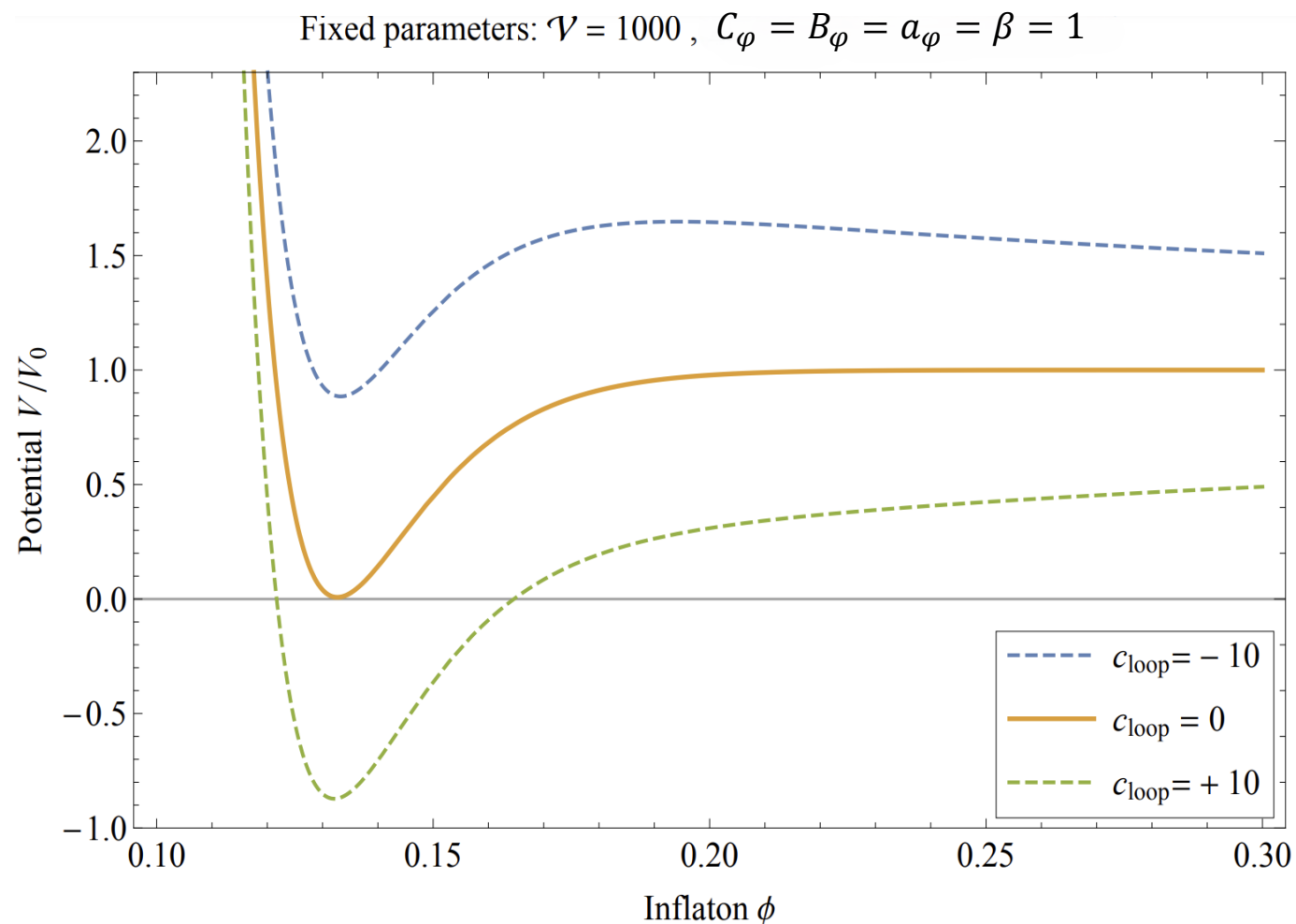
$$c_{loop} \ll 10^{-6}$$

- If $c_{loop} \gtrsim 10^{-6} \implies$ Loops dominate

- Inflationary potential:

$$V \simeq V_0 \left(1 - \frac{c_{loop}}{\beta \sqrt{\tau_\phi}} \right) = V_0 \left(1 - \frac{b c_{loop}}{\nu^{1/3} \phi^{2/3}} \right)$$

$$\text{with } b = \frac{1}{\beta} \left(\frac{4}{3} \right)^{1/3}.$$



Inflationary Parameters

- Slow-roll parameters:

$$V = V_0 \left(1 - \frac{b c_{loop}}{\nu^{1/3} \varphi^{2/3}} \right)$$



$$\begin{cases} \epsilon = \frac{1}{2} \left(\frac{V_{,\varphi}}{V} \right)^2 \simeq \frac{2}{9} \frac{(b c_{loop})^2}{\nu^{2/3} \varphi^{10/3}} \\ \eta = \frac{V_{,\varphi\varphi}}{V} \simeq -\frac{10}{9} \frac{b c_{loop}}{\nu^{1/3} \varphi^{8/3}} \end{cases}$$

- Cosmological parameters:

$$N_e = \int_{\varphi_e}^{\varphi_*} \frac{1}{\sqrt{2\epsilon}} d\varphi \simeq \frac{2}{9} \frac{\nu^{1/3} \varphi_*^{8/3}}{b c_{loop}}$$

$$c_{loop} = 1/(16 \pi^2)$$



$$\begin{cases} \varphi_* = 0.06 N_e^{7/22} \\ \nu = 1743 N_e^{5/11} \end{cases}$$

$$\hat{A}_s = \frac{V^3}{V_{,\varphi}^2} = \frac{9V_0}{4} \frac{\nu^{2/3} \varphi_*^{10/3}}{(b c_{loop})^2} \equiv 2.5 \times 10^{-7}$$

- $r - n_s$ relation:

$$n_s = 1 + 2\eta_* - 6\epsilon_* \simeq 1 - \frac{20}{9} \frac{b c_{loop}}{\nu^{1/3} \varphi_*^{8/3}}$$



$$r = 0.003(1 - n_s)^{11/15}$$

$$r \simeq 16\epsilon_* \simeq \frac{32}{9} \frac{(b c_{loop})^2}{\nu^{2/3} \varphi_*^{10/3}}$$

Post-Inflationary Evolution

- N_e from post-inflationary dynamics [Dutta, Maharana: 2015]:

$$N_e \simeq 57 + \frac{1}{4} \ln r - \frac{1}{4} (N_\varphi + N_\chi) + \frac{1}{4} \ln \left(\frac{\rho_*}{\rho_{end}} \right)$$

- N_φ, N_χ : e-folds of inflaton and volume domination \longrightarrow depend on SM realization

- Decay of last dominant modulus ψ drives reheating:

ψ $\begin{cases} \longrightarrow$ SM fields (Higgs, gauge bosons)

ψ $\begin{cases} \longrightarrow$ big cycle axions ϑ_b : Dark Radiation

$$\Delta N_{\text{eff}} \lesssim 0.2 - 0.5 \quad 95\% \text{ CL}$$

[Planck: 2018]

$$\Delta N_{\text{eff}} = \frac{43}{7} \left(\frac{10.75}{g_*(T_{rh})} \right)^{1/3} \frac{\Gamma_{\psi \rightarrow \vartheta\vartheta}}{\Gamma_{\psi \rightarrow \text{SM}}}$$

[Higaki, Takahashi: 2012]

[Cicoli, Conlon, Quevedo: 2013]

SM Realization and Scenarios

- SM D7-branes cannot wrap τ_s [Blumehagen, Moster, Plauschinn: 2007] nor τ_φ (FI terms would make it too heavy)
  introduce τ_{SM} and τ_{int}

$$\mathcal{V} = \tau_b^{3/2} - \tau_s^{3/2} - \tau_\varphi^{3/2} - \tau_{SM}^{3/2} - \lambda(\tau_{int} - \tau_{SM})^{3/2}$$

- D-term stabilization ($\xi_{FI} = 0$):

$$\tau_{SM} = \lambda^2(\tau_{int} - \tau_{SM})$$

- $\lambda = 0$  $\tau_{SM} \rightarrow 0$: SM on D3-branes at singularity
- $\lambda \neq 0$  τ_{int} fixed in terms of τ_{SM} , still flat. Fixed by loop potential [Cicoli, Mayrhofer, Valandro: 2011]:

$$V_{loop}(\tau_{SM}) = \frac{W_0^2}{\mathcal{V}^3} \left(\frac{\gamma}{\sqrt{\tau_{SM}}} - \frac{\delta}{\sqrt{\tau_{SM} - \sqrt{\tau_s}}} \right) \quad \text{img alt="blue arrow" data-bbox="608 645 698 675} \quad \text{SM on D7-branes}$$

- 3 Scenarios:

- i. Scenario I: SM on D7, τ_φ wrapped by hidden-sector D7s
- ii. Scenario II: SM on D7, τ_φ *not* wrapped
- iii. Scenario III: SM on D3

Scenario I

$$\Gamma(\varphi \rightarrow \gamma_h \gamma_h) \simeq \frac{\mathcal{V}}{64 \pi} \frac{m_\varphi^3}{M_p^2}$$

$$N_\varphi \simeq \frac{2}{3} \ln \left(\frac{H_{inf}}{\Gamma_{\varphi \rightarrow \gamma_h \gamma_h}} \right) \simeq 1$$

$$\Gamma(\chi \rightarrow hh) \simeq \left(\frac{c^2 W_0^3 \sqrt{\ln \mathcal{V}}}{32 \pi} \right) \frac{M_p}{\mathcal{V}^{5/2}}$$

[Cicoli, Hebecker, Jaeckel, Wittner: 2022]

$$N_\chi \simeq \frac{2}{3} \ln \left(\frac{H(t_{eq})}{\Gamma_\chi} \right) \simeq 3$$

$$\frac{\Gamma(\chi \rightarrow \nu_b \nu_b)}{\Gamma(\chi \rightarrow hh)} \ll 1$$

$$\Delta N_{\text{eff}} \simeq 0$$

Inflation

Inflaton
Domination

Radiation
Domination

Volume
Domination

Radiation
Domination

Matter
Domination

Dark
Energy

$$N_e \simeq 53$$

$$\varphi_* \simeq 0.2$$

$$\mathcal{V} \simeq 10616$$

$$n_s \simeq 0.9765$$

$$r \simeq 1.7 \times 10^{-5}$$

$$T_{rh} \simeq 4 \times 10^{10} \text{ GeV}$$

Scenario II

$$\Gamma(\varphi \rightarrow AA) = \left(\frac{N_g W_0^3 (\ln \mathcal{V})^{9/2}}{8\pi} \right) \frac{M_p}{\mathcal{V}^4}$$

$$N_\varphi \simeq \frac{2}{3} \ln \left(\frac{H_{inf}}{\Gamma_{\varphi \rightarrow AA}} \right) \simeq 8$$

$$\Delta N_{eff} \simeq 0.14$$

$$\frac{H(t_{eq})}{\Gamma(\chi \rightarrow hh)} \ll 1$$

$$N_\chi = 0$$

Inflation

Inflaton domination

Radiation
Domination

Matter
Domination

Dark
Energy

$$N_e \simeq 52$$

$$\varphi_* \simeq 0.2$$

$$\mathcal{V} \simeq 10525$$

$$n_s \simeq 0.9761$$

$$r \simeq 1.7 \times 10^{-5}$$

$$T_{rh} \simeq 3 \times 10^{12} \text{ GeV}$$

Scenario IIIa

$$\Gamma(\varphi \rightarrow \gamma_h \gamma_h) \simeq \frac{\mathcal{V}}{64 \pi} \frac{m_\varphi^3}{M_p^2}$$

$$N_\varphi \simeq \frac{2}{3} \ln \left(\frac{H_{inf}}{\Gamma_{\varphi \rightarrow \gamma_h \gamma_h}} \right) \simeq 1$$

$$\Gamma(\chi \rightarrow H_u H_d) = \frac{Z^2}{24 \pi} \frac{m_\chi^3}{M_p^2}$$

$$N_\chi \simeq \frac{2}{3} \ln \left(\frac{H(t_{eq})}{\Gamma_{\chi \rightarrow HH}} \right) \simeq 10.5$$

$$\frac{\Gamma(\chi \rightarrow \vartheta_b \vartheta_b)}{\Gamma(\chi \rightarrow H_u H_d)} \simeq 2Z^2$$

$Z \simeq 2$

$$\Delta N_{\text{eff}} \simeq \frac{1.43}{Z^2} \simeq 0.36$$



$$N_e \simeq 51.5$$

$$\varphi_* \simeq 0.2$$

$$\mathcal{V} \simeq 10447$$

$$n_s \simeq 0.9757$$

$$r \simeq 1.8 \times 10^{-5}$$

$$T_{rh} \simeq 10^8 \text{ GeV}$$

Scenario IIIb

$$\Gamma(\varphi \rightarrow \vartheta_b \vartheta_b) \simeq \left(\frac{W_0^3 (\ln \mathcal{V})^{9/2}}{64 \pi} \right) \frac{M_p}{\mathcal{V}^4}$$

$$N_\varphi \simeq \frac{2}{3} \ln \left(\frac{H_{inf}}{\Gamma_{\varphi \rightarrow \vartheta \vartheta}} \right) \simeq 11$$

$$\Gamma(\chi \rightarrow H_u H_d) = \frac{Z^2 m_\chi^3}{24 \pi M_p^2}$$

$$N_\chi \simeq \frac{2}{3} \ln \left(\frac{H(t_{eq})}{\Gamma_{\chi \rightarrow HH}} \right) \simeq 0.5$$

$$\frac{\Gamma(\chi \rightarrow \vartheta_b \vartheta_b)}{\Gamma(\chi \rightarrow H_u H_d)} \simeq 2Z^2$$

$Z \simeq 2$

$$\Delta N_{\text{eff}} \simeq \frac{1.43}{Z^2} \simeq 0.36$$



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Same predictions as in Scenario IIIa!

Conclusions

- New inflationary model: **Loop Blow-up Inflation**
- Inflaton: blow-up mode with potential from **1-loop corrections**
- **Loop corrections** from BHP conjecture and low-energy EFT considerations

- Inflationary potential:

$$V(\varphi) \simeq V_0 \left(1 - \frac{c_{loop}}{\mathcal{V}^{1/3} \varphi^{2/3}} \right)$$

- Interesting predictions:

1. **Microscopic parameters:** $\mathcal{V} \sim \mathcal{O}(10^4)$, $\varphi_* \simeq 0.2$ with EFT under control

2. **Number of e-foldings:** $51.5 \lesssim N_e \lesssim 53$

3. **Cosmological Parameters:** $n_s \simeq 0.976$, $r \simeq 2 \times 10^{-5}$, $0 \lesssim \Delta N_{eff} \lesssim 0.36$

Thank you for your attention!

Control over EFT

- EFT always under control: τ_φ is **within Kähler cone** throughout inflation.
- For $51.5 \lesssim N_e \lesssim 53$: $\mathcal{V} \sim \mathcal{O}(10^4)$, $\varphi_* \simeq 0.2$ \longrightarrow **Need to check!**

- **Explicit CY example** [Cicoli, Krippendorf, Mayrhofer, Quevedo, Valandro: 2012]:

$$\mathcal{V} = \frac{1}{9} \sqrt{\frac{2}{3}} (\tau_b^{3/2} - \sqrt{3} \tau_s^{3/2} - \sqrt{3} \tau_\varphi^{3/2}) \quad \text{with} \quad \tau_b = \frac{27}{2} t_b^2, \quad \tau_s = \frac{9}{2} t_s^2, \quad \tau_\varphi = \frac{9}{2} t_\varphi^2$$

- **Kähler cone conditions:**

$$t_b + t_s > 0, \quad t_b + t_\varphi > 0, \quad t_s < 0, \quad t_\varphi < 0$$

- **Canonical normalization:**

$$\tau_\varphi = \left(\frac{\sqrt{3}}{2}\right)^{2/3} \mathcal{V}^{2/3} \varphi^{4/3} \simeq \left(\frac{1}{18\sqrt{2}}\right)^{2/3} \tau_b \varphi^{4/3}$$

- **At horizon exit:**

$$\frac{|t_\varphi|}{t_b} = \left(\frac{1}{2\sqrt{6}}\right)^{1/3} \varphi_*^{2/3} \simeq 0.6 \varphi_*^{2/3} \simeq 0.2 \quad \longrightarrow \quad \text{Inside the Kähler cone!}$$

Comments on Spectral Index

- Scenario I:

$$n_s \simeq 0.9765, \Delta N_{\text{eff}} \simeq 0 \quad \overset{\sim 2\sigma}{\longleftrightarrow} \quad n_s = 0.9665 \pm 0.0038 \quad 68\% \text{ CL}$$

[Planck: 2018]

- Scenario II:

$$n_s \simeq 0.9761, \Delta N_{\text{eff}} \simeq 0.14 \quad \overset{\sim 2\sigma}{\longleftrightarrow} \quad n_s = 0.9589 \pm 0.0084 \quad 68\% \text{ CL}$$
$$N_{\text{eff}} = 2.89^{+0.36}_{-0.38}$$

[Planck: 2018]

- Scenario III:

$$n_s \simeq 0.9757, \Delta N_{\text{eff}} \simeq 0.36 \quad \overset{\sim 1.2\sigma}{\longleftrightarrow} \quad n_s = 0.983 \pm 0.006 \quad 68\% \text{ CL}$$
$$\Delta N_{\text{eff}} = 0.39$$

[Planck: 2015]

- Possible improvements: include additional corrections

- F^4 corrections [Cicoli, Licheri, Piantadosi, Quevedo, Shukla: 2023]
- Subleading loop corrections